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A BIOMECHANICAL ANALYSIS OF THE UPPER LIMB SEGMENTS DURING  
THE SOFTBALL PITCH

by



MARION JOYCE LINDSAY ALEXANDER

A THESIS

SUBMITTED TO THE FACULTY OF GRADUATE STUDIES AND RESEARCH  
IN PARTIAL FULFILMENT OF THE REQUIREMENTS FOR THE DEGREE  
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IN

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FACULTY OF GRADUATE STUDIES AND RESEARCH

The undersigned certify that they have read, and  
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for acceptance, a thesis entitled .A BIOMECHANICAL ANALYSIS...  
.OF THE UPPER LIMB SEGMENTS DURING THE SOFTBALL PITCH.....  
.....  
submitted by ..MARION JOYCE LINDSAY ALEXANDER.....  
in partial fulfilment of the requirements for the degree of  
DOCTOR OF PHILOSOPHY





## ABSTRACT

The purpose of this study was to determine the relative velocities of the three segments of the upper extremity during a highly skilled ballistic movement. The skill chosen for analysis was the windmill pitch in the game of softball.

Four highly skilled softball pitchers, two female and two male, were the subjects in the study. Of the ten pitches performed by each of the subjects during the testing session, the two pitches of each subject with the highest velocity were chosen for detailed analysis. The subjects were filmed by two cameras, one placed to the side at right angles to the direction of the pitch, and the other one placed to the rear of the subject. The subjects also pitched from a force platform, so that the reaction of the pitcher on the ground could be recorded. The records from the two cameras and the force platform were synchronized by means of an electric timer, such that the speed of the timing flashes was altered at a point in the pitch.

Other problems investigated in this study included the determination of the coordinates of the segmental endpoints of the pitching arm in three-space, and the comparison of these with the values obtained from the planar analysis. Also, a method was devised to calculate the magnitudes of the angular velocities of the lower arm segment which could be utilized to determine these parameters for any of the other body segments. In particular, the angular velocities



of particular interest were those occurring around the longitudinal axis of the segment, which were believed to be of importance in this skill.

Computer programs were written to calculate the kinematic and kinetic parameters of the segments of the upper extremity during this skill from the digitized film data. The spatial coordinates of the segmental endpoints were determined by use of an available computer program, and the X, Y, and Z velocity components of each of these points were determined and graphed. The pitching arm was analyzed further during the frames surrounding release of the ball to determine the magnitudes of the angular velocities around the three principal axes of the lower arm segment.

The following are the main results of the study: (1) the force platform and the calculated forces from the mass center accelerations produce similar X and Y force records, (2) there is a definite sequence of segment motions which characterizes the highly skilled performers analyzed in this activity, (3) the largest, most proximal arm segment reaches maximum velocity at the earliest point in the skill, followed by the peak velocities of the distal segments, (4) the proximal segment also attains peak acceleration earliest in the skill, followed by the peak accelerations of the other two segments, (5) the directions of the force and acceleration vectors are almost 90 degrees different from those of the velocity and displacement vectors for these segments (6) the most forceful muscle action occurring in





this skill is that produced by the shoulder extensors in decelerating this segment prior to release of the ball (7) the three dimensional coordinates produced from the film in this study are fairly accurate (+ or - 7%) estimates of these points, (8) the Z-component of the velocity of the arm segmental endpoints is relatively small (approximately twenty per cent of the X and Y values), and probably relatively unimportant in this skill (9) the peak value for the angular velocity of the pronation movement of this skill occurs at the same instant as the peak velocity for the elbow flexion movement.



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## CHAPTER I

### THE PROBLEM

#### Introduction

"I often say that when you can measure what you are speaking about and express it in numbers you know something about it; but when you cannot measure it, when you cannot express it in numbers, your knowledge is of a meagre and unsatisfactory kind" (Kelvin, 1891, quoted by Panjabi and White, 1971:203).

The science of biomechanics is a relatively new science compared with the other disciplines of physical education. As Nelson (1973:336) has stated: "Within the field of sport and physical education, however, biomechanics has progressed slowly and today remains relatively underdeveloped. This lack of development is characterized by a limited number of qualified researchers, a shortage of well equipped, productive laboratories, a small number of graduate programs training doctoral students and a general lack of identity in the scientific community." The first biomechanics conference of note in North America was held at Indiana University in 1970 (Cooper, 1971), and the First International Conference was held in 1967 (Wartenweiler, 1968). As Nelson further noted (1973:337): "The 1st International Seminar on



Biomechanics held in Zurich, Switzerland, in 1967 was a milestone for the emerging discipline of sport biomechanics." Because the science is itself so new, it is only comparatively recently that biomechanics researchers have had the technological tools to acquire large amounts of accurate data with which to describe human body motion. Some of the most useful tools used in biomechanics research include precision high speed 16 mm movie cameras, electromyography recorders, force platforms, electrogoniometers, and sophisticated multi-channel recording devices to record and integrate data from these sources. Some of the most dramatic advances have been made in film analysis procedures. Where at one time all film data digitizing and reduction was done by hand, much of this work is now automatized. By using a digitizing board attached to a digital computer, it is now possible to analyze large amounts of film data in a relatively short period of time.

Many of the recent studies in biomechanics use the mathematical methods of engineering mechanics to describe and calculate the kinetic and kinematic parameters of a performance from digitized film data (Miller, 1970; Dillman, 1970; Jensen, 1972). Many of the earlier studies concerned with skill analysis used a qualitative approach, in which the major movements of the skill were described qualitatively rather than quantitatively. Those researchers who used a quantitative approach often concluded that the joint or segment with the largest final velocity was the





greatest contributor to skilled performance in the activity. A series of recent studies from the university of Iowa (Hay et al., 1975a, 1975b, 1977) have determined that this is not often the case. In fact, the joint or segment with the highest velocity may have received this velocity from a preceding movement. In this case, this joint is only a transmitter of some previously-produced velocity, and the movement of this joint should not accurately be described as the "major contributor" to performance, as it was by Cooper (1972:124). In order to determine the relative contribution of each of the body segments to a skill, it is necessary to use a segmental analysis approach, whereby the kinematic and kinetic characteristics of each of the segments are determined (Plagenhoef, 1971).

Another area of biomechanics research which has recently been explored by means of the segmental analysis method of engineering is that of muscle analysis, that is determination of the muscle action which is occurring during a particular joint movement. Plagenhoef (1971:55) has described body motions in which muscle action at one joint can produce muscle action at an adjoining joint just opposite to what the movement indicates. An example of this is seen in the standing broad jump where hip extension is so great that the knee flexors are dominant even though the legs are straightening. This is due to the fact that the motion of a segment affects both ends of the segment, so that when the hips are forcefully extending the thigh





segment is moved in that direction. Since the knee joint is at the other end of the segment, it also moves in the direction of the hip extension, which may also be the direction of knee flexion. Although the movement at the knees is extension, the moment at the end of the thigh segment may be one towards flexion. A further example of the misconceptions in muscle analysis which are common in the analysis of skills is described by Gideon Ariel in an article by Moore (1977). In a study of major league pitchers, Ariel found that the forearm flexor muscles which act to flex the wrist have practically no contribution to make to this skill. The force of the pitch is built up by the legs and trunk rotation, and the hand is like the end of a whip. The wrist movement is far faster than any muscle can contract, so it is not really useful to attempt strength training of the wrist, according to Ariel. This could only be determined conclusively by comparing accurate estimates of muscle contraction times for the wrist flexor muscles with the actual linear velocities of the insertions of these muscles in the hand. A study of this type would of course be limited by the anatomical and physiological data available.

Another common problem in skill analysis has been the difficulty of accurately describing the movements which contribute to skilled performance. Since most of the previous research has been single-camera, two-plane research, only movements occurring in this plane (most commonly the sagittal plane) have been described. A common



example of errors in this area is seen in the usual descriptions of wrist movements in racquet sports. In badminton, for example, this movement has traditionally been referred to as "wrist snap", or the "uncocking of the wrist". recent investigations by Waddell and Gowitzke (1977) have determined that the primary force-producing movement in the badminton overhead smash is rotation of the forearm (pronation) accompanied by shoulder rotation, not the movements of flexion and extension that are usually described in this context. The final force-producing movement which provides so much of the force is not likely the wrist flexion movement described by such authors as Cooper and Glassow (1973) --- this wrist flexion is probably quite minimal. The most important movement in this skill is likely the forceful forearm pronation just prior to release of the ball, as found by Waddell and Gowitzke (1977) in the badminton overhead clear. It is notable that even though the majority of textbooks describe the pitch incorrectly, most highly skilled performers manage to execute it correctly regardless of these descriptions. As noted by Harris (1978:84): " --- players who have been taught to play overhead strokes according to the prevailing literature, manage to do so in spite of what they are being taught".

A further source of error in skill analysis is seen in calculation of acceleration at the joints. When calculating these accelerations, both the tangential and the normal components of the acceleration must be calculated. The





resultant of these often produce unpredictable force directions. As Plagenhoef(1966:111) has noted: "A slow moving but greatly accelerating segment can have a force direction almost 90 degrees different than if the segment were moving at a uniform velocity." It is clear that the intricate patterns of movement of the skilled performer cannot be described accurately without detailed analysis of each segment and its effects on the adjoining segments.

There has been much written in the literature of movement analysis and kinesiology regarding the pattern of limb movements during ballistic sports activities (Rasche and Burke,1974; Wells and Luttgens,1976; Broer,1973; Cooper and Glassow,1972). Ballistic sports activities include those skills characterized by high-velocity limb movements. Wells and Luttgens(1976) have described a ballistic movement as one which is initiated by vigorous muscular contraction and completed by momentum. These movements are characteristic of throwing, striking, and kicking, and are found in virtually all the sports and activities which physical educators are responsible for teaching.

The movement chosen as a representative ballistic skill in the present investigation was the windmill pitch in the game of softball, since it has the required characteristics of a multi-segment movement of relatively high velocity. Much of the literature is in disagreement as to the general pattern of segment motion during high velocity limb movement. Several authors (Broer,1973; Cooper and



Glassow, 1972) described this limb movement in terms of "successively added segmental velocities", while others (Rasche and Burke, 1974; Wells and Luttgens, 1976) described it as "sequential joint movement, from proximal to distal segments." The movement sequence has also been described as a sequence in which the joints begin their acceleration when the preceding joint has reached its maximum acceleration, so that the end of the lever is constantly being accelerated by successive segments (Bunn, 1972). Recently, however, several authors have contradicted these earlier descriptions of this movement pattern, and have suggested that optimal velocity at the distal end of a lever is produced by a 'slowing down' of the proximal segments. It is clear that more study is needed to determine the exact sequence of segment movements in a common ballistic skill.

The skill of windmill pitching in softball was chosen for analysis for several reasons, one of the most important of which is the universal and increasing popularity of the sport in Canada. It has been estimated that there are more Canadians of all ages and social classes playing softball than any other single sport. A popular magazine has recently reported that: "Softball is the game that everyone plays and hardly anyone watches, the game that is to baseball what checkers is to chess. And it is my guess that more Canadians have played softball than have skated, curled or jogged" (O'Malley, 1977:65). As well, softball is a sport in which Canadian teams are among the top in the world. The Men's





World Champions for the past several years have been Canadian teams (O'Malley, 1977) and the Canadian Women's Champions have ranked among the top four in the world for the past five years.

Several authors have stated that the softball pitcher is the most important player on the team, and that the skill of the pitcher may account for up to seventy five per cent of the success of a team (Dobson and Sisley, 1971; Kneer and McCord, 1976). With the current popularity of this game, and the importance of the skills of the pitcher to a team's success, it is clear that a closer examination of this skill would be valuable to a large number of participants. Further, the skill of softball pitching has always been fascinating to both players and spectators alike, as noted by O'Malley (1977): "It is this aspect of softball (pitching) which fascinates me, how anyone can throw a ball that big that fast with an underhand motion one might use to plop wet tea bags into the sink. It looks incredible, like a man jumping 20 feet into the air.---the underhand throw is natural and the overhand baseball throw is an aberration (O'Malley, 1977:65)". It is hoped that the present study will give greater insight into the factors which comprise a skilled performance in softball pitching, as a high velocity ballistic movement.



### The Problem

The purpose of this investigation was to examine the motions of the three segments of the arm during the delivery of the ball in the softball pitch, and thereby describe the relative motions of each of the segments during a skill of this type. There are some questions among kinesiologists and biomechanics researchers regarding the three segments which are contributing to the velocity of the ball during the softball pitch. Are they accelerating, decelerating, or maintaining a constant velocity through release? These questions extend to the angular motions of the limbs as well, whether their angular accelerations are increasing, decreasing, or constant. Since the objective of the softball pitch is to release the ball at the optimal velocity of the hand (in most cases), loss of velocity of the proximal segments would be inefficient. It seems logical that the upper arm segment and the lower arm segment should maintain their maximal velocity through the release of the ball. This should ensure maximum release speed. However, several authors have recently suggested that it is desirable to have the proximal segments slow down prior to release during a throw.

Plagenhoef (1971:55) described the extent of the contribution of each body segment as follows: "The movement of the segment nearest the fixed point should accelerate and increase velocity; then the deceleration of that first segment aids the increase in velocity of the next





segment. The same sequence takes place so that the deceleration of segment 2 aids the increase in velocity of segment 3. The timed sequence of one segment helping the next will produce the maximum velocity of the last segment with a minimum of muscle force at each joint." Broer (1973:87) continued with this theory when she noted: "This deceleration of the preceding segment acts to stabilize the axis for the motion of the second segment. In sequential action the first segment rotates around its axis, the second rotates around the moving end of the first segment, and the third around the moving end of the second. Thus, to gain maximum rotation of the second around its axis (the end of the first), the first segment must decelerate." Gideon Ariel, quoted by Moore (1977) in a recent popular magazine article, agreed with the previous authors when he stated: "It's vital to have everything stopping in the discus. In the best throws, we found a pattern. It is like using a fly rod, or snapping a towel. You have to decelerate the heavy parts, the legs and the trunk, so you can accelerate the light parts, the arm and the discus." This principle of deceleration of preceding body parts was summarized by Plagenhoef (1966) as follows: "The velocity of a given segment can be increased by decelerating the adjoining segment. (In whole body motions where a peak velocity is desired in the hands, the properly timed stopping action of each segment from foot to hand produces the best results)". It is clear that this question of relative segment motions





requires further investigation, as no accurate data describing the relative motions of the arm segments in a throwing motion is presently available.

The method most commonly used in current biomechanics research to examine questions of this type is known as segmental analysis. Each segment of the body is viewed as a link of variable length and weight for each subject, and segment movements can be described as motion about axes created by the joints (Jensen, 1972). The motions of segments may be described in terms of the displacements, velocities, and accelerations of their endpoints and of their respective centers of gravity, as well as by the angular equivalents to these. As well, from these kinematic parameters the magnitudes of the forces acting on these segments and at the joints may be estimated.

A further problem to be investigated in this study was the relative contributions of rotational movements of the segments around their own longitudinal axes to ball velocity. Little research has been located which examined the rotational movements of the body segments due to the difficulties in accurately measuring these from two-dimensional data. However, it is possible to measure accurately these rotations around the longitudinal axis of the segment by means of two camera filming procedures, whereby the data from these two cameras can be coordinated to produce three dimensional coordinates of any of the points on these segments. No previous attempts to actually



quantify the amount of shoulder medial rotation and forearm pronation present during the softball delivery were located. It is likely, however, that these movements are major contributors to the force in this skill.

Another question which was investigated in this study is the accuracy of the calculated ground reaction forces from film coordinate data, compared to force platform readings. The vertical and horizontal components of the acceleration of the body's center of gravity provides estimates of the forces being exerted down and back against the ground during the performance of a skill. Assuming that the force platform readings of these same forces are accurate, these readings may serve as checks on the accuracy of the calculations from film data.

A final question which was examined within the framework of the present study was the relationship between the two dimensional data produced from one camera placed at right angles to the direction of the movement, and the data produced from three-dimensional coordinates of the same data. This may give some insight into the actual amount of error present in the traditional one-camera, two dimensional analysis of physical skills. For example, in the calculation of the velocity of the hand during the release of the ball, a one camera view does not take into account any movements of the hand in the plane at right angles to the lens of the camera. It is possible that these lateral and rotational movements at the joints are important contributors to the



final velocity of the ball. A two camera view of the same skill, however, gives a more accurate estimate of the position of the hand in space, and so any movements which occur out of the sagittal plane are considered in the determination of the real velocity of the hand. It is hoped that the present study will also provide a comparison of the relative accuracy of two dimensional analysis of an activity which is actually occurring in three planes.

#### Statement of the Problem

The purpose of this study was to examine the motions of the three segments of the arm during the delivery of the ball in the softball pitch. In particular, the following objectives were set:

1. To examine the relative motions of the upper limb segments during the execution of the softball windmill pitch.
2. To examine the forces acting at each of the three joints of the upper limb during the windmill softball pitch.
3. To determine the direction of the moments acting at each of the joints during the pitch.
4. To determine the body movements which are most





significant in contributing to the velocity of the ball at release.

5. To estimate the muscle actions during the pitch.

### Subproblems

1. To examine the relationship between the forces as measured by the force plate tracings, and the same forces as measured from film data.

2. To examine the relationship between certain kinematic parameters as calculated from two-dimensional film data, and the same parameters as measured from three-dimensional coordinates.

3. To examine the rotational motions of the three segments of the upper limb.

4. To develop a technique for the production of accurate three-dimensional coordinates from film data, and to analyze these coordinates in a meaningful manner.

### Delimitations

1. The analysis of the upper limb segment motions of a ballistic movement was limited to the single skill of softball pitching.





2. The analysis was limited to the pitching motions of four highly skilled softball pitchers.



## CHAPTER II

### RELATED LITERATURE

The literature related to this study was classified into seven topical areas:

1. General Segmental Analysis Techniques
2. Analyses of Ballistic Skills
3. Upper Extremity Analyses
4. Data Smoothing Techniques
5. Analyses of Softball Pitching.
6. Three Dimensional Cinematographic Techniques.
7. Force Platform Studies.

#### General Segmental Analysis Techniques

Many of the earlier researchers in physical education analyzed sports' skills on a qualitative basis--they simply described what the performance looked like to a trained observer. This method obviously lacks accuracy, as the results are dependent upon the observational powers of the researcher. Recent investigators have used the segmental method of analysis of human movement, in which each of the body segments is considered as a separate body for the purposes of analysis (Dillman, 1971; Miller and Nelson, 1973). This method is derived from the methods of engineering analysis, whereby all the forces acting must be quantified and included in the analysis.



Most of the human body mathematical and segmental analysis techniques were derived from the United States space research program (Kane, et al., 1972; Kane and Scher, 1970; Dempster, 1955). One of the most often quoted studies from this program is that produced by Hanavan (1964), which has been used extensively by subsequent researchers in sports' biomechanics (Miller, 1970; Plagenhoef, 1971). Hanavan produced a mathematical model for predicting the inertial properties of a human body in various positions. He used twenty-five standard anthropometric dimensions to predict an individual's center of gravity, the moments of inertia and products of inertia about axes through the center of mass, principal moments of inertia about the principal axes through the center of mass, and the orientation of the principal axes. One of the reasons for the study was to make more efficient use of a propulsion device known as a Self Maneuvering Unit, which was designed for use outside a space vehicle. Undesirable rotations were produced when the thrust vector did not pass through the center of mass of the system, or the torque was produced about an axis other than a principle axis. It was therefore vital to determine the exact positions of the center of mass and the principle axes of the human body, since to that time no such studies had been attempted. Hanavan concluded that his model was capable of predicting these parameters accurately enough to be useable in subsequent space program research.

A later attempt at mathematical modelling of the human





body was produced by Huston and Passerello (1971), who developed a set of governing equations to describe human body motion which were applicable to a wide variety of situations. They noted that a principal source of difficulty in developing these equations was the complex geometry due to the irregular shape of the body and its' wide range of possible motions. They used the segment models as described by Hanavan (1964), and they described a series of reference frames to locate the positions of each of the segments within the model. They used a number of configuration charts to enable them to express unit vectors of one reference frame in terms of unit vectors of another reference frame; and another technique known as 'shifters' to relate the scalar components of vectors between different reference frames. They then developed a set of kinematical equations to describe the motions of each of the segments. Three sample motions were studied to illustrate the use of these equations: a lifting motion in two different gravitational fields (earth and moon), a kicking motion in swimming, and a kicking motion by a vertically suspended man. In most cases the input and output curves of the motion were similar, indicating that the mathematical modelling was fairly accurate for these particular movements.

The most popular method of acquiring human motion data used by sports' biomechanics researchers is by cinematography--usually by use of high speed 16mm motion pictures. As well as mathematical modelling from



anthropometric measures, biomechanics researchers have devised numerous methods of measuring and quantifying human movement parameters. Researchers in other fields have used several other methods of data gathering, some of which have been described by Ayoub(1972). He has described the use of accelerometers to calculate the forces being exerted during movement, as well as the use of potentiometers at the joints to record the range and velocity of movement. The signals from these devices can be recorded on a strip chart recorder. Padgaonkar(1975) also described a technique of kinematic analysis using accelerometers to measure linear accelerations, and then computation of angular accelerations from this data. He stated that although it theoretically requires a minimum of six linear accelerometers to determine the kinematics of a rigid body in three dimensions, attempts using only six were unsuccessful in accurately determining these kinematic parameters. An alternate method of determining angular accelerations was suggested based on the placement of nine accelerometers on the segment. He noted that the key to the accurate solution to the problem of accurately describing the motions is the choice of location of the accelerometers. If the solutions are then accurate, the resulting acceleration values may then be integrated to produce estimates of the angular velocity and displacement. This method may only prove useful for motions involving low values of linear and angular acceleration data.

Ramsey(1968) developed a device which mounted





externally on the human subject for the purpose of measuring the kinematic characteristics of his limbs.

Another study which utilized accelerometers to measure the accelerations of a segment was that of Cavanagh and Landa(1976) in an examination of the karate chop. They utilized the methods of cinematography, accelerometry, and electromyography to study the preimpact movements of the arm during karate chops intended to break several boards. Their kinematic analysis showed a sequential pattern of action at the shoulder and elbow joints, with shoulder action nearly complete before the elbow extension began. The linear acceleration of the forearm at the wrist was measured by an accelerometer mounted over the radial styloid. This component of radial acceleration was found to be a maximum of 7 g as recorded by direct measurement from the accelerometer. As well, "a second estimate of acceleration was calculated from numerical double differentiation and this showed considerable variation from the accelerometer measurement (1976:610)". The authors published graphical comparisons of the acceleration data derived from these two experimental sources, and they concluded that "The discrepancies both in amplitude and in phase are considerable, casting further doubt on the process of double differentiation (1976:615)". This 'Exoskeletal Kinematometer' was developed for measuring angular displacements of the joints of the upper limbs by the use of potentiometers at these joints which are sensitive to





changes in joint angles. The displacement data from the Kinematometer provided the information necessary for the calculation of instantaneous velocity, acceleration, potential and kinetic energy, force, torque, linear impulse, and angular impulse. He determined that angular impulse was the best single measure of human effort and could provide the most reliable quantification of this effort.

Zernicke(1977) has described the techniques of segmental analysis as they may be applied to analysis of cinematographic data, although his study was concerned with the analysis of a particular weight lifting skill. The sequence of film images was projected onto a digitizer, and rectangular coordinates were digitized for each of the segmental endpoints as well as the center of gravity of the weight. These coordinates were analyzed by computer programs which included the calculation of center of gravity locations and segmental inclinations for each time interval between frames. Following this, "Film-derived kinematic segmental linear and angular accelerations and mass parameter estimates were incorporated into the kinetic equations of motion for a mathematical model of the lifter" (Zernicke,1977:179). The net forces and moments of force at each joint were calculated from the equations of Newtonian rigid-body dynamics. Each of the segments was considered to be a rigid body, and for each segment the sum of the horizontal and vertical forces was equal to the product of the segment mass and the corresponding horizontal and



vertical acceleration of that segment's center of mass. Also, the sum of the moments of force was equal to the product of the segment's angular acceleration and the appropriate moment of inertia about the segment's center of gravity. This computational model was validated by comparing the computed vertical reaction forces at the foot, with those measured from a force platform. The mean agreement between the two techniques was found to be greater than 93.0 per cent.

Sutherland and Hagy (1972) conducted a study of the leg movements during gait, as recorded on movie film. One of the problems they discussed was that of estimating the amount of medial and lateral rotation occurring in the leg segments and the pelvis during locomotion. By calculating the angle between measurements of a certain distance taken from the film from the front camera, and the angle between the same distance taken from the side camera, the investigators had developed an accurate estimate of these rotations. These techniques are especially useful when examining the differences between normal and pathological gait, and may be used in analysis of the rotations in any of the body segments. It may then be possible to adapt this technique to estimate the rotations of the arm segments during a throwing motion.

One of the earliest physical education researchers to advocate the use of segmental analysis in examining sports skills was Plagenhoef (1966). In this early article he





described the steps necessary to follow in using this technique to accurately quantify film data. These steps included: determining the length and weight of each body segment, filming the motion, tracing the entire motion, locating the center of gravity and radius of gyration for each segment, and calculating the required parameters. Plagenhoef (1971) described these techniques in greater detail in a subsequent book. In this publication, he outlined the procedures for segmental analysis with much more explanation, and as well he included the equations of motion for each of the segments in a multi-segment model. His analysis differed from that used by other investigators in that he included a term for the Coriolis acceleration in his equations--this term has traditionally been neglected by most sports' researchers.

The Coriolis effect is simply the tendency of an object to drift sideways during movement on the earth--to the right in the northern hemisphere, and to the left in the southern hemisphere. This motion is due to the counterclockwise spinning of the earth around its longitudinal axis, so that objects moving across the surface of the earth tend to move slightly with respect to their original path. As noted by McDonald (1952) in an article on the subject: "This tendency to drift sideways--is due simply to the rotation of the earth, and it appears in all motions as soon as we refer those motions to any coordinate system fixed with respect to the earth (eg., the latitude-longitude grid)". He is of the





opinion that the effects of this force should be included in the examination of movements, as he noted: "All things that move over the surface of our spinning earth, whether birds, winds, ----bullets, or rockets are inevitably subjected to this effect as we view them in our terrestrial coordinate systems. Even when man gets away from his planetary home and stakes out better behaved coordinate systems in interplanetary space, he will not be able to omit consideration of the Coriolis effect from his dynamics (McDonald, 1952:77)". However, contrary to this opinion, it is common practice in the study of the motion of body segments to neglect the velocity and acceleration components due to Coriolis motion between moving links (Ayoub, et al., 1976; Pearson, et.al ., 1963).

The techniques of segmental analysis have been extensively revised and reviewed by Plagenhoef (1966, 1968, 1971, 1973), from his early models encompassing one or two segments he developed models including a large number of segments of the whole body. He has recently described a technique to obtain the joint forces due to motion at all segmental endpoints of the body (Plagenhoef, 1973). Separate frames of whole-body motion as recorded by cinematography were analyzed. A system of body links was chosen which would best define the desired forces and this set of segments was known as the primary chain. The forces due to body segments outside of the primary chain were introduced as external forces at appropriate points.



The procedure was then to solve the smaller systems of links for certain unknowns which were necessary to solve the links of the primary chain. These forces and moments determined from earlier analyses were applied at the appropriate points--from here the final link system can then be analyzed.

This technique was used in a study by Stapleton and Karas(1968) in which the skill of swinging on the parallel bars was analyzed. A free body diagram was constructed of the forces acting on the various joints during this action, and especially the forces acting on the shoulder joint. The moment of force due to the acceleration of the shoulder joint during the upward swing phase of this skill was found to be considerable. An attempt was also made to calculate the moments of inertia of the trunk and legs from the data calculated in this study.

Segmental analysis techniques were also utilized by Susanka(1974) to develop computer programs to analyze sports' movements. His programs were similar to those described earlier by Plagenhoef, in that both accepted as input film data points, and the output from the program consisted of displacements, velocity, and acceleration as a function of time. In addition, horizontal and vertical components of force and their resultants were produced together with joint moments. Susanka then reported analyses of two activities, the pole vault and the shot put, in terms of the kinetic parameters calculated. This study is also





notable in that Susanka is one of the few European researchers engaged in developing segmental analysis techniques and publishing results in this area.

Koniar(1973) has used a slightly different method of analysis of segment motions. He used electrogoniometry and chronography as the methods to determine angular speeds in joints and the initial speed of whole-body movements. The movements analyzed were flexion and extension in the leg joints, and the whole body motion in the vertical jump. Among the findings of this study was that the height of the vertical jump was dependent not only on the timing of the angular speeds at the joints, but also on the summation of these speeds. He found that the peak velocities of the hip, knee and ankle joint extensions occurred in 'one moment', or at virtually the same instant (Koniar,1973:428). The author named this special summation of movements 'the principle of superposition of angular speeds in joints', and he concluded it reflected an exceptional functional ability in highly skilled athletes. These findings are not in agreement with those of Plagenhoef(1966), who found that the peak velocities of the joint motions were sequential, with the proximal segment reaching the peak velocity earliest in the activity.

Nubar and Contini(1961) developed a mathematical model of the human body to illustrate their principle of minimum effort in human motion. This principle was stated by the authors as follows: "A mentally normal individual will in





all likelihood move (or adjust his posture) in such a way as to reduce his total muscular effort to a minimum, consistent with the constraints". Their model was a two dimensional representation of the human figure, made up of only five segments, and the physical properties of the segments are estimated from average values for these parameters. The equations of motion are written in the form of five moment equations, one for each segment, each containing one of the nine unknowns in the system (one of the five segment inclinations, or one of the four unknown joint moments). The equations are further simplified by assuming the static case for the body model, so that all second derivative terms are dropped from the equations. The solution to the equations is several equilibrium positions in which the moment terms are minimized, thus satisfying the constraint. The authors then diagrammed these positions for the five segment model, and it appeared that these mathematically derived positions were very awkward in terms of human comfort or esthetic value. These authors concluded that it may not be practical to attempt to simulate an ideal human posture, since the human body does not really behave as a series of rigid segments.

A similar study to the above was a mathematical model of human gait (Oberg, 1974) in which the body was modelled as a series of seven segments moving through a single plane. The instantaneous position of the body was determined by the X and Y coordinates of the endpoints of the segments, and these points provide the input data to the computer program.



The program then calculated the velocity and acceleration of each of the points of interest, and the moment and force functions are also calculated. The program also produced plots of the model executing a complete cycle of the gait, with certain of the parameters altered. The author suggested that this program may form the basis of a more complex model in which the design was extended to a three-dimensional model, or to one with more of the body segments included in the analysis.

Dillman(1971) used the technique of segmental analysis in a recent study, in which he examined the relative motions of the three leg segments during the recovery phase of sprint running. He simplified earlier segmental models by replacing the muscle force acting to rotate a segment at a joint, by an equivalent joint force and couple acting at the joint. This step simplified the computational procedures required to estimate the muscle forces acting to rotate a joint during a movement, by elimination of one of the unknowns in his equations--the distance from the joint center at which the muscle force acts. Using this model for segmental analysis, Dillman was able to estimate the direction and magnitude of the torques acting at the three joints of the leg during recovery. This enabled him to estimate the amount and type of muscle action occurring in the muscles of the lower extremity during this activity--some of which are quite unexpected in terms of the direction of motion of the segment.





Cavanagh and Gregor (1975) also used this method of analysis in an examination of knee joint torque values during the swing phase of normal treadmill walking. They assumed that the shank and foot were a single rigid body attached to the thigh by a frictionless pin joint. Using this model they calculated the torque at the knee joint; and compared these torque values with the integrated EMG recordings of the muscle activity occurring at this time. They found a marked similarity between the changes in the integrated electromyograms and the net torque-time curves, indicating there was some accuracy in their methods of measuring joint torques.

Some of the more ambitious biomechanics researchers have focussed their energies on the development of whole-body mathematical models to study certain activities. Chaffin (1969) developed a computerized biomechanical model which viewed the whole body as a series of seven links from which reactive forces and torques were computed at each articulation for several different lifting skills. One of the major purposes of his investigation was to estimate the stress in the lower lumbar spine, especially with the addition of external loads on the hands. Another aspect of performance studied was to evaluate the effects of muscle strength in various muscle groups on the ability to lift and hold certain loads. The model described in this study was primarily a static model, so that the investigators were able to analyze only stationary positions, or slow movements





which could be described as a series of static positions.

Another problem which has plagued researchers in biomechanical analysis is that of three-dimensional movements between the two articulating surfaces of a joint. The investigator usually has to assume that the joint is a pinned joint which allows movement in only one plane, when in fact there are other motions occurring between these surfaces. Kinzel, Hall and Hillberry (1972) have designed a mathematical system to measure the total motion between two body segments. They noted that all joints of human and animal bodies permit six degrees of freedom although the motions in one plane may be very small. They were able to measure the extent of this rotation using a method of matrix algebra to facilitate data reduction. The system outlined by these investigators permitted both the study of the relative motion between two body segments, as well as the detailed study of the relative motion between the two articular surfaces of the joint between segments.

Miller (1970) also utilized the principles of segmental analysis in formulating her model of the airborne phase of springboard diving. She used a four-segment model based on Hanavan's model of a movable man (Hanavan, 1964), for which she developed a series of equations to describe the motion of this model in the air after leaving the diving board. Whereas Hanavan's model was composed of fifteen segments, Miller was able to describe the motion of the diver adequately using a composite of four of these segments. The



work of Miller in this study represents one of the few detailed mathematical models of performance produced by a researcher in physical education, and as such represents a milestone in the field of sports' biomechanics. The input data for the computer program consisted of three-dimensional film data from actual dives performed by highly skilled divers; and the necessary body segment parameters were also measured from these performers. Using this data from actual performances, Miller was able to validate the results of her modelling, and once the model was fairly accurate she was able to alter some of the input parameters of the diver. Using this model, it was then possible to alter the positions of the various body segments in the air, and the computer could then calculate the effects of these alterations on the ensuing performance. Although the value of such modelling to our understanding of the components of skilled performance is unquestioned, no similar studies have been attempted since that time--undoubtedly a tribute to the capabilities of this investigator. Possibly in the future, when physical educators are more highly skilled in the techniques of mathematical analysis and engineering mechanics, more such ambitious studies will be attempted.

Gallenstein and Huston(1973) devised a mechanical model based on Hanavan's(1964) model of the human body. This model was used to simulate the motions of a swimmer executing several strokes and kicks. The arms were modelled as the frustrums of elliptical cylinders and cones connected by





pins and ball-and-socket joints. Flat elliptical plates represent the hands, as proposed by Hanavan, 1964. Different angles and velocities for the three segments were input data into a computer program written to simulate the breast stroke, and some estimates were derived of possible optimal angles of the upper limb for this skill.

Several authors have focussed their attention on the measurement of rotation of body segments around their longitudinal axes. This is an important problem in the quantification of human movement, and one that has no consistent solution even today. Eberhart and Inman (1951) have described one solution to this problem, in that they inserted pins into the lateral aspects of the joints of their subjects. They then filmed these subjects during locomotion, and measured the different lengths of the pins at various stages in the gait cycle. Although this technique did result in reasonable estimates of the rotations of the leg segments, it was painful and caused some discomfort to the subjects. The authors noted: "--the possibility that some of the motions are suppressed due to the discomfort of the subjects." Although this technique may have some value in a clinical situation, even then the results likely do not justify the procedure.

Panjabi and White (1971) have described a method of three-dimensional mathematical analysis of the rotation of the spine, which may be adapted to provide a general three-dimensional analysis procedure. This analysis took two





forms: Euler's method, (based on the Euler method of solution of differential equations) which was found to give unreasonable results or none at all when actual experimental data were employed; and a vector method specially modified. They also suggested a method of reporting the rotations of the segments of the spine in terms of helical motions, used if bodies are of irregular shapes and sizes and it is not then possible to compare their translation components of motion. They noted that this experimental technique and mathematical analysis can be "--productively applied to other joints, especially some of the more complex ones like the shoulder, hip and ankle". (1971:210) However, their technique of analysis once again has limited value in the analysis of in vivo movements due to the necessity for extreme precision in measurement the locations of the anatomical landmarks on the vertebrae. They used actual vertebrae in their study, which were carefully marked with steel pins and were then x-rayed and measured from a film analyzer. This technique obviously has little practical significance for the analysis of joint motions as they occur in sports' skills.

Measurement of rotation of body segments was also the topic of a paper by Ramey and Nicodemus (1977). They noted that much of the literature of sport' biomechanics has reported angular kinematic values based on single plane analysis which usually give erroneous values. This is due to the fact that analysis is most often carried out from single



plane film data, when the rotations are actually occurring in three-dimensional space. They described the procedures of transforming reference frames for each type of rotation which is occurring in the segment, so that the angular velocity can then be reported in terms of the components of angular velocity around each one of the three primary axes: X, Y, and Z. They suggested that all angular velocities should be reported in this way, although the methods require a knowledge of three-dimensional vector mechanics, as well as the ability to produce accurate spatial coordinates. It is undoubtedly the latter problem which has prevented sports' biomechanists from reporting rotations in the suggested manner.

### Analyses of Ballistic Skills

Although the use of the segmental analysis techniques of engineering in sports' biomechanics is relatively new, there have been several researchers who have published studies of this nature. This technique as applied to ballistic movements has been outlined in detail by several of these researchers (Dillman, 1971; Miller and Nelson, 1973; Youm, et al., 1973; Roberts, et al., 1974; Zernicke, 1977). The steps to be followed in applying this technique to skills' analysis are as follows:

1. Filming the activity and reduction of film data by some





type of digitizing process.

2. Design of a mathematical model for use in analysis of the film data.
3. Estimation of body segment parameters.
4. Construction of a computer program which smooths the input data, and calculates accurate estimates of the kinematic and kinetic parameters of the activity.
5. Production of graphs of these calculated parameters, and interpretation of these graphs on the basis of the actual film records of the activity.

One of the most popular activities which has been analyzed by these techniques is that of kicking, undoubtedly due to its' simplicity in terms of the amount and range of motion involved. Roberts and Metcalfe(1968) noted that one of the most important joint motions in this skill was that of pelvic rotation, which they estimated from film taken from an overhead camera. The other movements of most importance in this skill were hip flexion and knee extension just prior to contact with the ball. They found that as the thigh passes the perpendicular position, its' angular movement begins to slow and almost stop; at which point knee extension starts and accelerates. This knee extension which does not start until the thigh is past the perpendicular is the chief contributor to speed at and through contact. They also found that foot speed 15ms. before contact is 18 to 24 m/s; and that the resulting ball speed is 5 to 7 m/s faster than the foot. These authors suggested that 'trailing' of





the distal segments during these activities may lengthen the agonist muscles and thus provide for a more forceful contraction via the stretch reflex (1968:318).

Youm,et al.(1973) devised a quantitative method for analyzing a simulated kick motion. They developed a mathematical model of the forces and moments acting on the leg segments during the skill of kicking, and a computer program was written to simulate this model. The authors could then alter the input parameters, and then graph the effects of these changes on the kinematic and kinetic parameters of the motion. The study included a series of graphs illustrating the displacements, velocities, accelerations, and forces and moments acting at the joints during this skill.

Roberts,et al.(1974) continued with this analysis of the skill of kicking, with the objective of attaining more accurate estimates of limb segment accelerations and to then produce more accurate estimates of the muscular forces involved. They attempted to compare vertical ground reaction forces calculated from film displacement measures with vertical reaction forces recorded by a force platform. They found the forces calculated from these two independent means deviated by only 6 per cent, and this disagreement occurred where the force platform record deviates from a smooth polynomial shaped curve. They attributed this lack of agreement to the error inherent in the techniques of curve-fitting, since the curve did not describe the data



perfectly. Another reason for the lack of agreement between the two sources may be due to movement of the trunk, which was not accounted for in the mathematical modelling. The authors concluded that "Cross-comparison and verification of results obtained by different methods appear to be almost essential"(1974:162).

A further study of football kicking was carried out by Macmillan(1975) on the kick used in Australian rules football. Although there seems to be a preponderance of kicking studies published in the literature utilizing similar techniques and methodology, it is notable that all of the above studies were carried out at the same laboratory--at the Department of Physical Education for Women at the University of Wisconsin, Madison. It is likely that an analysis technique for this skill has been developed over the years by these investigators. Macmillan's study focussed on determining the factors which affect the path of the kicked football to the greatest extent. As well as calculation of the linear velocities of each of the segmental endpoints, statistical methods were used to determine that angular velocity at the knee was the major determinant of linear foot velocity. The most notable finding of this study was that the foot velocity had little relationship to the resultant ball velocity, and was consistently lower than ball velocity. Macmillan suggested that the question of momentum transfer at impact from foot to ball needs further study to determine the exact





relationship between these two factors. Kermond and Konz(1978) conducted a similar study to that of Macmillan, and they also concluded that the most important factor in football kicking distance is the force transferred to the ball at impact.

### Upper Extremity Analyses

There have been numerous analyses of the upper extremity published by various researchers, and each of these described a slightly different method to analyze the motions of this limb. Although most of these analyses are single plane, two dimensional analyses, several authors have attempted to develop a method of three dimensional analysis of arm movements. These latter studies have generally been developed in an attempt to measure abduction-adduction of the arm segments, as well as to measure rotation of the arm segments around their longitudinal axes.

The commonly accepted procedure of graphing the angular displacement data with respect to time, and then determining the slope of the curve to calculate velocity was used as long ago as 1931 in a study by Fenn, Brody and Petrelli. They then used the slope of the velocity curve to determine acceleration. The graphs of each of these curves for a simple arm-swinging motion were then superimposed upon one another, and from these curves the relative muscle tensions at certain points in the arm swing were estimated. Although this was a rather rough method of estimating these forces,





the principle behind their method for estimating these forces is still in use today.

One of the earliest attempts at a detailed analysis of the motions of the upper limb was an attempt at three dimensional analysis (Taylor and Blaschke, 1955). It described a single camera technique, in which the subject was photographed from each of the three primary directions while sitting upright in a 'standard posture chair'. The limbs were measured as accurately as possible from the subject, and these same limbs were measured from the photographic data. Using carefully marked anatomical landmarks, the angles at the joints in various positions were calculated by the use of a device called a Kinematic Analyzer. This apparatus was "--a half scale system of joints, members, and scales which is capable of reproducing the major joint rotations of the shoulder, arm, forearm, and hand" (1951:1263). Using this mechanical simulator, it was then possible to estimate the angular displacements of the arm segments, as well as the amounts of pronation-supination occurring in these movements.

Pearson, McGinley and Butzel (1960) described another method of analysis of the motion of the upper extremity in the X-Y plane. They regarded the upper limb as consisting of only two segments--the upper arm and the lower arm plus hand. Angular values were calculated for the displacements of each of these segments throughout a particular motion. The arm motion analyzed in this study consisted of an



underhand throwing motion similar to that used in the present study. The body segment parameters used were calculated empirically by the authors on the subjects they tested. Weights of the hand, forearm and upper arm were determined by the water displacement method. Moments of inertia were estimated by constructing models of the limbs, swinging them as pendulums, and determining the periods of the pendulums. The intent of this model was to compute the forces and torques at the shoulder and elbow joints, to derive an understanding of the muscle actions involved at this joint as well as the amount of strain at these joints. Although the authors were able to compute values for these parameters, it is likely that these values were of questionable accuracy. The main reason for this is their assumption of the lower arm plus hand as a single segment. Since there is considerable movement at the wrist joint in most movements of the arm, the assumption of these two segments as a single rigid body is in error. Movements of the hand segment would erroneously be calculated as movements of the entire segment, so that this assumption should not be made.

Morrey and Chao(1976) described a method of measuring the passive motion of the elbow joint using a three dimensional vector analysis technique. They used the frozen upper extremities of two cadavers to examine this elbow motion, with the humerus firmly fixed to a stationary object with pins. The rotational motion of the forearm with respect





to the humerus was expressed in terms of the Eulerian angles which uniquely describe the components of three-dimensional elbow motion. The first angle is the flexion-extension angle, the second angle is the carrying angle, (abduction and adduction at the elbow), and the third angle is that of axial rotation. The investigators determined the following facts regarding the motion of the elbow: as the elbow flexes, the carrying angle varies linearly; in extension there is a valgus angulation and the forearm rotates axially on the humerus during flexion.

Youm, Flatt and Sprague(1977) conducted a similar three-dimensional joint kinematic analysis of two rigid links, in that they were also interested in measuring rotation of the elbow joint. They used 3 non-collinear spark gaps to determine the position of the radius and ulna during the motions examined. They reported equations to determine the angular velocity of the movement of the radius around the ulna in pronation and supination. This rotation was measured around two different axes and was found to be different depending on the axis measured. They also described the position of the main axes for forearm pronation-supination, and elbow flexion in relation to the major bony landmarks of the upper limb. This study represented one of the few attempts available to analyze the motions at the elbow joint using the fundamental principles of three dimensional rigid-body kinematics.

Youm and Yoon(1977) have recently devised a mechanical





model for two dimensional analysis of the motion of the upper limb. As a mechanical model for this investigation, a four-bar linkage model was employed by introducing a fictitious link between the shoulder joint and the end of the hand, so that the open linkage formed a closed linkage. To derive input data for their analysis, an experiment was conducted using photographic technique with L.E.D.s. attached to the hand and shoulder. A 35 mm slide photograph was taken perpendicular to the motion at various pulse rates of the L.E.D.s, and at the same time the ground reaction was recorded by the force plate which was mounted underneath the subject's feet. The joint forces were then calculated at slow, moderate, and fast speeds, and they found that in the motions of slow and moderate speed, the joint forces were close to their segments own weight. When the speed of motion was increased, the joint forces increased quite dramatically.

Ayoub, Walvekar, and Petrino (1974) also developed a biomechanical model for upper extremity motion analysis in three dimensions. They used the basic equations of Newtonian mechanics to calculate the forces and moments at the joints, since "At any instant in time a rigid body in motion will be in dynamic equilibrium if the sum of the moments due to external forces acting on the body are equal to the rate of change of the angular momentum of the body" (1974:1142). They used the Euler angles to specify a body segment orientation in space at any time during the motion, relative



to an X,Y, and Z coordinate system. The angular velocity and acceleration of the segment could then be expressed as a function of the first and second derivatives of the segment's Euler angles. They used the anthropometric data from five adult male subjects performing various arm movements to attempt to verify the application of their model. They found that their model broke down at certain arm angles throughout the range of motion, and the equations did not adequately describe the movements. They stated: "In general, it must be concluded that the model as presently constituted is insufficient for predicting human motion characteristics". It is apparent that the complexities of movement of the human body are such that mathematical modelling of these motions is extremely difficult, and often leads to failure.

Jacobsen and Mann(1973) developed a series of equations which were designed to estimate the torque produced at the shoulder joint during a simple flexion motion. The predictor equation was known as the VMG (Vector-Myo-Gram) equation, and it's input consisted of the segment position vectors, the joint velocities and accelerations, and the integrated EMG signals from 9 shoulder muscles. They found that the curves of estimated shoulder torque vs. actual shoulder torque were very similar, so that this model may be used as a fairly accurate predictor of joint moments.

Plagenhoef(1971) also described a model which could be used to calculate the kinematic and kinetic forces acting on





the upper extremity. Although Plagenhoef did not specify that the 3-segment model he described was indeed the upper extremity, the forces acting on all body segments are similar so that the model could be generalized to represent the arm. Andrews(1974) also described a mechanical model of the forces which are acting on body segments during the performance of a dynamic activity, which could also be generalized to represent the upper limb.

Ray,et al.(1951) examined the actual movements occurring in the bones of the lower arm during the movements of pronation and supination around a fixed axis of rotation. The axis of rotation was varied by fixing the epicondyles of the humerus by pins. The motions of the two bones was examined by the use of X-rays, as well as by electromyograms of the muscular activity occurring during these motions. They found that under ordinary circumstances the ulna is abducted during pronation and adducted during supination, which is contrary to a common belief that the ulna is stationary during these actions, and the radius simply rotates around this fixed point. They stated: "--although limited pronation and supination can occur with the ulna remaining stationary, under ordinary circumstances the distal end of the ulna moves laterally as the radius travels medially during pronation, and that during supination the ulna moves in the opposite direction." (Ray, et al.,1951:996)

Another study which was concerned with lower arm





rotations was that of Chao and Morrey(1978), who attempted to measure the rotatory components of elbow motion under passive flexion. These investigators once again used cadaver limbs in their experiment, whereby the anatomical landmarks were located by steel pins, and the bones were x-rayed during the motion of interest. In this study the bones were photographed from two views which were perpendicular, and the spatial coordinates of several points of interest were calculated. The three-dimensional rotation of the forearm with respect to the humerus was measured based on Eulerian angles. This study was conducted primarily for use in the development and refinement of elbow prostheses, although the mathematical techniques may be of some value in analysis of other activities.

As can be concluded from the preceding sections of this review, little has been done in the development of techniques for the analysis of the arm motions in vigorous activities. The vast majority of the studies published are of a clinical nature, and are carried out on cadaver or skeleton parts. This method also allows the investigator to implant numerous wire and pin markings into the specimen, and so the measurement of anatomical landmarks is very simple. The error associated with each point measured is therefore relatively small, so that the mathematical techniques used for analysis often work very well. However, because the location of spatial coordinates often requires the use of an approximation technique, if the error



associated with the coordinates is too large the technique fails. Most of the mathematical analysis techniques published in these studies simply will not work with data derived from film of high speed body movements. It is clear that it is left to the researchers in sports biomechanics to develop techniques which are accurate and viable for the type of data which they are able to produce.

### Data Smoothing Techniques

Since there is always a certain degree of error associated with displacement points calculated from film data, it is necessary to use the methods of numerical analysis to 'smooth' these data points. There are several different methods of data smoothing currently in use in biomechanics research, each of which has had a short-lived period of popularity and has then been replaced by a newer method. For example, early researchers used manual smoothing methods using a planimeter to draw smooth curves through successive data points (Miller and Nelson, 1973). Successive methods, roughly in order of their rise and subsequent decline in popularity, included first central difference methods, polynomial approximation by least squares methods, cubic spline approximations, and digital filtering.

One of the earliest sports biomechanics researchers to attempt to smooth film data was Plagenhoef (1973), and he used a polynomial approximation method. Using the film displacement data, he determined the coefficients of a





polynomial which best fit the data points using the method of least squares approximation. The order of this polynomial could be altered depending on the regularity of the displacement data--more abrupt changes in the direction or magnitude of the displacement data resulted in a polynomial of higher degree. This polynomial could then be differentiated once to obtain estimates of velocities of the points for which displacements were calculated; and then differentiated again to obtain estimates of the acceleration between these points. However, it is notable that the motion of the point may be so complex that its' path may not be described by a polynomial of low degree. In cases where the curve is a poor fit to the data points, the calculated velocities and accelerations are often too inaccurate for use in further analysis (Pezzack, Norman and Winter, 1978).

The use of the first central difference methods to smooth film data was described by Widule and Gossard (1971) as simply a method of averaging between data points. Points on either side of a certain data point are taken and a line drawn between them. The slope of the tangent to the curve at the given data point is taken to approximate the derivative. This method was found to be fairly accurate for determining the velocity curves of a motion, but "since errors tend to propagate for the higher order derivatives, the results for measures of acceleration have not been completely satisfactory (Widule and Gossard, 1971:110)".

A more recent method of data smoothing is known as





cubic spline approximation, and has been widely accepted by biomechanics researchers (Zernicke et al., 1975; MacLaughlin et al., 1976). This is a method of averaging the displacements between successive data points, so that a smooth cubic curve is drawn through each three successive points. The velocities and accelerations of these points may also be approximated by differentiation of the equation of the curve between these points. It has been reported that the acceleration values calculated by this method for film displacement data are much more accurate than those derived from other methods.

McLaughlin et al. (1976) have reported comparisons of the cubic spline method and the polynomial curve fitting techniques. They noted that polynomials were inferior because fluctuations in one part of a curve will affect other parts of the curve, and also because polynomials are quite insensitive to quickly varying data of an otherwise uniformly varying curve. One of the problems associated with the use of cubic spline methods is that the endpoint values for the second derivative are zero. Zernicke et al. (1975:14) indicated that "...three extra data points at the beginning and ending of each data set served to minimize the second derivative zero end point tendency." Both of the above investigators used the IMSL Computer Library cubic spline routine called ICSSCU, and they have suggested several methods of estimating the degree of smoothing to be used with this routine. The most practical method suggested



(McLaughlin, 1976) was that of calculating the average error in measurement of distances from film. Since the error in calculating distances was determined by the measurement of two points, it was assumed that the total error was equally distributed between both points. Thus, the error for each point was calculated as the degree of smoothing for each set of data in the analysis. Zernicke (1975) has further suggested that this computed error should be used as input to the program to calculate the second derivative values and these values graphed against time. "If the acceleration curve is smooth, use a smaller error value; and if the acceleration curve is ragged, increase the error (1975:14)".

A more recent technique has been reported by Pezzack, Winter and Norman (1978), and is known as digital filtering. They reported graphs of the acceleration values calculated from film data of a simple movement, and they calculated that this may be the most accurate and reliable method to date of determining acceleration values. They stated (1976:381): "Digital filtering of the raw film displacement data followed by simple finite difference differentiation was the only one of the three techniques studied that accurately reproduced the acceleration time curves recorded from an accelerometer". They found that polynomial curve fitting smoothed the acceleration curves too much, and finite difference differentiation did not smooth them enough.

It should be noted here, however, that not all





researchers in biomechanics are in agreement as to the importance of data smoothing techniques in biomechanics research. Chao and Rim (1973) have noted that data smoothing techniques are not always desirable, as they noted: "--since numerical differentiation procedure as applied to the experimentally obtained data would magnify the inherent measurement errors. Besides, the final results usually depend upon what numerical techniques for smoothing and curve fitting were applied" (1973:498). They described a system of mathematical optimization equations to determine the applied moments at the leg joints during walking. They developed a two-dimensional model consisting of two segments, the thigh and the lower leg and foot segment, and they used parameters as measured from live subjects as input for their computer program. The displacements of each of the segments of their model were measured through the various phases of the gait cycle, and from these displacements the values of the moments at each of the joints is estimated. They concluded that this method was more advantageous because it required no numerical differentiation of experimental data, and thus the possibility of "magnifying inherent experimental errors is minimized". (1973:510)

A further problem in data smoothing techniques is that the smoothing technique may obscure true motion characteristics in the motion being observed. There may be quick, radical changes in the motion which are smoothed out by one of these techniques, which may be very important to





the skill. Widule and Gossard(1971) suggested that a sudden change in the angular direction of a joint at takeoff could be masked if a curve were passed through that point. The investigator must have a clear picture of the motion that he is analyzing to ensure that such important movements are not obscured.

### Kinematic and Kinetic Analyses of Softball Pitching

Few studies were located which included accurate quantified data on the softball pitch. Leviton(1975) described the windmill pitching motion qualitatively, noting that the longer path followed by the arm during this style of delivery may allow more time for the performer to apply force to the ball, and thus may result in greater velocity of the ball on release than in other styles of delivery. Kirby(1969) also described this motion in general terms, although he did provide a more detailed description of the arm motion. "It is important that the pitcher keep his arm in a fully extended position, thus lengthening the lever and increasing his arm and shoulder contribution to the ball's velocity. It is also important that his wrist be hyperextended or cocked during this forward whip...the wrist and ball should trail the forearm until the final wrist snap. This will increase the distance over which the wrist can develop momentum."

Although the skill of softball pitching is mentioned in most books on the sport, as well as in most books on skill



analysis, the descriptions are often sketchy and inaccurate. Kneer and McCord (1976) noted in their description of the skill that one of the most important motions in the skill is to "snap your wrist forward and roll the ball off your fingertips". No clear description was given of the exact movement involved in this wrist snap, not in which direction it was most advantageous to roll the ball. As well, their description of the timing of the step of the pitcher is in error, as they stated: "as the hand reaches head-high, begin to lift the opposite foot off the rubber and forward in order to keep your balance (1976:39)." The step begins far earlier in the sequence than is stated here, and in fact the step commences as the hand passes the plane of the body. A further description of the windmill pitch was attempted by Dobson and Sisley (1971), which also contained several inaccuracies. They noted that the pitching arm should be straightened at the highest point of the circular arm swing, because the "straight arm, backward and downward swing adds more power to the delivery. This arm action does not permit a high degree of body rotation, and as a result much of the power for the windmill pitch comes from the shoulder muscles (1971:44)". No explanation was attempted to describe how a straight arm action would tend to inhibit body turn.

Zollinger (1963) provided the only study in which any quantitative measures were calculated on the windmill pitch. She calculated the length of stride, the horizontal velocity of the pitch, the torque of the arm about the shoulder





joint, and the torque of the hand-ball system about the wrist joint at release. She found that the velocity of the ball at release was determined by two rotary forces: a torque about the glenohumeral joint (shoulder) and a torque about the radiocarpal joint (wrist). In fact, she has stated that the velocity of the ball at release was determined by the magnitudes of shoulder flexion and wrist flexion, which may be only partially true. However, no attempt was made to describe the rotational forces around the longitudinal axes of the arm segments, which may likely be the most important torques occurring in the skill.

### Three Dimensional Cinematographic Techniques

Cinematography has been the primary tool used to examine quantitative external mechanics of all types of human motions (Miller and Nelson, 1973). It is well known that such motions have been studied in two planes by one camera filming. However, the validity of studies in which film analysis is the primary tool for gathering data has not gone unquestioned. As noted by Penrose et al. (1976): "The validity of measurements obtained by cinematography and other photographic methods depends on the accurate recording of spatial and temporal relations. The relative ease of camera use has deceived many investigators into thinking that film data parameters can be compared directly with the real world. A major problem has been to obtain accurate spatial coordinates of joint centres and other points of





interest during the preformance of a motor activity." In most film analysis studies centers of gravity are located and displacements calculated, from which derivatives of velocities and accelerations may be made. However, as Miller and Petak (1973:14) have noted, "Since virtually all human motion occurs in 3 dimensions, a single camera and planar film analysis methods cannot provide a complete quantitative description of performance." There have been several studies published in recent years which have reported various methods of filming movements using two cameras with the intention of synchronizing these film records to produce three-dimensional coordinates of various points of interest. Other researchers have utilized three cameras to collect film data from which to derive spatial coordinates, normally with one of the cameras being oriented in each of the three principal planes of action.

Noble and Kelley (1969) utilized a three camera technique to determine the three-dimensional coordinates of a moving ball following the path of a right circular helix. They determined the position of the ball, distance traversed, elapsed time, velocity, and acceleration. The films were synchronized by firing a flash bulb at the beginning of each sequence, and timing of the cameras was accomplished by separately photographing a standard electric timer. One camera was located along each of the X, Y and Z axes, and a horizontal and a vertical coordinate were obtained from each of the three films, resulting in a total



of six coordinates for each point visible from all three cameras. The mean of each pair was taken to be the true value. The authors concluded that this procedure was of adequate precision to determine the position of a moving object and the primary values of distance traversed and time elapsed, and their first derivative velocity values. They found that the acceleration values were quite inaccurate, and not useful to include in their analysis of results (1969:645). No explanation was attempted for the inaccuracy of these calculations.

Duquet, Borms and Hebbelinck (1973) described a complicated method of three-dimensional analysis of twisting movements which required film data from two cameras, a side view and an overhead camera. By projecting the images onto a grid placed behind the performer, the actual coordinates of the segments of interest could be estimated. As the authors stated: "By a procedure of graphically manipulating projected anatomical reference points to a common plane, it is possible to determine actual positions in space and obtain dimensions and angles, and, from these, derive covered distances, linear velocities and accelerations as well as angular velocities and accelerations" (1973:175). However, the method appears to require much time consuming measurement and transformation of the original film data, and may not be practical for analysis of any reasonable amount of data.

A further study to develop three-dimensional filming





procedures was conducted by Bergemann(1974), who was most concerned with the camera placement which would produce accurate spatial coordinates. The two cameras were positioned so that their optical axes intersected at a common origin point, which was determined by surveying equipment. Equations were derived which were used to calculate the position of several arbitrary points on a coordinate grid. The procedure was found to be useful for the determination of these stationary, defined points, but no attempt was made by the author to expand its' use. A similar study was reported by Penrose et al.(1976), in which they investigated the positioning and alignment of cameras with and without intersecting alignment of the optical axes. They studied three camera alignment positions, with the cameras placed in different positions with respect to the origin and the point of intersection of their optical axes. The magnitudes of error in all three filming situations were similar, "indicating that non-intersection alignment of the optical axes should provide information as accurately as the more rigidly controlled camera conditions (1976:6)". The authors noted that this more flexible filming situation would be more useful for collection of data from a game or competitive performance, without any appreciable loss in accuracy.

Miller and Petak(1975) described a method of three-dimensional filming in which the three cameras must be placed so that their optical axes intersect at a point near





the subject. The three cameras were placed so that their optical axes were at angles of 120 degrees to one another. It was felt that this positioning of the cameras would maximize the number of points visible in the film of any two of the three cameras. Equations were derived to determine the spatial coordinates from the two camera film coordinates. Although this method was reported to produce accurate three-dimensional data it required that the investigators use surveying equipment to locate the optical axis and to ensure that the cameras were horizontal. Van Gheluwe (1974) described a similar technique of three-dimensional filming, where once again the cameras had to be placed in an exact position in relation to the subject.

Black (1977) has recently described a method of three-dimensional filming whereby the X, Y, and Z coordinates are simply read directly from the film analyzer. The two cameras were placed in positions at right angles to one another, with their optical axes intersecting--this point of intersection is the origin of the three-dimensional coordinate system. After some correction for perspective error due to the location of the subject in relation to the origin, the X, Y, and Z coordinates were at right angles to their respective cameras. From one camera the X and Y coordinates were read; and from the other camera the Z and Y coordinates were read. These coordinates were then used to calculate directly the X, Y, and Z displacements, velocities, and accelerations. The film from the two cameras was



syschronized by a unique method in which a bicycle was turned upside down in the field of view of the cameras. The rear wheel was marked with several white markers at different intervals, and the wheel was turning during the filming. The film could then be synchronized by the location of the markers as they appeared in each of the film frames.

Dapena(1977) has developed a method of three-dimensional filming by using horizontally panning cameras. The cameras were placed at approximately 90 degrees to each other throughout the field of action of the subjects. The subject was filmed while executing the Fosbury Flop method of high jump, during the last strides of the run-up, the takeoff, and the bar clearance. During this time, each camera was panned horizontally (ie. was rotated about a vertical axis) so that the subject remained within the optical field throughout the entire performance. The cameras filmed independently of each other, and the film records were synchronized by use of critical instants (ie. instant of first touchdown or takeoff). The X,Y, and Z coordinates of landmarks on the body were determined by using several landmarks in the photographic field which were filmed in the background of the jumper. Since the coordinates of each of the background markers were known, their orientation relative to the cameras (some angle  $\theta$ ) was readily computed. A series of markers was then filmed, and the locations of the marks estimated from film data. Dapena found a random error of .5 cm in the X,Y, and Z coordinates,





which he concluded was well within acceptable limits for most analyses of sports activities.

Van Gheluwe (1975) has described one of the most common sources of error in attempts at three-dimensional film analysis to be misalignment of the cameras with respect to the intersection of the optical axes. He developed a simple method of evaluating the error on the measured coordinates resulting from camera misalignments. The estimations of deviation errors were based on trigonometric formulas whereby the alignment errors were proportional to the errors in the spatial coordinates, and occurred in the same direction. He suggested that telephoto lenses be used whenever possible, as these will reduce these errors due to misalignment because of their smaller viewing angles and the longer focal length.

A more recent study by Van Gheluwe (1977) has reported a technique in which the cameras may be placed in any position in relation to the subject being filmed. Van Gheluwe has refined his earlier computer program (Van Gheluwe, 1974) which is used to transform the two camera film coordinates into three dimensional data so that exact camera placement is no longer necessary. As he stated: "This means that the camera position is now completely free from any restriction: the camera may be tilted at any angle, positioned at any place or distance, etc...Reference points on the steel reference frame are sufficient to reconstruct the spatial coordinates at any arbitrary point in the view field of the



cameras." The only necessary step required to coordinate the data from these cameras is that a three-dimensional object be placed in the field and photographed by each of the cameras. The object must have a number of points in each of the three perpendicular planes which are a known distance from the origin of these planes. The author constructed a set of coordinate axes from steel tubing, marked appropriately at regular intervals. The program then calculated a transformation matrix for each of the cameras, and also one for the combined data, and the output consisted of three-dimensional coordinates of a series of points photographed by the two cameras simultaneously. He found that the X,Y, and Z coordinates calculated from this program were accurate to five per cent when a grid composed of known distances was photographed.

However, once the three dimensional coordinates of a point moving in space have been determined it is then necessary to use this data to calculate important kinematic and kinetic data from the film. Much of this computer programming of analysis techniques has been attempted in a recent study by Black(1977), in which she described a three-dimensional filming technique, and she also developed a computer program utilizing the methods of engineering vector analysis to determine velocity and acceleration values for this data. Black also attempted to estimate the magnitudes of angular velocity and acceleration of the segments in some simple skills, but did not attempt to verify these





estimates. These estimates were based on the assumption that the rotations occurring were only occurring in two planes, and that the rotation in the horizontal plane was negligible. She assumed that the rotations of the segments around their longitudinal axes were not critical so were assumed to be zero. This assumption is likely not viable for most of the activities analyzed, so that this technique is of limited value to other researchers interested in calculation of angular parameters.

One of the major problems encountered by investigators in attempting to measure spatial coordinates is that of photographic perspective error (Black, 1977). Martin and Pongratz (1974:469) stated that "Photographic perspective error has long plagued the researcher attempting to obtain accurate three-dimensional coordinates from two-dimensional film data". They developed formulae to correct for this error, based on their study using film from two 35mm cameras. The cameras were set up with their optical axes intersecting at right angles to one another, to define the spatial coordinate system. They determined the perspective error by comparing actual distances on their reference measure with the distances calculated from film displacement data. These formulae may be used by any researcher to correct the film data from two positioned cameras for perspective error, and in fact these were used by Black (1977) in a recent study.

The problem of producing accurate three-dimensional





coordinates of film data has been one of continuing interest to researchers in sports' biomechanics. However, virtually all of the above studies reviewed have validated their procedures by filming a coordinate grid, or a series of fixed reference markers. None of the studies located attempted to locate the spatial coordinates of the joint centers of the body during a vigorous sporting activity. It must then be concluded that there is no useful and accurate procedure presently available to determine the X,Y, and Z coordinates of the body segmental endpoints. This difficult problem is one to which a useful and viable solution is necessary in order for biomechanical analysis to continue to provide answers to questions of technique in skills analysis.

#### Force Platform Studies

The use of force platform data is relatively recent in the biomechanics of sports investigations. Ramey(1973) has stated: "The force plate has become a useful tool for the study of many types of human motion--the force plate yields some fundamental data and substantially assists in the understanding of the motion involved. In the particular case of the athletic studies the force plate has been used to identify faults in technique and has led to new ways to perform the event." The force platform is basically an electronic sensing device in which a strain gauge or an LVDT



is mounted within the platform so that strain on the platform is picked up as a change in the resistance of the device. Many of the platforms in current use are able to record forces in the X,Y, and Z directions, as well as torques about each of these axes (Miller and Nelson, 1973).

One of the early reports summarizing the use of this technique was reported by Payne(1968). He noted that the force platform was a valuable tool to examine the forces exerted against the ground during a performance. However, he warned that the natural frequency of the platform is excited by the sports' performance and the tracings may not be accurate for some activities. Miller and Nelson(1973) have also noted some difficulties in force platform use, such as the difficulty in securing the platform properly to attain proper damping. Also, they are limited in size because of their complex construction and instrumentation, and they are limited to a certain frequency response level. In a more detailed study, Payne(1968b) described the use of the force platform in examining the ground reaction forces in a number of activities, including the sprint start, the running stride, shot put and weight lifting. He noted that these tracings could provide the coach with valuable insight into faulty technique in some of these skills. In the shot, for example, there was a change in the value of the horizontal thrust from positive to negative, indicating a shift in the drive from the legs from the rear leg to the front one. The timing of this shift in relation to the throw can tell the





coach a great deal about the application of forces by the thrower, and the timing of these forces.

Lamb and Stothart (1977) conducted a vertical jump study in which they compared the force platform method of determining center of gravity kinematics and kinetics, and the method of calculating these parameters from film data. They found that there were no significant differences between the parameters calculated using either of these two methods and so the force platform provides an accurate estimate of the forces exerted against the ground.

Probably the greatest value in force platform data in cinematographical studies is as a check on the accuracy of the digitized data. As the shape of the force curves approach those produced from calculations from film data, so the data become a more accurate representation of the application of ground forces during the skill. Since the calculation of ground forces is based upon the determination of acceleration from film coordinates, this is also a test of the amount of error present in the digitized data. Similarly, a large discrepancy in the shape of these two records may indicate that the data calculated from the film has a large amount of error.



## CHAPTER III

### PROCEDURES

#### Experimental Procedures

This chapter deals with the experimental procedures undertaken by the investigator in this study, as well as the techniques of data analysis employed.

#### Pilot Study

A pilot study was carried out in November, 1977 to verify the experimental procedures to be used in the final project. Two subjects were originally used in this study, one male and one female, both scheduled to participate in the final study.

The filming of the subjects was conducted in the strength laboratory of the Faculty of Physical Education. The photographic field consisted of a force platform mounted on a larger platform, from which the subject pitched the ball into a large cargo net suspended from the ceiling of the laboratory. A target was indicated on the cargo net to approximate the size of the strike zone during the game of softball. Only those pitches which entered the strike zone were chosen for analysis. This precaution was taken to ensure the analysis of pitches which would be good pitches



in a game situation, and would not include 'wild' pitches which may involve incorrect joint movements.

Two Photo Sonics 1PL 16mm movie cameras were placed at two positions in the laboratory with their optical axes almost at right angles to one another. The cameras were at a maximal distance from the subject within this relatively small area. Camera 1 was placed so that the optical axis was perpendicular to the direction of the pitched ball, which was also at right angles to the direction of the major joint motions of the pitcher. Camera 2 was placed in front of the performer, and slightly to the right of the direction of the pitch. The two cameras were set so that the exposure time was as short as possible with the available lighting. In particular, the exposure time was calculated to be .00125 seconds with the shutter angle set at 45 degrees. Since the light in the laboratory was rather poor for high speed filming, the film was 'pushed twice' during development. This still resulted in rather dark films.

Both cameras were set at an operating speed of 100 frames per second (fps), and both were connected to a timing light which placed a mark on the films at every .1 second interval. The two films were further synchronized by use of a flash signal, operated manually at the beginning of the pitch to be filmed. The flash device was operated by an assistant during the actual filming, and this flash served as the signal for the subject to begin the pitching motion. The assistant was in a position behind the subject so as not





to interfere with the activity, but so that the flash was visible in each of the camera fields. In this way the film from each of the cameras could be analyzed from the same point in each pitch, and the data from the two films could be converted into a single set of three-dimensional coordinates by the use of an appropriate computer program.

The film from the pilot study was found to be too dark for detailed analysis when shot under these experimental conditions at 100 frames per second. However, part of the film was shot at 30 frames per second, and resulted in satisfactory exposures. This film was subjected to some preliminary analysis to ensure that the necessary parameters could be determined for this study. Several decisions were made on the basis of the findings of the experimental study, which affected the subsequent filming of the subjects. One, was that the available lighting in the strength laboratory was inadequate to film at 100 frames per second, and that more lighting would have to be made available in the final study. Secondly, this area was too small for the cameras to be placed an adequate distance from the subject to avoid large perspective errors. A larger indoor filming area had to be located. Thirdly, it was found to be difficult to measure the rotation of the arm segments around their longitudinal axes from the front view camera. Since the markings on the arm were obscured from the camera view by the pitcher's body, a more advantageous position for the second camera was found to be to the rear of the subject.



## Testing Apparatus

### Filming Equipment

Two Photo-Sonics 1PL 16mm cameras were used in the present study, in which the frame rate could be altered from 1 to 500 frames per second. The cameras are motor-driven, so that the frame rate remained relatively constant (+ or - 1%) throughout the filming session. The two cameras were calibrated by using a strobe light set at 100 flashes per second, which was then synchronized with the camera shutter. The two cameras were attached to a single Photo-Sonics Timing Light Generator electronic timer, which was set to mark each film with a light flash at every .1 second interval. This timing device was also used to synchronize the film records of both cameras, as described in a later section.

Each of the cameras was equipped with an Angenieux 12-120 zoom lens, adjusted to the desired focal length.

In order to utilize the three-dimensional computer program to analyze the film data from two cameras, a metal 'tree' was constructed. This tree consists of six one-meter pieces of copper tubing fixed into a wooden block forming an orthogonal triad of axes, emanating from a common origin. These axes were then divided into 10-centimeter divisions by marking them with black tape. The tree was then attached to a wooden stand so that it would remain rigid at the site of the filming. This tree was then placed in position on the





site from which the subject was to pitch the ball, and was then photographed by each of the two movie cameras. The tree was filmed at regular intervals throughout the filming sessions, in case the cameras were inadvertently moved during the actual filming.

### Force Plate

Three pitchers were filmed in the dance studio. Each of the pitchers pitched the ball while standing on a force plate. The force plate used in this study is a commercially manufactured plate, a Stoelting's Model #19570 which was purchased by the Physical Education Department six years earlier. This platform uses 'Linear Variable Differential Transformers' (LVDT), and is supposed to be linear in all three axes. The force tracings attained from this plate during the pilot study were found to be inconsistent, attempts were made to correct this for the final study. The subjects were asked to begin the pitch with both feet in contact with the force platform, and during the actual pitch the subjects took a step forward onto the left foot. Therefore for most of the duration of the pitch, the performer had one foot in contact with the force plate. Since the other foot was free in the air for most of the force-producing phase of the pitch, the forces recorded by the force plate were representative of the forces exerted by the pitcher during the major portion of the delivery of the



ball.

The forces exerted on the force platform were recorded by a Honeywell model #1912 visicorder. The tracings of the exerted forces, recorded by the Honeywell, were synchronized with the appropriate film records by means of the same Photo Sonics timing light which was attached to both cameras. Thus it was possible to compare the forces calculated from the film records to the forces recorded by the force platform tracing, at any particular instant in the performance.

#### Film Analysis Equipment

The preliminary analysis of the film was carried out with the aid of a Lafayette 16mm Analyst projector. It was possible to carry out considerable preliminary temporal and spatial analysis by using the attached digital frame counter. Editing and synchronizing of the films by ink markers was also carried out by a Traid Model V/R-100 film analyzer, which also enabled the investigator to record the positions of various points of interest during this phase of the analysis.

The film records were analyzed by digitizing body segment endpoints with a Bendix 9864A digitizing board attached to a Hewlett-Packard 9825 programmable calculator. Since the investigator had spent a good deal of time in digitizing segmental endpoints from movie film, the



reliability in locating joint centers was considered to be very high. However, this reliability was checked on several sets of data by using Pearson's Product Moment Correlation between sets of measures. The segmental endpoints for the three arm segments were digitized, and input directly into the HP 9825 where a program was stored to produce segmental inclination values. The test-retest reliability of these angular values was found to be at least  $r=0.97$  for all sets of data tested. The required endpoints were digitized for each frame of interest, and the film records were stored on magnetic tape for further analysis. The data was then read into the large time-sharing computer system at the University of Alberta, which was operated by an Ahmdahl 460V/6 computer. Much of the data analysis was also carried out by the HP 9825 which was programmed to calculate several of the parameters of interest in the pitches.

## Subjects

The subjects used in this study were four highly skilled softball pitchers, two male and two female. All of the subjects were right-handed, so that camera positions and descriptions of the pitch were the same for all. All four performers could be classified among the top pitchers in the Province of Alberta, since all four had played in a number of National Championships. Two of these pitchers (1 male and 1 female) had been chosen as Canadian All Stars on at least one occasion, and so could be classified as among the best





in the country. All were currently members of a Senior or semi-professional softball team, although the testing was done in the month of February when none of the pitchers were actively involved in playing. It is possible that the ball velocity measures may have been considerably higher if the testing had been done in mid-season, but for such highly skilled performers it is unlikely that the technique would alter a great deal. Following the actual filming session, each of the subjects was asked to complete a questionnaire describing his or her softball pitching history. This history provided the investigator with greater insight into the actual skill level of each of the performers.

#### Subject Preparation and Measures

As each subject arrived at the filming site, the following anthropometric measures were taken by the investigator: standing height, weight, upper arm length, biceps girth (flexed and relaxed), lower arm length, wrist diameter, hand length, and hand span. These measures were taken to enable the investigator to determine more accurate estimates of the moment of inertia and radius of gyration of the segments of the pitching arm.

The subjects were further prepared for filming by placement of tape strips and markers on the pitching arm, to assist the investigator in measuring the rotation of these segments. The following tape strips were placed on the



subject: (1) from tip of acromion process to lateral epiepicondyle of humerus, (2) from median border of axilla to medial epicondyle of the humerus, (3) from lateral epicondyle of humerus to styloid process of radius, (4) from medial epicondyle of humerus to styloid process of ulna, (5) around diameter of wrist (6) from styloid process of radius to tip of the thumb (7) from base of the lunate to the tip of the III phalanx. As well as these strips of black tape, each of the bony prominences marking the centers of the joints were marked with a circle of white tape in order to allow for more accurate estimates of the position of the joint centers.

#### Filming Procedures

The filming of three of the subjects was conducted in the dance studio of the Physical Education Building in February, 1978. The fourth subject was filmed outdoors a few weeks later. All procedures for this subject were the same as described herein, except for the location of the filming, and the absence of the force platform. This area was selected for the actual filming because of its' larger size, the black curtain along one wall, and especially for the large number of floodlights located on the ceiling, usually used for dance performances. The side view camera was located exactly 50 feet 9 inches from the performer, and at right angles to the direction of the pitch. The pitchers performed from a position with the back foot placed directly





in the center of the the force plate, which was located in a larger force platform, and threw the ball at a thick gymnastics mat placed against the wall of the room. No attempt was made to measure the accuracy of these pitches, although the skill level of the performers was such that no really 'wild' pitches were filmed.

The other camera was placed to the rear of the performer, at an angle of approximately seventy degrees to the side view camera. This placement was chosen because of the necessity to film the joint markers as long as possible

during the actual release of the ball. This camera position was found to be optimal when different camera positions were tested in an earlier film of the rear view of the pitcher. This camera was placed exactly forty feet from the subject, which was the maximum distance it could be positioned in the filming area.

The two cameras were set so that the exposure time was as short as possible with the available lighting in the dance studio, so as to minimize the blurring of the ball during release. Kodak Ektachrome #7240 Tungsten film, with an ASA rating of 125 was used. The exposure time was calculated to be .000833 seconds with the shutter angle set at 30 degrees, and the film was 'pushed one stop' during development. The fourth subject who was filmed outdoors, was filmed using Kodak Ektachrome #7239 Daylight film, with an ASA rating of 160. Both cameras were set at 100 frames per second, and were calibrated by use of a strobe light so that



the camera speeds were exact. Further information on filming techniques may be found in Appendix A. The two films were further synchronized by the use of a timing light which placed a timing mark on the edge of the film at any set interval. This timing light was used to synchronize the films by the following method: the cameras were started at the same time by a signal from the investigator; a verbal signal was then given to the subject to begin the pitch--on this verbal signal the timing light was switched from 100 flashes per second to 10 flashes per second by one of the cameramen. Thus each film was clearly marked as to the point at which the pitch began, simply by the decrease in the number of timing marks. This method was found to be an effective means of synchronizing the film records, which was necessary for the three-dimensional analysis procedures.

Ten trials of each subject's 'fastest' softball pitch was filmed, and the best five of these trials were selected for study. Since one of the prime characteristics of good pitching is the velocity of the pitch, the five trials in which the greatest ball velocity was attained were chosen for analysis. Since there were four subjects in the study, taking the best five trials for each one resulted in twenty separate pitches being analyzed in a preliminary way. However, since the subjects were all very highly skilled, there was found to be very little variation between the pitches for a single pitcher. Since it was clear that analysis of five pitches by each pitcher would be an





unnecessary duplication of data, it was finally decided to analyze in detail only the two fastest pitches of each of the four pitchers. In this way, only the most highly skilled movements of these skilled performers would be subject to detailed analysis.

#### Force Plate Procedures

The subjects were instructed to pitch each ball with the back foot placed on the force platform. The forces exerted by the performer against the force platform were picked up by the strain gauges within the platform, and these signals were amplified and appeared as tracings on the Honeywell visrecorder. This tracing allowed comparison of the ground reaction forces calculated from the film data with the force plate recordings, so that a check was available on the accuracy of the accelerations computed for the body mass center.

The force plate data was synchronized with the film data for each pitch by means of the flashes from the timing device attached to the cameras. This timing device was also attached to the Honeywell recorder, and was recorded as an event marker on the tracing of the forces recorded from the force platform. In this way the three independent sets of data (that from camera 1, camera 2, and the force plate) could be synchronized, and the records of each pitch could be analyzed from three different data sources at any particular instant in time.





## Analysis of Data

The data collected for this study have been analyzed under the following nine classifications:

1. Subject Pitching Data
2. Pitching Parameters
3. Body Segment Parameters
4. Ground Reaction Forces
5. Angular Kinematics
6. Linear Kinematics
7. Single Plane Kinetics
8. Three Dimensional Analysis
9. Three Dimensional Angular Velocities

### Subject Pitching Data

To provide a basis for description of the entire pitching motion, the film of each pitch was analyzed from the beginning of the windup to the end of the followthrough. Since the entire motion took up to 150 frames to complete, every fifth frame was digitized for the whole body calculations. The film was digitized by the investigator using the Bendix digitizer board and an HP 9825 programmable calculator. Since there were two cameras filming each of the pitches, each of the pitches analyzed had to be digitized twice, once from the side view camera and once from the rear view camera. The digitized segmental endpoints were stored



on magnetic tape by the HP 9825, and were later transferred to the Ahmdal 460/V for analysis by the mass center programs stored there. Each of twenty-two segmental end points was digitized and the coordinates of each of these points was recorded onto magnetic tape. This data could later be stored into disc files in the computer memory, or could be punched onto computer cards for storage and later assembly into a computer program.

It should be noted here that one of the critical problems in carrying out the present study was the ability to read the digitized endpoints into the Ahmdal computer for further analysis. Since the digitizer board could only be attached directly to the HP 9825 and the points stored onto magnetic tapes, these tapes were only readable by this machine. It was necessary to have a computer program written which would allow the HP 9825 to be attached directly to the large computer, so that the HP would act like a regular terminal and could then send data to be stored in the Ahmdal. This program was eventually provided by the Hewlett Packard programmers, and with this program and some additional hardware (a ROM connector and a high speed line printer) the digitized data was transferred. Some problems were encountered with the actual transfer of the data points, in that the speed of the transfer was too great for the receiver, so that there were numerous errors in the data files which had to be corrected. This was possible because the original data were stored on the cassette tapes, which





could be read by the HP 9825.

The segmental endpoints of the upper extremity involved in the pitching motion were digitized separately from the whole-body data. The four endpoints involved in this digitizing process were: the shoulder joint, the elbow joint, the wrist joint and the fingertips. These four endpoints were digitized in two different ways for each pitch. First, the whole pitch was digitized--from a point .40 seconds prior to release to a point .10 seconds after release, every second frame of the film was digitized for a total of 25 frames. Secondly, the pitch was digitized from a point .20 seconds prior to release to a point .05 seconds after release, every frame was digitized for a total of 25 frames. For each of the eight pitches analyzed, then, there were two independently measured sets of data describing the motions of the arm segments, which could be used as a check on the reliability of the digitizing process.

#### Pitching Parameters

For each of the pitches filmed, the velocity of the ball in each of the six frames following release was calculated by use of a computer program written for the HP 9825. To determine the actual velocity of the ball in each of the pitches, the highest and the lowest velocity estimates were dropped, and the remainder of the velocities were averaged. These velocity estimates were found to be in close agreement, both those between frames for a single



pitch, and those between pitches for a particular subject.

Another parameter of the pitch that was calculated for each of the pitches was the time for the pitch. For the purposes of this study, the time for a pitch was the time from loss of left foot contact with the force plate, until the actual release of the ball. This parameter was determined by counting the frames between these two events, using a Lafayette Analyst Projector which was equipped with an electronic digital frame counter.

Another important factor in the softball pitch is the length of the stride taken during the pitch--generally more highly skilled pitchers will take a relatively longer stride. Stride lengths may be compared between pitchers of different sizes by reporting them as percentages of standing height (Zollinger, 1973). The stride length for the pitches of each subject was calculated as the distance from the toe of the rear foot to the heel of the front (left) foot.

#### Body Segment Parameters

It is of critical importance in biomechanical research to have accurate estimates of the relative weights of the segments being analyzed, as these values are used both in the segmental analysis, as well as in the determination of the mass center using the segmental method. There are several sets of percentage weight data which are in common use in biomechanics research today (Miller, 1971; Hay, 1973),





which are primarily derived from cadaver data. As noted by Plagenhoef(1973), the anatomical data presented by Dempster(1955) has been the most widely used, and modifications of his data may be used to estimate body proportions in the living. The accuracy of these estimates is therefore open to question, as the body proportions of cadavers differ markedly from those of a muscular athlete-- and the more muscular the athlete, the larger the magnitude of error. Hay(1973) has reported tables of segmental weights which list slightly different percentages depending on the body build of the subject, but since these estimates were originally calculated from equations calculated from cadaver data, they are still open to question. Widule(1976) has noted that although the accuracy of these percentage values is questionable, particularly in the application to females and children, relatively close approximations of segmental mass can be obtained and values can be adjusted according to what is known about the mass distribution of individuals of different somatotype, sex, and age.

The most recent work in the area of estimating body segment parameters is reported in a publication called 'Humanscale', published by the MIT press and compiled by Daffrident, Tilley and Bardayjy (1974). Since these parameters were determined from a large number of live subjects and are likely the most accurate presently available, these were the segment weights and inertia factors used in the present study. This publication includes





location of the centers of gravity for each of the segments, and estimates of the segment lengths for each of the segments for subjects of three sizes: large, medium, and small. This publication also included all the above parameters calculated for females, which was unique for a publication in this area. The calculated segment masses and calculated weights are reported in Table I.

The moment of inertia is the resistance of a body to rotation (rotary motion). The moment of inertia of the mass of a body with respect to any axis is the sum of the products of each element of mass and the square of its distance from the axis. Various methods have been used to determine moment of inertia values of the body and body segments, including pendular methods, quick release method, volumetric determination, and through the use of physical models (Widule, 1976).

Since the moment of inertia of a living body segment cannot be determined directly (Plagenhoef, 1973:166), an alternate technique is needed to calculate this parameter. The method used in this study was that proposed by Miller and Nelson (1973) whereby the radii of gyration are calculated from the moments of inertia determined from cadaver studies. Miller and Nelson (1973:98) quoted Fischer when they stated that the radius of gyration for the greater extremities with respect to all axes passing through the mass center and perpendicular to the long axis of the limb was three tenths of the segment length. The formula for



calculation of the segment moments of inertia then became:

$$I_g = M * K^2 = M (.3 * L)^2$$

where

$I_g$  = Moment of Inertia of the segment about G

M = Mass of Segment

K = Radius of Gyration

L = Length of the Segment

G = Mass Center

The moments of inertia around G (the mass center) of the segments are reported in Table I. These are comparable to those reported by Widule (1976), although they are larger due to the larger size of these subjects. The measures calculated by Widule were derived from the data of eight cadavers, all of which were much below normal size and weight. Plagenhoef (1971) also calculated the moments of inertia of the segments around axes passing through the proximal and distal ends of the particular segments--these were calculated from Dempster's data (1955) on cadaver moments of inertia. However, Miller and Nelson (1973:99) have noted that although these methods can provide estimates of masses and moments of inertia, they will always be





somewhat inaccurate because they were derived from adult male cadavers. These inaccuracies may be magnified when the populations differ in age, sex, race, etc. However, since these estimates were the best available, these were used in the calculation of subsequent kinetic parameters in the present study.



TABLE I. Subject-Data-for-Kinetic-Analysis

Subject	Upper Arm Segment			
	DS	BL	SW	CM
Total Mass (kg.)	106.6	74.84	72.57	89.36
Segment Mass (% Total Body)	3.3	3.0	3.0	3.3
Segment Mass (kg.)	3.52	2.24	2.18	2.95
Segment Weight (W=M*G) (Newtons)	34.54	21.98	21.39	28.95
Segment Length (cm.)	.39	.33	.31	34.5
Distance to C of G (43.6% from Prox end)	.170	.144	.135	.150
Moment of Inertia (around G, where $I=M*K**2$ and $K=.3*L$ )	.0482	.0219	.0188	.0316
Moment of Inertia (around proximal end, where $I=I(cg) + M*D**2$ )	.1499	.0683	.0585	.0979

Subject	Lower Arm Segment			
	DS	BL	SW	CM
Segment Mass (% Total Body)	1.9	1.6	1.6	1.9
Segment Mass (kg.)	2.02	1.197	1.16	1.69
Segment Weight (W=M*G) (Newtons)	19.82	11.75	11.38	16.58
Segment Length (cm.)	.29	.28	.27	29.5
Distance to C of G (43.0% from Prox end)	.125	.120	.116	.127
Moment of Inertia (around G, where $I=M*K**2$ and $K=.3*L$ ) (units: kg/m**2)	.0152	.0084	.0076	.0132
Moment of Inertia (around proximal end, where $I=I(cg) + M*D**2$ )	.0467	.0256	.0232	.0404



TABLE I. Subject-Data-for-Kinetic-Analysis-(cont'd)

	Hand and Ball Segment			
	(Ball Mass=.185kg.)			
Segment Mass (% Total Body)	.65	.50	.50	.878
Segment Mass (kg.)	.878	.559	.549	.765
Segment Weight ( $W=M*G$ ) (Newtons)	8.62	5.49	5.39	7.51
Segment Length (Actual Segment Length in cm.)	20.5	18.5	19.0	19.5
Distance to C of G (28.0% from Prox end)	.057	.0518	.053	.055
Moment of Inertia (around G, where $I=M*K**2$ and $K=.3*L$ ) (units:kg/m**2)	.00332	.00172	.00178	.00261
Moment of Inertia (around proximal end, where $I=I(cg) + M*D**2$ )	.00617	.00322	.00332	.00492

### Ground Reaction Forces

To calculate the ground reaction forces, the whole body of the subject was considered to be a single rigid body with the mass concentrated at the mass center. The position of the mass center was calculated by: digitizing the segmental endpoints for each of the body segments, calculating the mass center of each of the segments, and utilizing the segmental method of determination of the body mass center. The actual calculations were carried out by a computer program written expressly for the purpose of calculating and graphing the mass center. For the top two pitchers, the position of the mass center in each frame analyzed was





determined by use of this mass center program (Bates, 1974). The displacements between successive frames in the X and Y directions could then be calculated, and from this displacement data the velocities and accelerations of the mass center throughout the pitch could be determined. These kinematic parameters were calculated by use of a program written by the author, in which the raw displacement values were read in to the IMSL cubic spline smoothing program. These displacement values were then smoothed and the acceleration values were calculated. Using the principle of Newton's second law, the applied forces are equal to the mass times the acceleration of that mass, so that the horizontal and vertical ground reaction forces could be calculated from the accelerations of the mass center. The equations used in this calculation are found in Appendix C.

As well as the calculated ground reaction forces, the applied ground reaction forces were recorded by the force platform connected to the Honeywell visicorder. These forces were represented by a paper tape tracing of the forces exerted on the force platform in the X and Y direction. These two independent methods of determination of ground forces were compared qualitatively by visual inspection. It was not possible to quantify accurately the magnitudes of the forces measured from the force plate, since these tracings were not accurately calibrated. This technique provided an estimate of the accuracy of the data calculated from the film coordinates and especially provided a check on



the vertical and horizontal accelerations of the mass center, which are often subject to considerable error.

### Angular Kinematics

The angular motions of the pitching arm were analyzed from the beginning of the delivery, to a point 5 frames (.10 sec) after release. To ensure a constant point of analysis for each of the eight pitches analyzed, the release frame was assumed to be zero, and the film was reversed to a position 40 frames prior to release. From this point in the delivery, the four segmental endpoints of the arm were digitized for every second frame through release of the ball and for five frames afterward. Because the frame rate was calculated to be exactly 100 fps, this represented a time interval of .02s between frames analyzed. A computer program was written for the HP 9825 which accepted as input the digitized segmental endpoints, and calculated the angular positions (segmental inclinations) for each of the three segments of the arm, for each of the 25 positions analyzed. All positions calculated were measured from the right horizontal in degrees, and each position in degrees was changed to radians within the computer program.

Since the greatest rise in the velocity of the upper arm segment occurs just after the high point of the backswing is reached, the pitching arm was analyzed in detail from this point. The four segmental endpoints of the





arm were then digitized a second time, such that the film was reversed to a position 20 frames prior to release. From this point, every frame was digitized through release and for five frames afterward, for a total of 25 frames digitized at this shorter time interval between frames.

These angular positions for each of the three segments were then read into the Ahmdal 460V/6 computer, in which the cubic spline data smoothing programs were stored. These angular displacements were then smoothed by the IMSL cubic spline program called ICSSCU, which smooths the angular displacement data to reduce the effects of random errors in the data. This cubic spline program has been used extensively in biomechanics research, and is the program recommended for data of this type (Mclaughlin et al., 1977; Zernicke et al., 1975). From this smoothed displacement data, the angular velocities and accelerations were calculated for each of the segments for each of the frames analyzed. The computer program written by the author to analyze these angular motions is reported in Appendix E. The angular displacement, velocity, and acceleration data was then graphed for each of the pitches analyzed. The angular displacements for each of the segments were plotted on the same graph against time so that these angular kinematic parameters could be compared, and this was also done for the angular velocity and acceleration values.



## Linear Kinematics

The exact frame rate was determined by counting the number of frames between the flashes of the timing light on the edge of the film. The conversion factor for changing film distances into real life distances was calculated by use of a reference marker of known length in the field. From the coordinates of the upper limb joints and segmental centers of gravity, kinematic parameters were calculated for each of these points.

The linear kinematics of the pitching arm were calculated from the film data digitized separately of the 4 segmental endpoints of the arm, and from the angular displacement calculations. The shoulder joint displacements were smoothed using the cubic spline program described earlier, and the shoulder linear velocities and accelerations were calculated from this data.

The same computer program which was used to calculate the angular kinematics was expanded to carry out the linear kinematic calculations. The linear velocities and accelerations of the shoulder, elbow, wrist and fingertips were determined for each of the 25 frames analyzed, for each of the pitches. The kinematic analysis of each of the segments of the arm was carried out using the method described by Youm(1977a,1977b) and Pearson(1963). This method consisted of using vector equations to solve for the linear velocities and accelerations, once the angular kinematic parameters have been calculated. These equations



have been reported by Youm (1977a,1977b). The relative velocity of a point at the end of a rotating segment is equal to the vector product of the angular velocity of the segment and the position vector of the segment, or,  $V = w \times r$  where  $V$  = the linear velocity of the point,  $r$  = the position vector relative to the fixed endpoint of the segment, and  $w$  = the angular velocity of the segment. The absolute linear velocity of a point is equal to the vector sum of the absolute velocity of the proximal endpoint and the calculated relative linear velocity. For example, the velocity of the elbow joint is calculated as the vector sum of the velocity of the shoulder joint, and the cross product of the angular velocity of the upper arm segment and the vectors describing its' axis. Similarly, the acceleration of the shoulder joint is calculated as the vector sum of the tangential acceleration (the vector product of the angular acceleration of the segment and it's position vector), and the normal acceleration (the cross product of the angular velocity and the cross product of the position vector and the angular velocity of the segment) ( $w \times (w \times r)$ ). A diagram of the segments and these formulas may be found in Appendix C.

### Single Plane Kinetics

The kinetic segmental linear and angular accelerations and the mass parameter estimates of the body segments were





incorporated into kinetic equations of motion for a mathematical model of the arm, as described by Zernicke(1977). The arm was modelled as a three-link rigid body system consisting of the upper arm segment, the lower arm segment, and the hand and ball segment. A free body diagram of these segments are reported in appendix D. The segments were assumed to be connected by hinge joints and friction at the joints was assumed to be negligible (Jensen, 1974). The forces and moments of force at each joint were calculated from the equations of Newtonian rigid-body dynamics. The general equations of motion consisted of two force equations;  $F_x = M \cdot Acc_x$  and  $F_y = M \cdot Acc_y$ , and one Moment of force equation;  $M = I_z \cdot \text{Alphaz}$  (Meriam, 1975:240). For each rigid body, the sum of the forces, either horizontal ( $F_x$ ) or vertical ( $F_y$ ), was equivalent to the product of the segment mass( $m$ ) and the corresponding horizontal or vertical acceleration of the mass center of that segment. Similarly, the sum of the moments of force ( $M_z$ ) perpendicular to the plane of the motion was equal to the product of the segment's angular acceleration and the appropriate mass moment of inertia at the segment's center of mass (Zernicke, 1977:180).

Equations were developed to determine the magnitudes of the moments of force at the three joints of the upper extremity. These equations were modelled after those of Dillman(1970) in which the muscle forces acting on each of the segments to provide movement at the joints were replaced



by an equivalent force at the joint and a couple causing rotation at the joint. These free body diagrams and equations were reported by Miller and Nelson (1973). It was therefore possible to determine the resultant joint torques at each joint, and to estimate their magnitudes and directions. The diagrams and equations used in the present study to calculate these kinetic parameters are reported in Appendix E. These joint torques are believed by many biomechanics researchers (Ariel, 1974; Plagenhoef, 1971) to be an indication of the most important muscle group acting at a particular instant in the performance of a skill. Dillman (1970) has conducted an extensive study of the magnitudes of these joint torques and their effects on movements during a performance.

### Three Dimensional Analysis

To determine the locations of the points of interest of the throwing arm in three-space, it was necessary to digitize these points for the sixty frames of interest from the film from both of the cameras. The film was analyzed frame-by-frame, so that for each frame twenty two points were digitized using the HP digitizing board. These points included the segmental endpoints of each of the body segments, as well as a reference point in each frame, and the center of the ball. These points were read into the HP 9825 calculator, and stored on HP cassette tapes one frame





at a time. This procedure was carried out for one complete pitch for each of the four subjects. Since one complete pitch normally occurred in sixty frames, and the pitch was filmed from two cameras, each pitch required one-hundred and twenty frames of digitized data. This data stored on cassette tapes was then read into the Ahmdal 460V/6 computer by means of the interface with the HP 9825 and the accompanying programs described earlier.

The single most critical problem to be solved in this analysis was that of the synchronization of the film frames of each pitch. Although the cameras were both started at the same time, and the frame rate was the same for each camera, the film was in a slightly different position in the camera for each pitch. This caused the film data to be slightly out of phase, and so produced some inaccuracies in the spatial coordinates. However, the films were synchronized by a frame-by-frame analysis by the author, in which the frames occurring at the same time (ie. containing a light flash from the timer), were marked with a marking pen. During the digitizing process, these frames were carefully synchronized by numbering them consecutively for storage.

Since the three-dimensional analysis program was based on the accuracy of the digitized data, it was then necessary to correct each of the digitized points for a common reference point. A Fortran program was written by the author to perform these corrections on each of the data points. The digitized points from each of the cameras were then read in



to a three dimensional analysis program written by Van Gheluwe(1977), which was subsequently adapted by the author to run on the University of Alberta computer system. This program accepted as input the digitized points from each of the cameras, and from these points the spatial coordinates of each of these points are calculated. The program was based on the determination of the location of each of the cameras in space by their positions in relation to the 'tree', or set of orthogonal axes described earlier. This tree was filmed by each of the cameras for each of the subjects, and twenty-two points were digitized from the tree from each of the camera views. For a detailed description of this program, see Appendix B.

Using this program, then, the spatial coordinates of the four segmental endpoints of the pitching arm, as well as the center of the ball, were determined. Each of these points then had a set of X,Y, and Z values for each of the frames digitized. From these X,Y, and Z values it was then possible to calculate the displacement, velocity, and acceleration values in each of these three directions . A computer program was written by the author to calculate these smoothed values using the IMSL cubic spline routine. The calculated linear velocity values for each of the X,Y, and Z directions were then graphed against time, and compared to the previously calculated X and Y values. The graph of the Z velocity values were of particular interest to determine the relative magnitude of these in comparison





to those in the X-Y plane.

### Three Dimensional Angular Velocities

The angular motions of interest in this section of the analysis were primarily those motions occurring around the longitudinal axes of the arm segments. No previous studies were located in which these rotations were estimated by vector analysis methods in a vigorous, high speed activity. Gowitzke and Waddell(1977) attempted to determine the magnitudes of forearm and upper arm rotations in the badminton overhead clear by measuring the displacement of a tape strip filmed on the arm segments. However, this method is open to question because of the assumptions made that the movement of the tape marker is like the movement on the arc of a circle. Also the radius of the circle(the arm segment) may only be roughly estimated.

The present analysis was carried out on the lower arm segment motions during the pitch of two of the subjects. In order to calculate the magnitude of the angular velocity of this segment in relation to the major reference system, it was necessary to determine the X,Y, and Z coordinates of three non-collinear points on this segment through the desired range of movement. These points were designated as: the joint marker on the lateral aspect of the elbow joint, and the joint markers on the medial and the lateral sides of the wrist joints. These three points on the lower arm





segment, as well as the shoulder joint and the tip of the third finger were digitized for each subject for the eight frames during release of the ball, from each of the two cameras. These five points from each of the films were then input into the three-dimensional analysis program, and the X,Y, and Z coordinates of each of the points were then determined.

Since the positions of each of these points over this eight frames was now available, the displacements, velocities and accelerations of each of the points were then calculated. These calculations were carried out by a computer program written by the author, in which each of the X,Y and Z coordinates were read into the IMSL smoothing program and the required velocities were produced as output. These linear velocities were then further utilized to calculate the magnitude of the total angular velocity of this segment in relation to the original X,Y, and Z axes. The equations used to determine these parameters are reported in Appendix D.

In order to calculate the angular velocities of the lower arm segment around a set of axes passing through the actual segment, it was then necessary to define this set of axes. The position vectors defining this set of axes were determined by use of the spatial coordinates of the other segmental endpoints digitized in this analysis (Appendix D.). Since the total angular velocity components were determined, and the position vectors were then defined, it



was then possible to define three equations in three unknowns for the scalar product of these components. The solutions for these three equations contained the three angular velocity components for the lower arm segment (Appendix D). A computer program was written by the author in which the above calculations were carried out from the X, Y, and Z input data. The output consisted of the solutions to the three equations, which were the angular velocity estimates. Although in the present study the calculations were carried out for only one of the arm segments, this method made it possible to determine the magnitudes of these rotations for any of the body segments.





## CHAPTER IV

### Results and Discussion

The results of the analysis of the windmill pitch in softball are subdivided into the following general topics:

1. Introduction to Analysis of Results
2. Individual Subject Data
3. Description of the Pitching Motion
4. Ball Velocities
5. Ground Reaction Forces
6. Angular Kinematics
7. Linear Kinematics
8. Linear and Angular Kinetics
9. Three Dimensional Analysis
10. Three Dimensional Angular Velocities

#### Introduction to Analysis of Results

The analysis of human performance from a quantitative, mechanical point of view is subject to certain inaccuracies due to unavoidable assumptions in the modelling of the movement. The body is assumed to be an assemblage of rigid segments, which is obviously not the case since these segments are constantly changing due to tissue deformations, blood movement, and changing concentrations of substances in the tissues. The joints are assumed to be simple pinned joints which allow movement in only one plane, when in fact there are movements occurring in all three planes in the joints of the upper extremity. The masses and



moments of inertia of the body segments are estimated from other studies, in which these measurements are determined from cadaver data, or from averages determined from a large number of subjects. Movement techniques are very individual, and depend on such characteristics of the performer as speed, strength, body build, and temperament. Therefore, any attempt to describe the characteristics of a movement in quantitative terms is subject to a certain amount of error. However, studies of this type will help us to a greater understanding of the kinetic and kinematic parameters involved in skilled performance, and in that way provide greater insight to teachers and coaches of these skills.

Although many experimenters are engaged in the applications of classical mechanics to human movement, the many estimated parameters make these studies inaccurate in many cases (Ayoub, 1974). It is often not possible to explain all the quantitative numerical results on the basis of efficient mechanics. Nubar and Contini (1961) have postulated what they have called the 'minimal principle', such that only as much muscle force as is necessary to provide for the efficient movement of the body part is applied. However, this theory has not been verified by the results of studies which have examined the magnitudes of such forces at the joints.



## Individual Subject Data

The anthropometric and personal data of each of the subjects is summarized in Table II. There was a wide range

TABLE II.—INDIVIDUAL-SUBJECT-DATA

SUBJECT	DS	BL	SW	CM
SEX	MALE	FEMALE	FEMALE	MALE
PARAMETER				
AGE	38	32	19	23
HEIGHT (CM.)	193.0	177.8	175.3	185.4
WEIGHT (KG.)	106.6	74.84	72.57	89.36
UPPER ARM LENGTH (CM.)	38.	33.	31.	34.5
BICEPS DIAMETER (CM.) (RELAXED)	37.	28.	29.5	35.
(FLEXED)	40.	29.5	32.	38.5
LOWER ARM LENGTH (CM.)	29.	28.	27.	29.5
WRIST DIAMETER (CM.)	21.	16.5	16.	18.5
HAND LENGTH (CM.)	20.5	18.5	19.	19.5
HAND SPAN (CM.)	26.	20.	19.	23.

of ages in the four subjects tested, from the youngest female at 19 years, to the oldest male at 38 years. It is notable that these two subjects at the extremes of age were judged to be the two most highly skilled of the pitchers tested. It is also notable that many of the anthropometric





measures are much larger than those for the average person, as reported in the tables of the most recent anthropometric data available. (Diffrient, 1974) The average height for a large-framed male was estimated (from the tables) to be 188 cm, while Subject DS was 193.0 cm tall. The average height reported for a large-framed female was 174 cm, while Subject BL was 177.8 cm tall. The average weight for a large male was estimated at 87.1 kg, while Subject DS weighed 106.6 kg; the female tested was also considerably heavier than the normal for a large person. Since all of the subjects tested were above the 90th percentile in terms of their height and weight compared to the average person, this may indicate that a prerequisite for successful pitching in the game of softball is size.

The individual anthropometric measurements of the upper extremity of the subjects were also well above the average measures published as being those of a large person (Table II). For example, the upper arm length of a large male was estimated at 30.2 cm (Diffrient, 1974), while the present Subject DS had a measured upper arm length of 38 cm. Similarly, the average flexed biceps diameter for a large male was reported to be 35.8 cm, while that of DS was measured to be 40.0 cm. The largest subject in the present study was found to be up to 25 per cent larger than the largest subject reported in current literature, and this difference was apparent in both the male and female subjects. These results possibly suggest that highly skilled



softball pitchers are generally much larger than the average person, and that in order to be a successful pitcher the individual should possess this exceptional size.

The subjects chosen for the present study were the most highly skilled available to the investigator at the time of the study, and the summaries of their softball experiences will verify this conclusion. The summaries are included in Appendix D, page . All subjects had had at least some national exposure, being involved in some level of National Championships. The most highly skilled male subject had led his team to the Western Canadian Men's Fastball League Championship last year (1977). The most highly skilled female had led the Alberta Provincial Team to a third-place finish at the Canada Summer Games in Newfoundland in 1977. Although the other two pitchers were not actively involved in 'A' level softball in the past year, both had some experience at this level in their careers.

#### Description of the Pitching Motion

The film of the four highly skilled subjects was viewed numerous times by the present investigator, and the following description represents the skill as it was performed by at least three of the subjects. Sequence Photographs taken directly from the film of subjects 1 and 2 are found in Figures 1 and 2. The total motion of the windmill pitch takes only .4 to .5 second to perform, from the presentation position which signals the start of the pitch, to the time the ball actually leaves the hand of the





pitcher. The temporal characteristics of the softball pitch are reported in Table III. The time reported for each pitch

Table III Stride Length and Temporal Characteristics of Pitchers

Subject	DS	BL	SW	CM
Average Stride Length (Metres)	1.019	1.102	1.196	1.50
% of Height	52.79	61.97	68.22	80.90
Time for Complete Pitch (Sec)	.55	.69	.56	.60
Time to Top of Backswing (S)	.40	.52	.41	.45
Time from Top of BS to Release (S)	.15	.16	.15	.15

was taken as the time from the end of the presentation phase of the pitch to the point at which the ball is released. It should be noted that this time was affected by extraneous motions of the pitcher following separation of the hands. For example, Subject BL moved her pitching arm backward after separation, and this motion accounted for the longer period of time taken by this subject in the actual delivery of the ball. Otherwise, the average time taken for the pitcher to deliver the ball to the batter was between .50 and .60 seconds, which was a relatively short time to impart such a large velocity to the ball. The time taken for the actual downswing of the pitching arm prior to delivery was



approximately .15 seconds, which indicates that the majority of the forceful muscle activity of the pitching arm occurs in this short time period.

The presentation position is one in which the pitcher must stand motionless with both feet in contact with the pitcher's board, with the ball held with both hands in front of the pitcher. This position must be held for at least two seconds prior to the beginning of the pitch, according to the Official Rules (1978:13). This position is illustrated in Figures 1A and 2A. From this position, two movements occur simultaneously: the hands separate and the arm is flexed at the shoulder to raise the ball in line with a position approximately opposite the midline of the trunk. At the same time, the left leg is raised and the pitcher commences to step forward onto this foot. Thus these two movements are occurring simultaneously, and in a coordinated pattern as is seen in taking a normal walking step forward--the right hip and the left shoulder are both flexing and raising their respective limbs upward and forward from their starting positions. This pattern is also notable in that the angular displacement of each of these limbs is occurring at the same rate, so that their respective angular velocities are similar for the first part of the movement. The coordinated pattern of movement such as this one described for these highly skilled performers serve to illustrate the many factors which comprise a high level performance. These movements are illustrated in Figures 1A-G, 2A-G. This pattern



is likely facilitated by the action of the crossed extensor reflex, in which the movement in one limb is accompanied by increased tonus in the muscles of the contralateral limb. Thus in this case the extensor muscles of the right lower extremity are facilitated by increased tonus, along with the extensors of the left upper extremity. In the contralateral limbs, the extensor tone is inhibited, and thus flexor tone is facilitated.

As the right arm and the left leg are moving upward and forward during this phase of the delivery, the right hip, knee and ankle are being rapidly and forcefully extended to drive the body forward onto the left foot. Since it is commonly accepted that one of the characteristics of a highly skilled pitcher is an extremely long step into the pitch, it was expected that the present performers all used such a step. The measurements of the length of the stride into the pitch are reported in Table III, first as an absolute length and then as a percentage of the subject's height. An earlier study of a highly skilled softball pitcher (Zollinger, 1973) reported that the average stride length was 68 per cent of the performer's height, which was very close to the findings in the present study. Subject SW had a stride length of almost exactly that of the skilled pitcher in the above study, while BL and DS had one somewhat shorter. Subject CM had an exceptionally long stride length, but this was due to the long hop which he took on his right foot prior to placing his left foot on the ground. As was





stated earlier, although this method may have some advantage in imparting greater forces to the ball, it is illegal according to the rules of the game, and would likely be called as an illegal pitch in a game. The rule states clearly that "The pivot foot must remain in contact with the pitcher's plate until the other foot with which the pitcher steps toward home plate has touched the ground (CASA, 1968:13)."

Another important motion occurring during this step is the rotation of the trunk laterally toward the side of the pitching arm. As the pitching arm is being raised forward and upward, the trunk is rotating to the right, so that the shoulder movement which was originally flexion, becomes abduction as the trunk twists (See Figure 1H-I, 2H-I). As the pitching arm reaches a position directly above the shoulder, the left foot contacts the ground as the step forward is completed (See Figure 1H, 2H). It is notable that the pitching arm remains relatively straight during this part of the motion, maintaining an angle at the elbow joint of approximately 170 degrees. The wrist joint also actually maintains a relatively stable position throughout the windup, but it appears to be undergoing changes due to the rotation occurring in the upper arm and shoulder. When the left foot is firmly planted on the ground in a position directly in front of the pitcher, the body weight is shifted onto this foot (See Figure 1I-K, 2I-K). The foot is planted so that the toe is pointing toward home plate, as this





A



B



C



D

**E****F**

G



H



1



J

**K**

L



M



N



O

Figure 1. Sequence Photographs of Subject 1.







A



B



C



D



E



F



G



H



I



J



K



L



M



N



O

Figure 2. Sequence Photographs of Subject 2.



position of lateral rotation of the left hip allows for a full range of medial rotation of the trunk around this hip during delivery. Although three of the subjects in this study exhibited the above position of the left foot, one of the female performers placed this foot in a position at right angles to the direction of the pitch (See Figure 2I-K). It is notable that this position did in fact restrict the trunk rotation of this subject, who then exhibited little trunk rotation during delivery of the ball.

From this position with the arm directly overhead and the weight being taken on the left foot, the shoulder is now forcefully adducted and flexed to bring the ball around to the position of release. As the arm is moving forward and downward, the trunk is also undergoing rotation to the left-- this rotation consists of medial rotation of the left hip, as well as spinal rotation to the left. As the arm is moving downward, the distal segments are trailing the proximal segments--the upper arm segment is leading the motion, followed by the lower arm, and the hand-and-ball segment is trailing (See Figure 1I-J). This alignment is maintained up to .04 seconds before release, at which time the lower arm, and then the hand pass the upper arm segment (in terms of their angular positions from the right horizontal). The exact timing of the alignment of the arm segments during release will be described in a later section (See Figure J-L, 2J-L).

Probably the most notable movement occurring in the





upper limb during the softball pitch is the rotation of the forearm, accompanied by some rotation of the upper arm segment. The joint movement of importance consists of forceful and rapid pronation of the forearm, beginning at a point .03 seconds prior to release of the ball (See Figure 1J-L, 2J-L). This movement is undoubtedly a major contributor to the final velocity of the ball, accompanied by wrist flexion which is likely the result of the rapid pronation movement rather than the concentric contraction of the wrist flexors. Zollinger (1973) has noted that "the wrist was fully flexed at the release", which was also observed in this study although this wrist flexion movement by itself may not be of major importance in contributing to the velocity of the ball.

The ball is released at a point approximately opposite to the midline of the body, or in a position just after the hand and ball pass the right leg (See Figure 1L, 2M). At this point in the pitch, the weight shifted completely onto the left foot, and the back foot lost contact with the pitching rubber. It is notable that although the rules of softball state (CASA, 1978:13) that the pitcher must remain in contact with the pitching rubber until the other foot with which the pitcher steps toward home plate has touched the ground, this rule is often broken in practice. Of the subjects filmed in the present study, three of the subjects managed to keep the back foot in contact with the force plate until the front foot touched the ground.. One of the subjects was



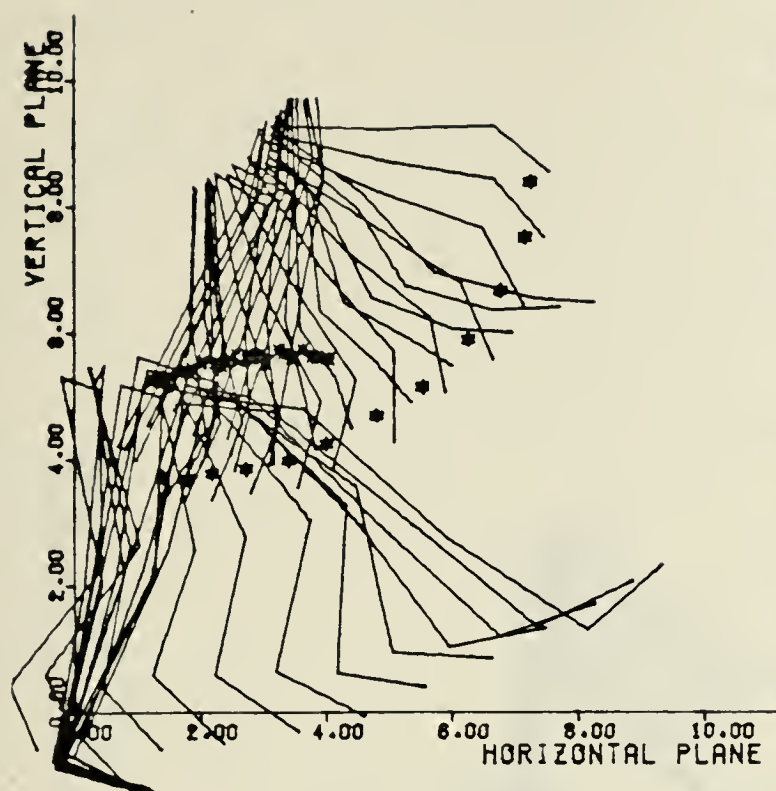


consistently over one meter in front of the rubber at the time of release--this style of pitching would almost certainly be called as an illegal pitch by the umpire in a game situation.

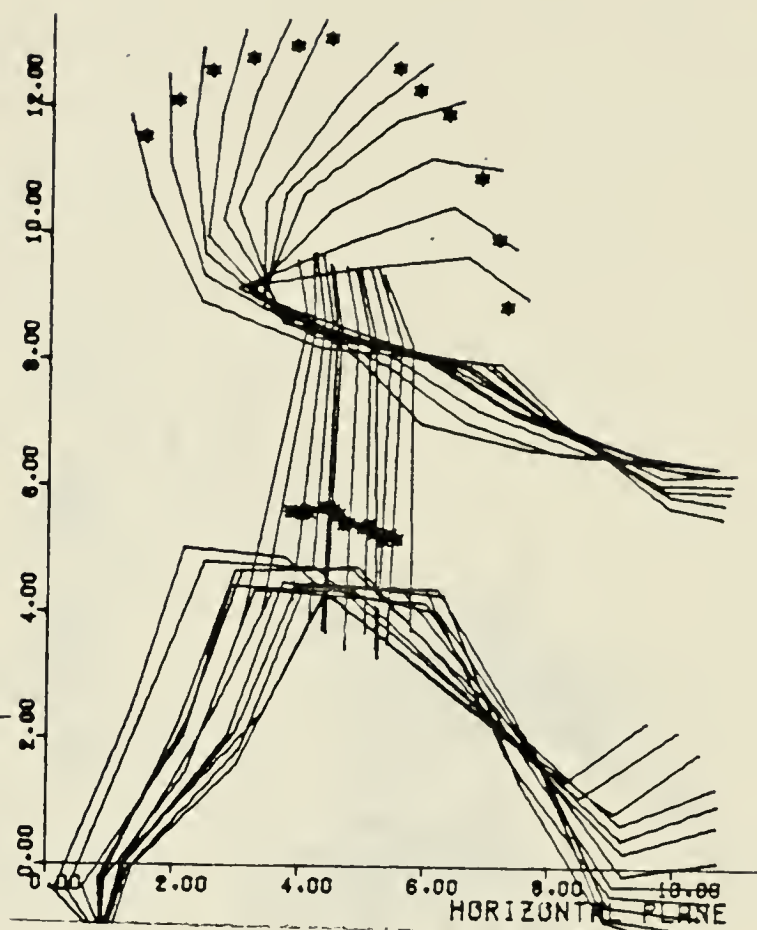
The pitching arm continues to flex at the shoulder joint after release of the ball, so that the follow-through is completed with the hand in a position above the head (See Figure 10). Although the follow-through has no direct effect on the path of the ball after the ball has left the hand, a long follow-through is desirable to ensure that the pitching hand has not lost any velocity prior to release of the ball. Also, using a long range of movement through which to decelerate the segments of the pitching arm will ensure that the momentum of the arm is dissipated gradually to help prevent undue strain on the shoulder joint. The pitcher normally finishes in a position squarely facing the batter, with the feet parallel so that he is able to field any balls which may be hit directly back towards him.

The pitching motion of each of the subjects is further illustrated by computer-drawn plots of each of the body segments and the ball (See Figures 3,4). In the subsequent Figures, the subjects have been identified by number as follows: Subject 1-Dale Smith; Subject 2-Sue Wilcox; Subject 3-Bernice Lechner; Subject 4-Clint Marshall. This system of identification has been used throughout the remainder of the study. These plots were constructed from the digitized segmental endpoints of the best pitch of Subject 1 and

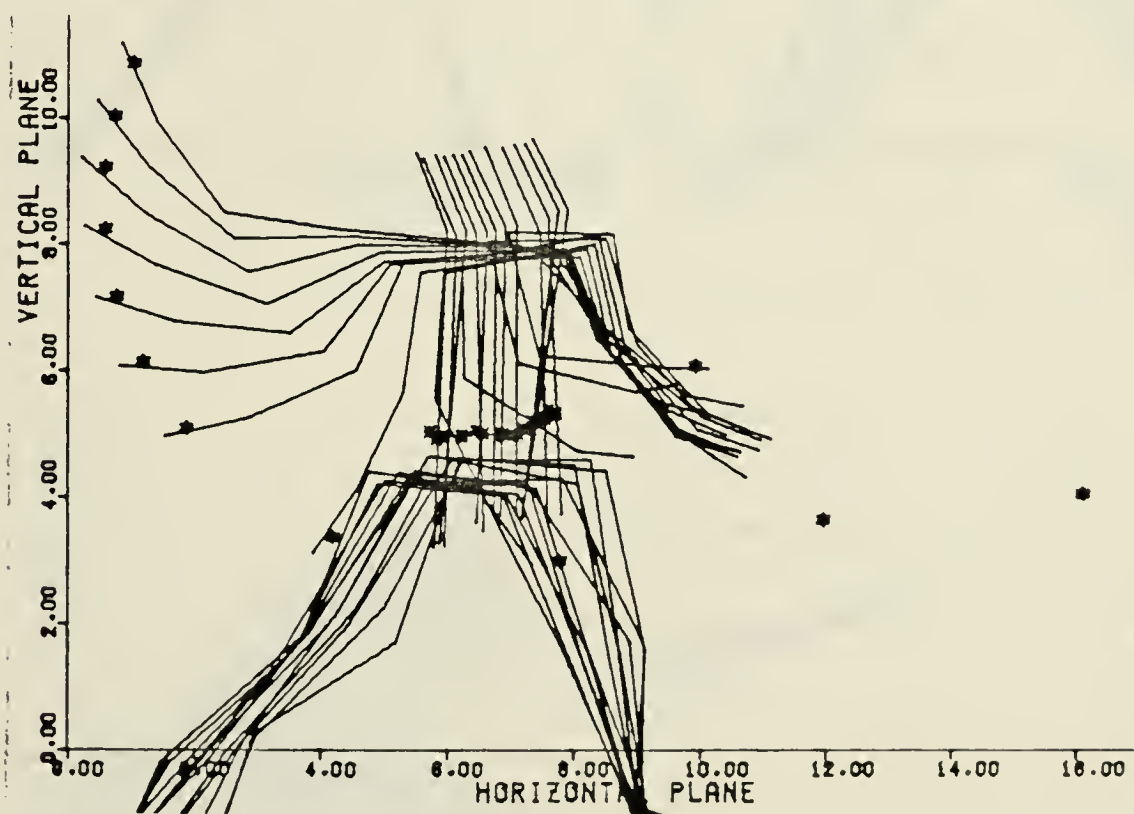




A



B



C

Figure 3. Pitching Motion of Subject 1.





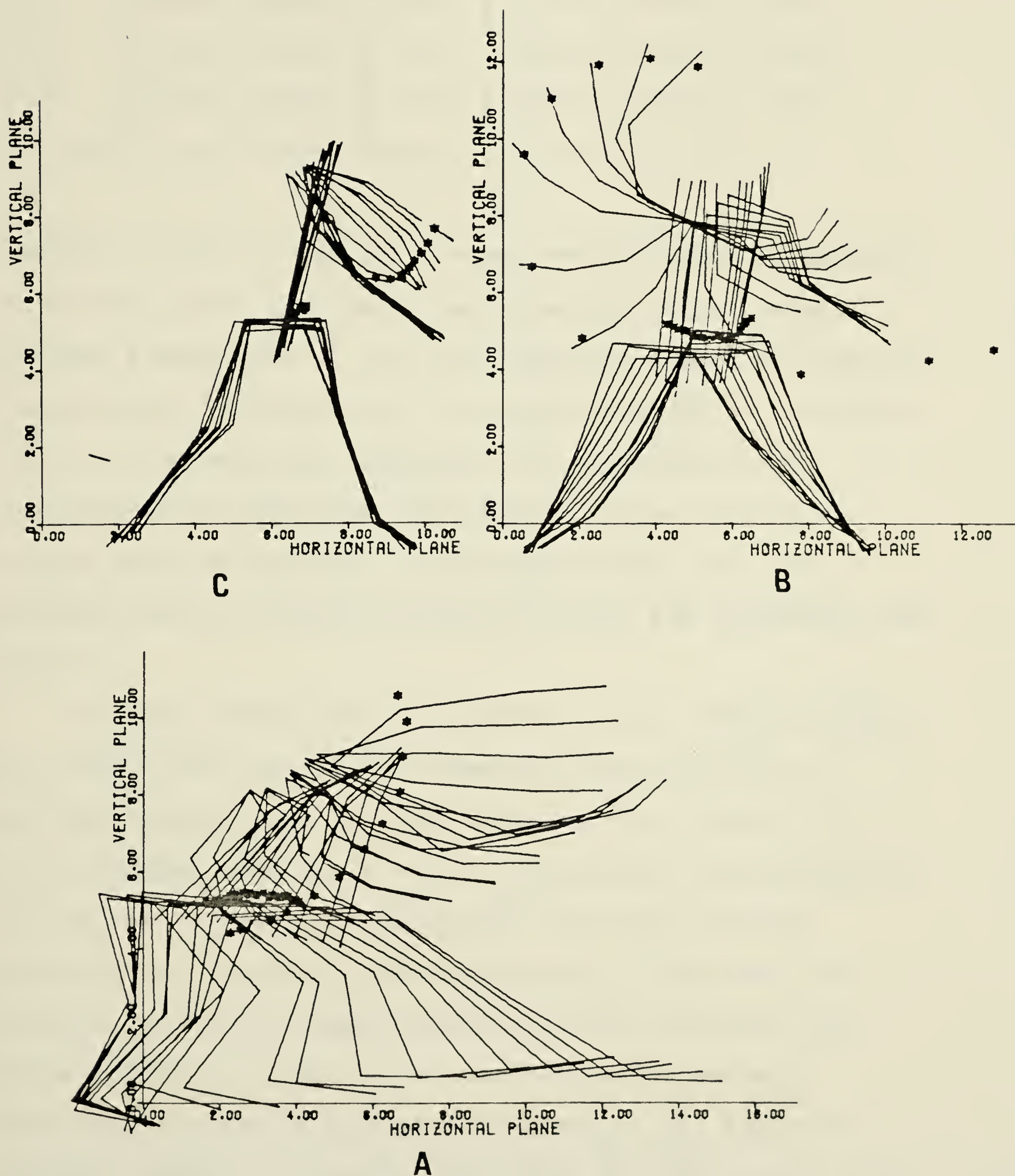


Figure 4. Pitching Motion of Subject 2.



Table IV Ball Velocities of Pitched Balls (Metres/Second)

Pitch#	1	2	3	4	5	Average
Subject						
DS	30.43	29.53	29.78	28.87	31.30	29.68
BL	24.42	25.17	24.67	23.97	24.06	24.46
SW	24.71	24.95	25.41	24.95	24.70	24.94
CM	32.22	32.72	32.11	32.88	32.38	32.46

Subject 2, and in most cases every second frame was plotted. Thus these plots represent time intervals of .02 seconds between frames. One of the most important values of plots of this type is to illustrate the consistency of the digitized data. If the segmental endpoints were inaccurately or inconsistently digitized, the plots would be erratic and errors would be apparent. In the case of the two plots included here, no highly inaccurate points are visible on the plots.

Another illustration of interest in the softball pitch is that of the path of the segmental endpoints for the pitching arm of each of these subjects (See Figure 5,6). These figures once again serve to illustrate the consistency of the path of these endpoints for the highly skilled pitchers in this study. The consistency of the point of release for each of these subjects is also apparent from these figures (1C,2B). As was noted from the sequence photographs reported earlier, the pitching arm follows a circular pathway throughout the windup for this skill, with



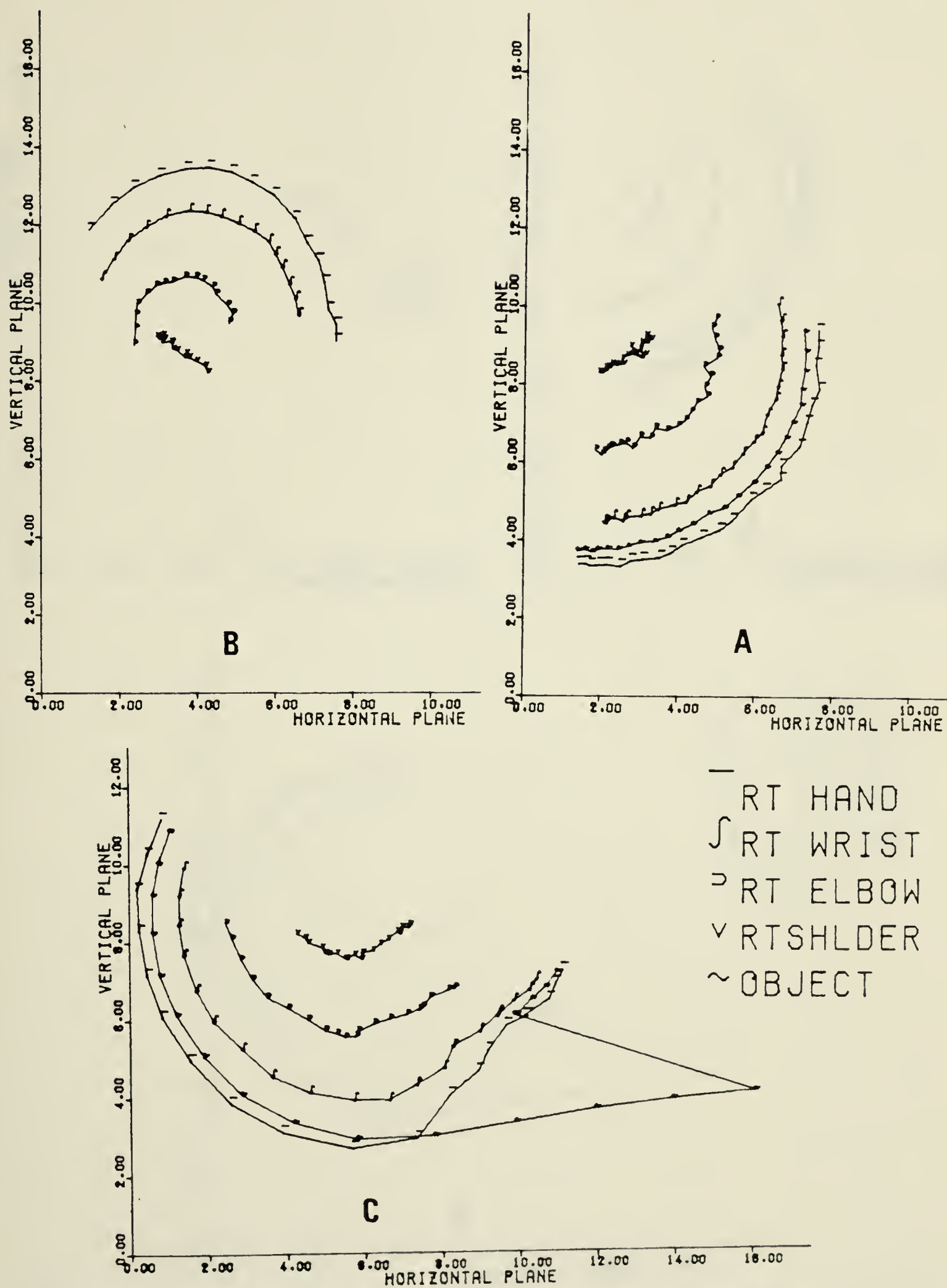


Figure 5. Path of Segmental Endpoints of Subject 1.





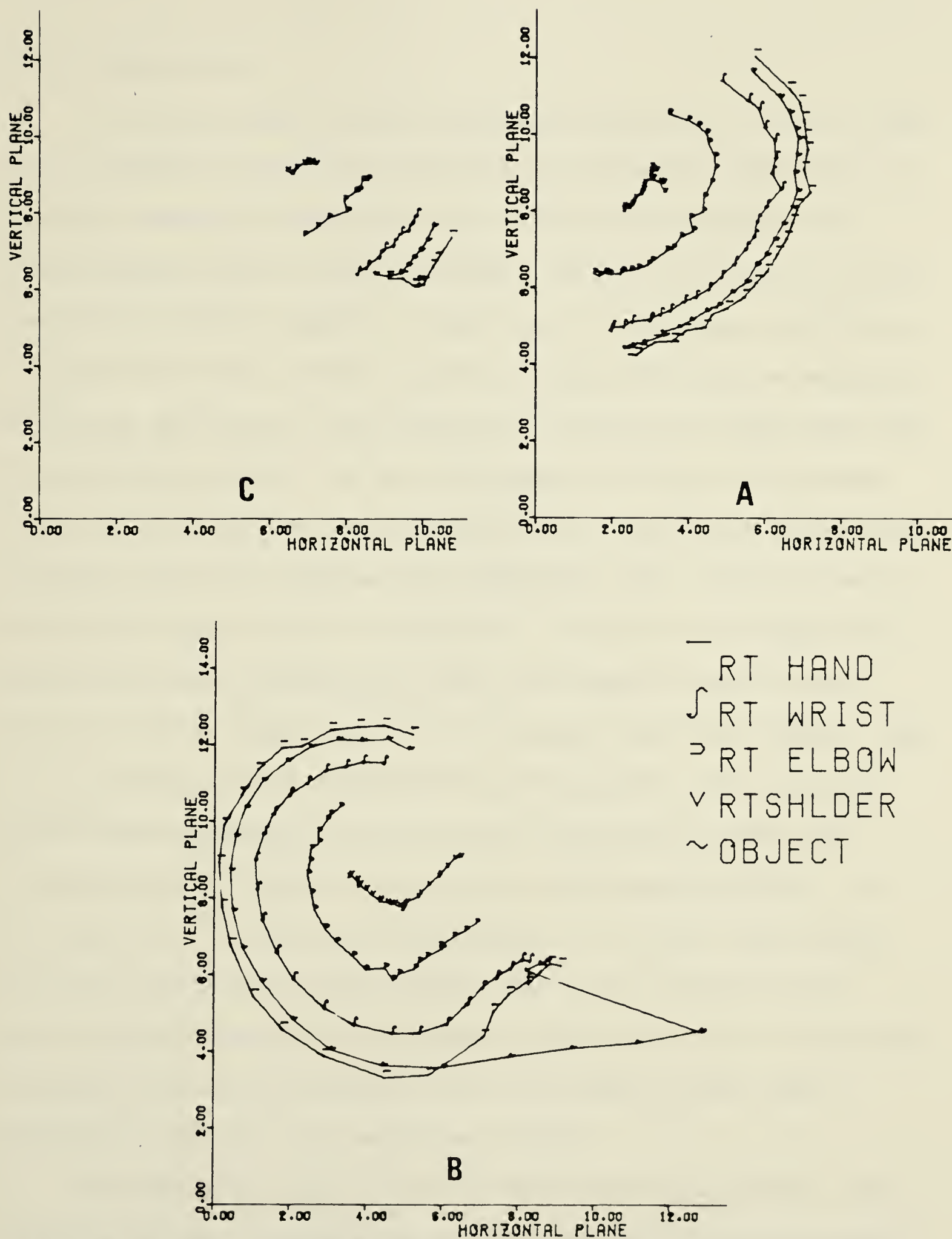


Figure 6. Path of Segmental Endpoints of Subject 2.



the velocity of the endpoint on the limb being maximal at release.

### Ball Velocities

The velocities for the best five pitches of each of the four pitchers tested are reported in Table IV. Although the fastest measured velocities were produced by Subject CM, this subject was the one mentioned earlier as being at least one meter off the rubber at the time of release. One of the reasons for this illegal pitching style was that he started with his left foot a good distance behind his right foot on the pitching rubber. He was then able to take a very long step into the pitch, and his body had a very high horizontal velocity into the release. In addition, this subject used a technique known as the 'crow-hop', in which the right foot drives the body forcefully from the rubber, takes a short hop, and then lands again some distance from the rubber, and the pitching motion proceeds from this point. It is clear that this technique may have some advantage in that the velocity of the body is once again increased markedly, but it must be noted that it is illegal. It is for this reason that the pitches of this Subject were not chosen for the most detailed analysis, although if the criterion of maximum velocity were used strictly for the choice of the most effective pitches, his would be chosen.

The measured velocities of these skilled pitchers were seen to be very consistent between pitches, and relatively





consistent between the male and the female performers. The pitches of DS were among those chosen for the most detailed analysis because these pitches were closest to a legal pitch in a game situation; as well as those of SW as these were the fastest of the female performers.

One further point regarding ball velocities during the pitch is the relationship between ball velocity and the velocity of the hand at release of the ball. For all of the pitches tested, the release velocity of the ball was found to be up to four or five meters per second faster than the velocity of the hand at release. This pattern has been noted earlier by Macmillan(1975) and Roberts and Metcalfe(1968), in studies of football kicking. Both these investigators found that the release velocity of the ball was considerably faster than the velocity of the foot at contact. Roberts and Metcalfe(1968:317) stated: "When contact is good the ball speed is 5 to 7 M/s faster than the foot". This pattern may be explained by the principle of transfer of momentum, whereby the mass times velocity of the hand and arm complex is so much greater than that of the ball's mass times velocity, that the release velocity of the ball after contact is greater than that of the hand. This does pose some interesting questions regarding the nature of the release of the ball by the pitcher, as it is possible that the efficiency of this release may be a factor in the efficiency of the transfer of momentum. More detailed analysis of this interaction is necessary before it is fully



understood.

### Ground Reaction Forces

The graphs of the calculated and the measured ground reaction forces are shown in Figures 7 and 8. Since the general shape of these curves is very similar, it may be concluded that the forces calculated from the mass center displacement data are reasonably accurate estimates of these forces. The force curves for Subject 1 (Figure 7) illustrate that the peak X force is exerted prior to the peak Y forces, and that there is in fact likely a summation effect of these two components of the ground reaction force. There is also a period of overlap of these two force curves seen in both of the representative curves, so that while the downward forces are decreasing in magnitude, the upward forces are increasing. This occurs during the windup at the time that the weight is being taken onto the front foot, and the body weight is actually moving downward onto this foot. At the same time the X forces are reaching their peak, as the pitcher is forcefully driving his body weight forward onto this left leg. The peak Y force is reached very close to the point of release of the ball, and is likely caused by a very forceful extension of the joints of the right leg as the subject drives his body upward and forward into the pitch. This forceful hip, knee and ankle extension is also accompanied by rapid and forceful rotation of the body



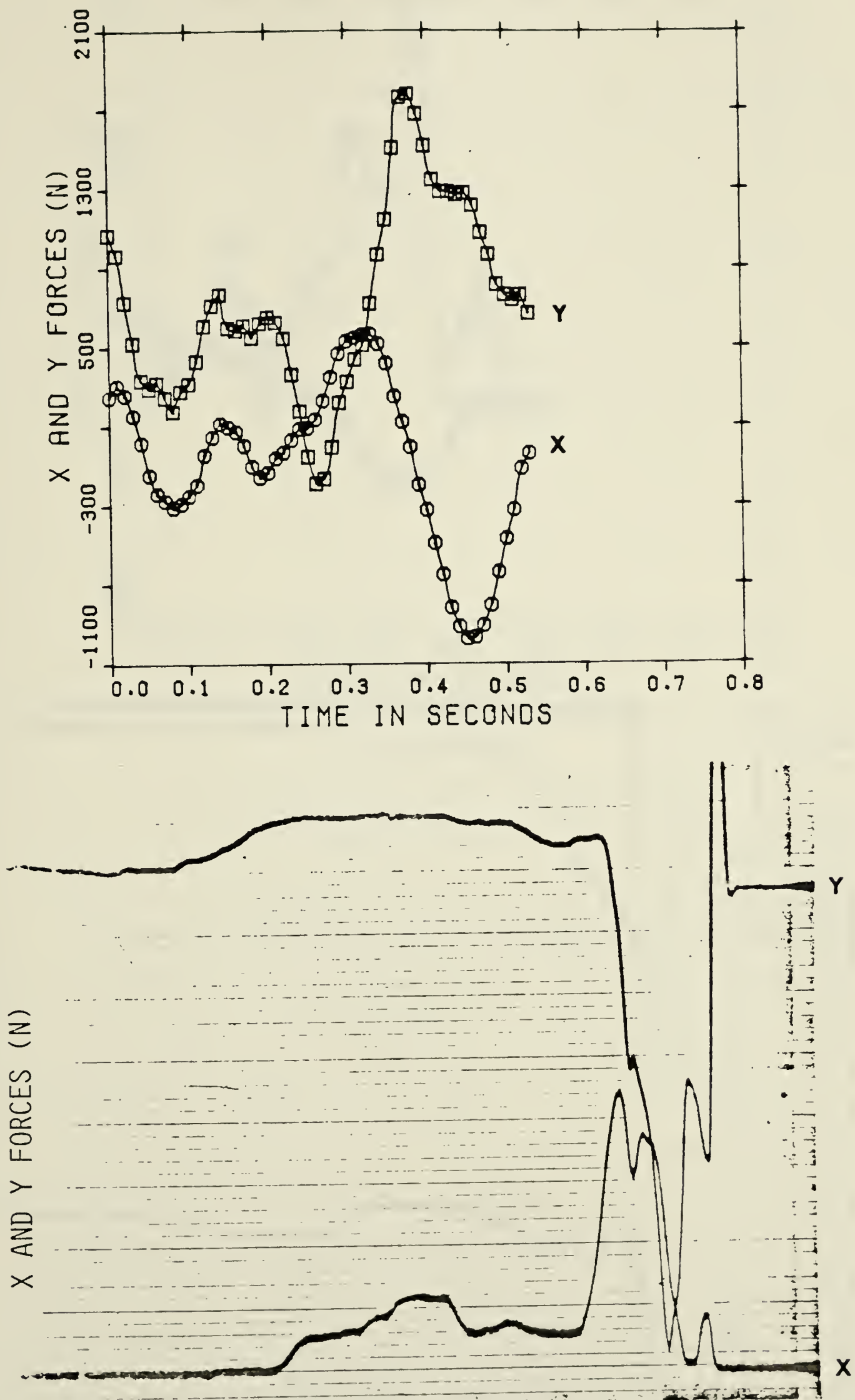


Figure 7. Ground Reaction Forces: Calculated and Force Platform Measures of Subject 1.





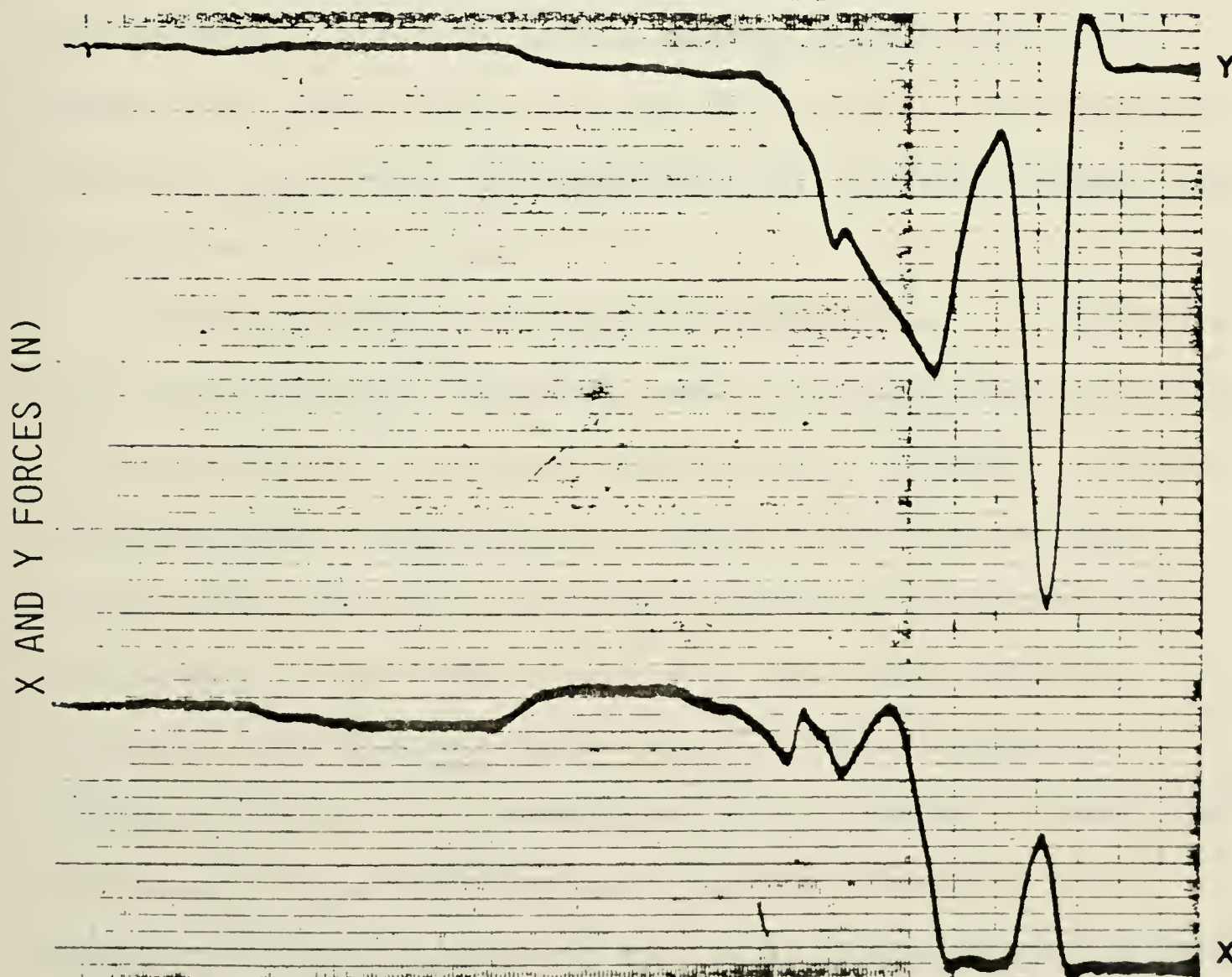
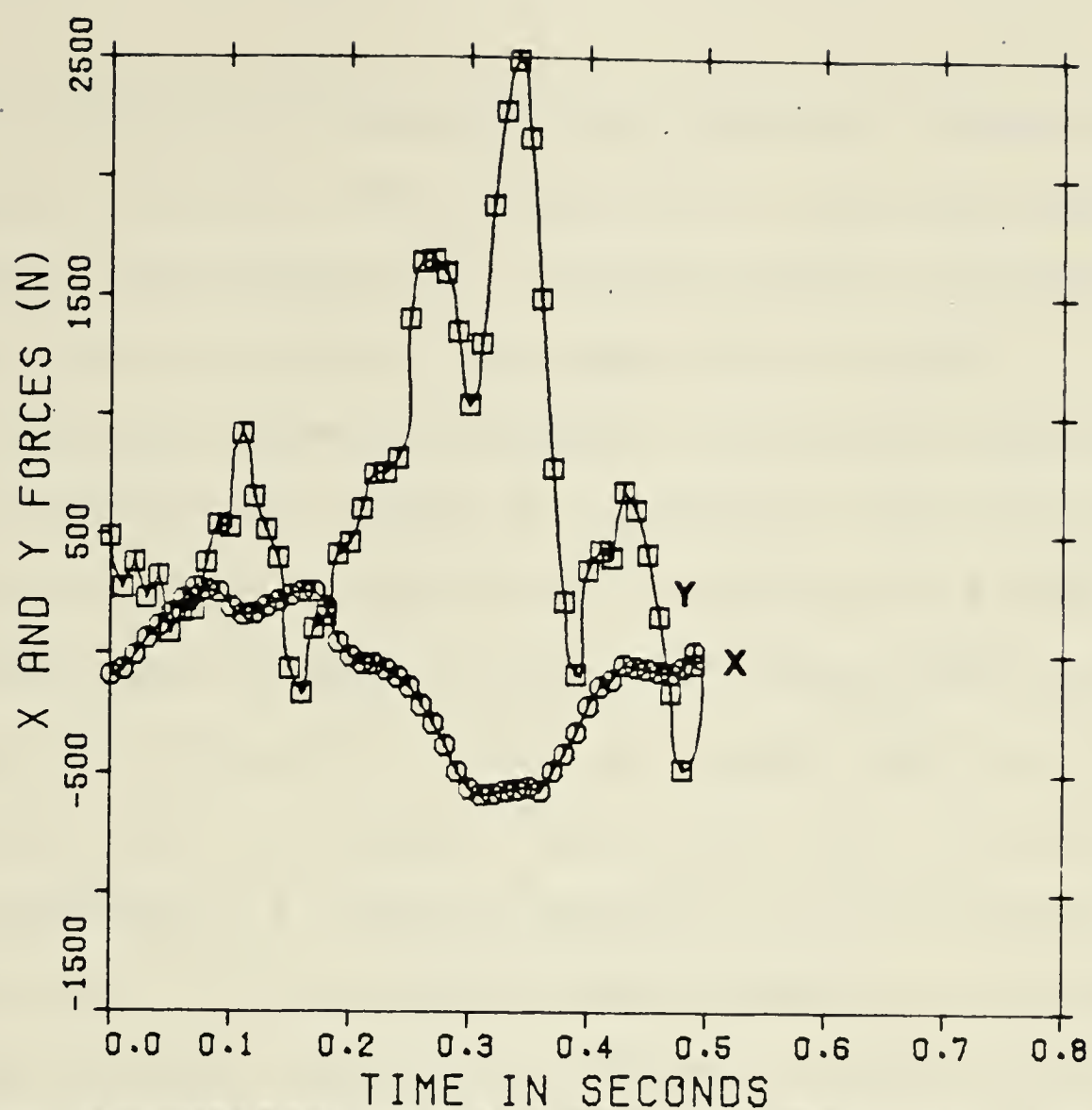


Figure 8. Ground Reaction Forces: Calculated and Force Platform Measures of Subject 2.



around the left hip (lateral body rotation). These rapid leg extension movements are accompanied by the rapid shoulder adduction and flexion--all of which produce downward forces which cause the peak at this point in the skill.

The force curves for Subject 2 are quite different from those produced for Subject 1, indicating that highly skilled performers may be exerting their body forces in quite different ways to produce a similar skilled performance (Figure 8). The peak X forces are reached much earlier in the skill for this subject, and in fact the X forces are being exerted in a negative direction at the time of release of the ball for this subject. The Y forces are somewhat similar to those exhibited by Subject 1, and in fact the peak of the Y ground reaction forces occurs at almost exactly the same instant in the delivery for each of the subjects. This point is approximately .04-.05 seconds prior to release of the ball.

Although this is a very noticeable peak, a recent study has indicated that a greater peak of ground reaction forces is not necessarily better. Kermond and Konz(1978) studied the force plate tracings of a highly skilled football kicker, and they found that the vertical force peak was significantly inversely related to the predicted kick distance. They stated: "This implies that a greater predicted distance is associated with a lesser ground force reaction. In practical terms, a kicker should try to maximize the force transfer to the ball and minimize the





amount of pushing down on the ground with the support leg. It implies that the support leg ought to 'caress' the ground rather than 'stomp' on it (1978:76)". However, these authors attempted no real explanation for this phenomenon, and in fact there are few explanations to verify this conclusion. It would seem more likely that a greater vertical force component would produce a greater force against the ball. More study is needed to examine this question.

## Angular Kinematics

### Angular Displacements

The angular displacements of each of the arm segments against time are shown in Figures 9, 16, 23, 30, 37 and the numerical values of these measurements are reported in Appendix G, Raw Data Tables. The angular displacements have been determined by two independent sets of digitized data--the first set of displacements were digitized from the beginning of the windup (.40 secs) and every second frame was digitized through release and followthrough; and the second set of displacements was digitized from a point at the top of the backswing (.20 secs) and every frame was digitized through release and follow-through. The two sets of data for each pitch then included: a larger overview of the entire pitching motion, and a more detailed view of the frame-by-frame analysis of the motion of the segments through release. There were therefore two separate sets of



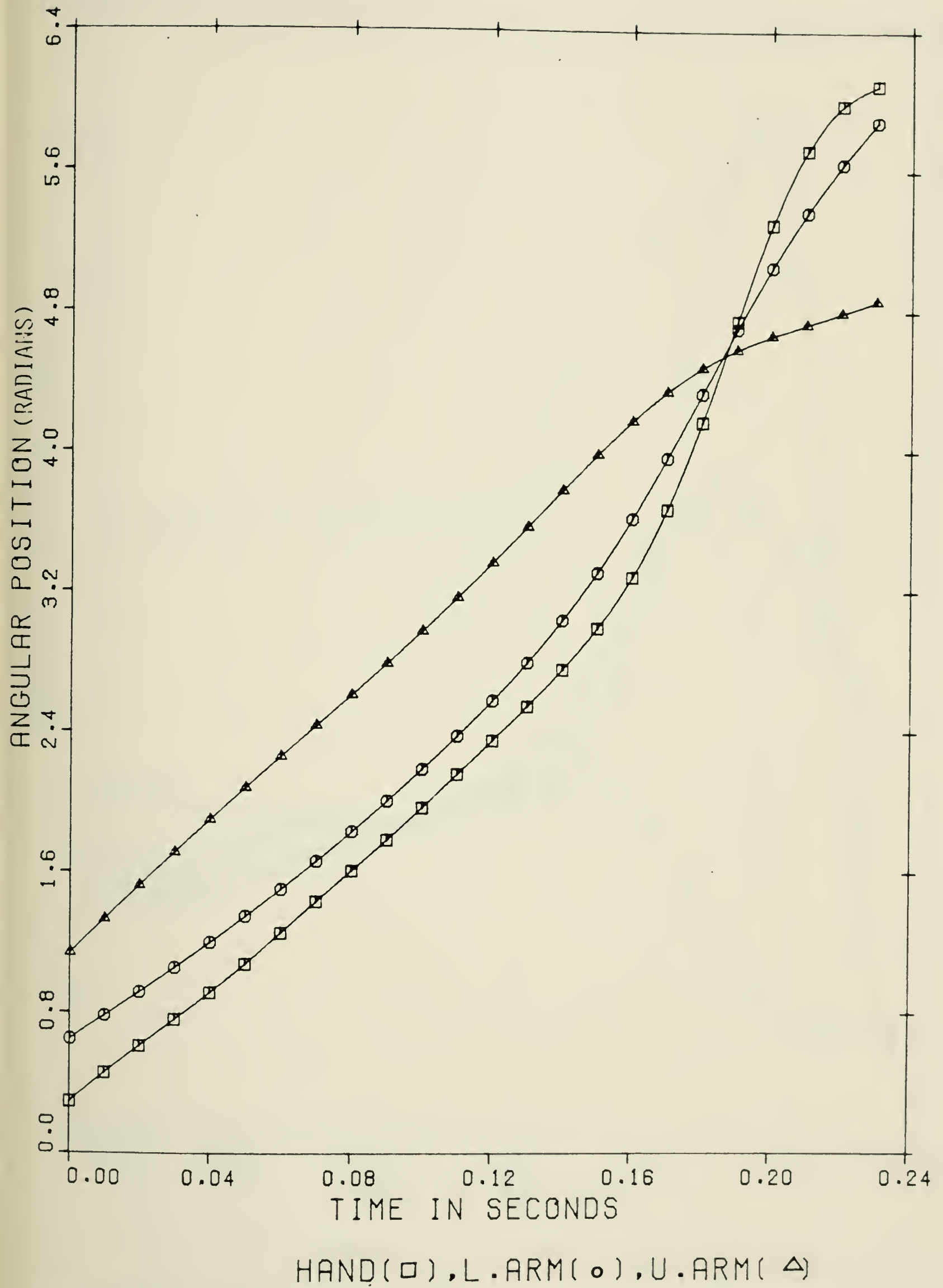


Figure 9. Angular Position vs Time of the Arm Segments for Subject 1.



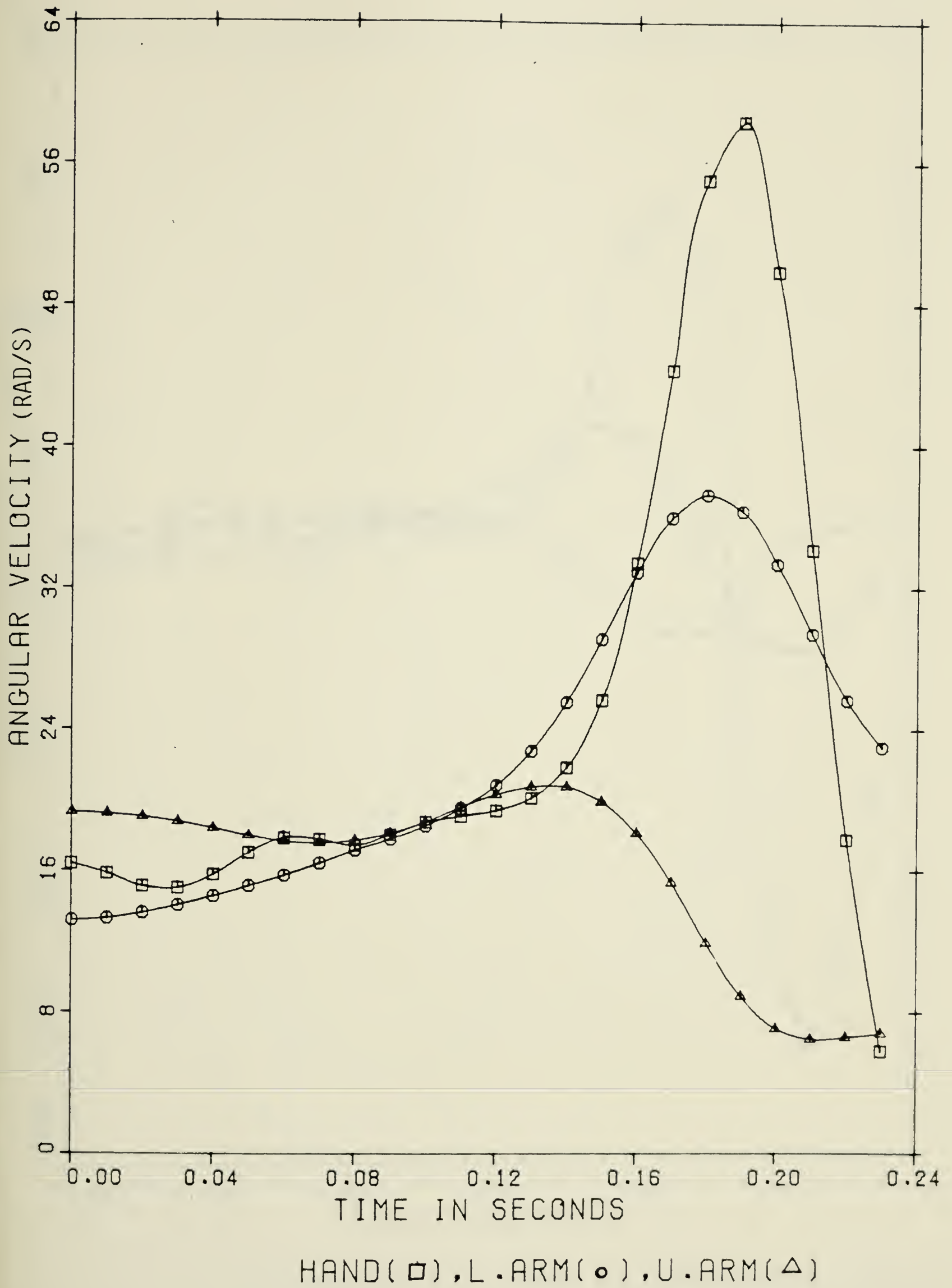


Figure 10. Angular Velocity vs Time of the Arm Segments for Subject 1.





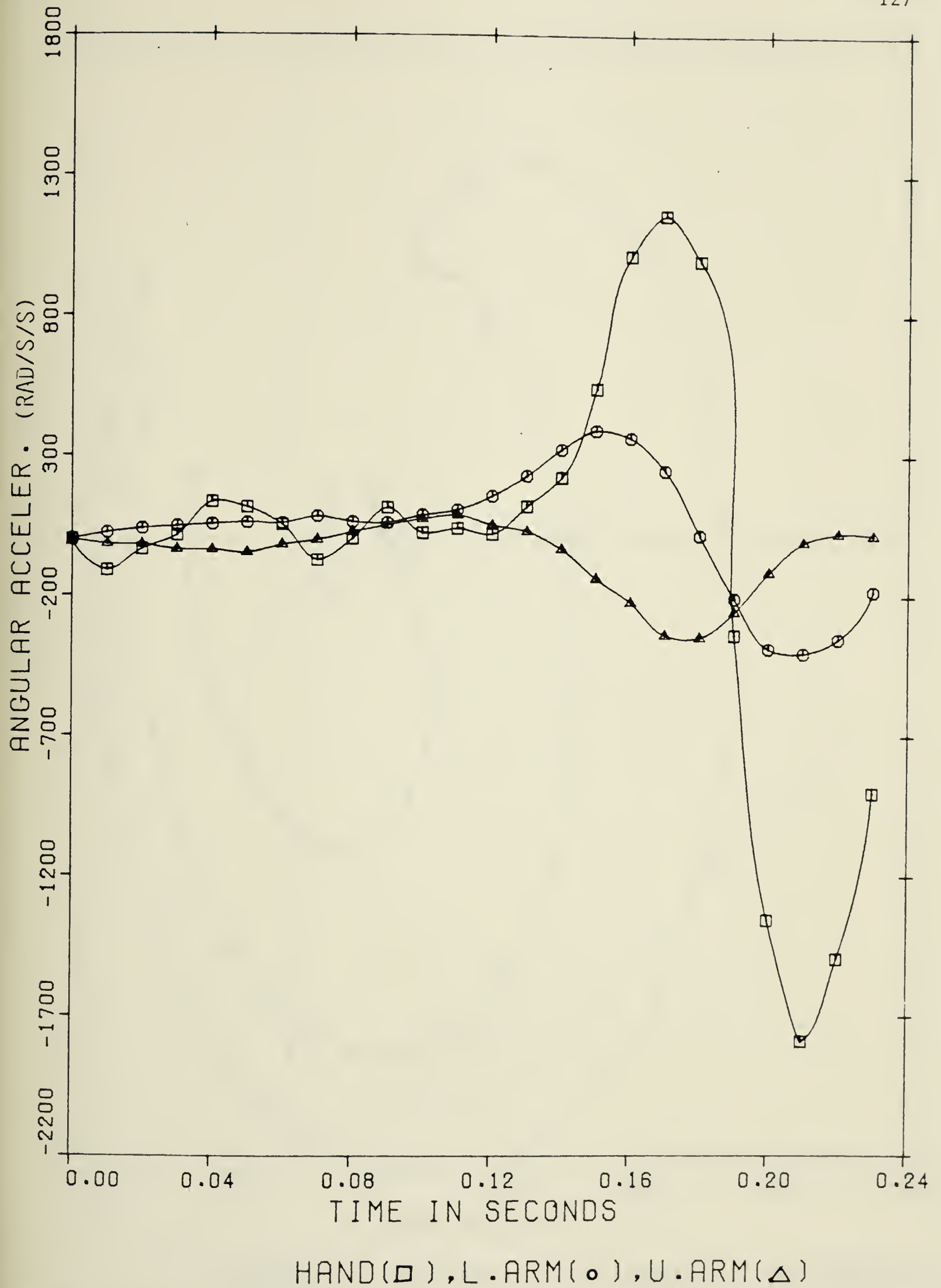
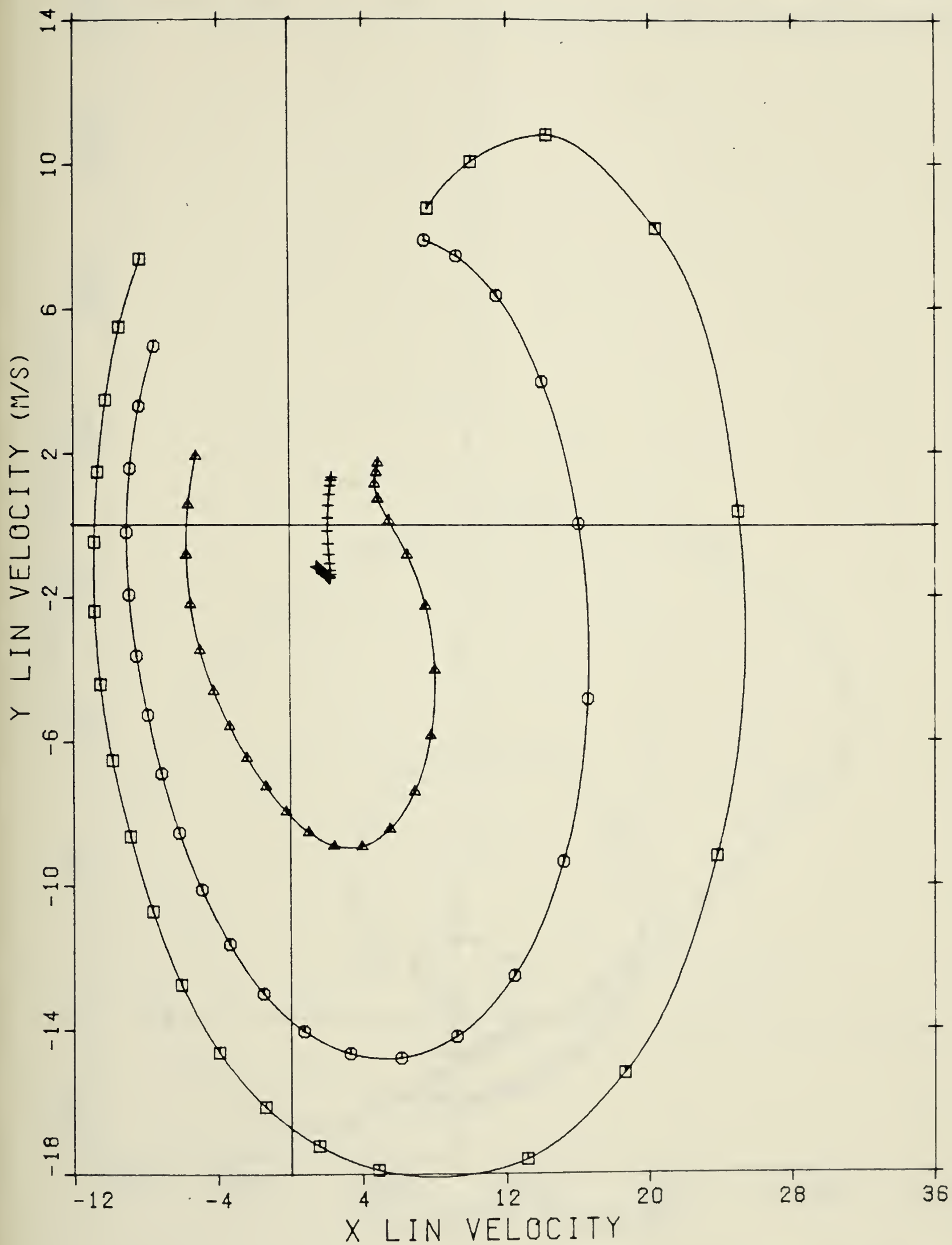


Figure 11. Angular Acceleration vs Time of the Arm Segments for Subject 1.





HAND( $\square$ ), WRIST( $\circ$ ), ELBOW( $\triangle$ ), SHLDR( $+$ )

Figure 12. X and Y Linear Velocities of the Segmental Endpoints for Subject 1.





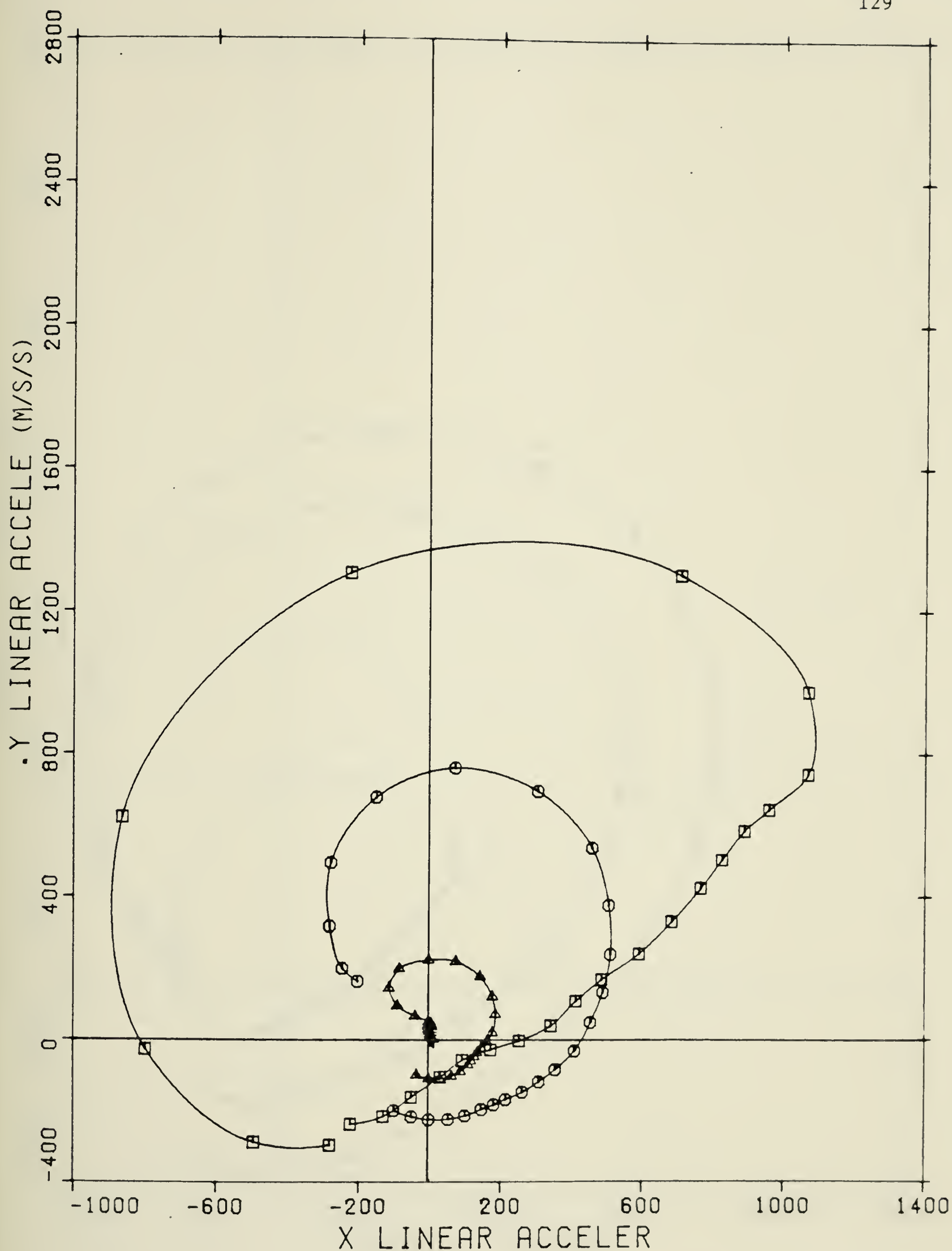
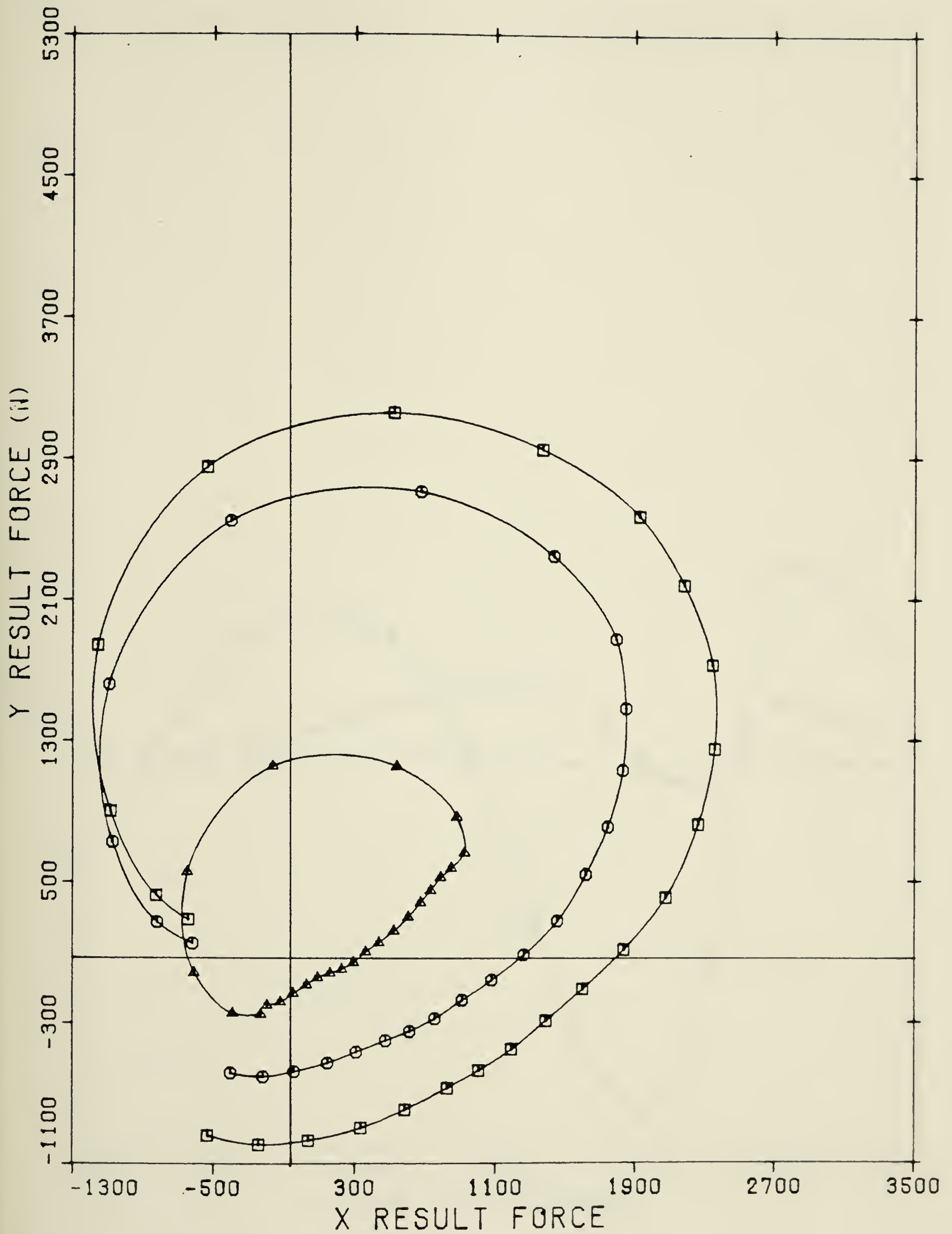


Figure 13. X and Y Linear Accelerations of the Segmental Endpoints for Subject 1.

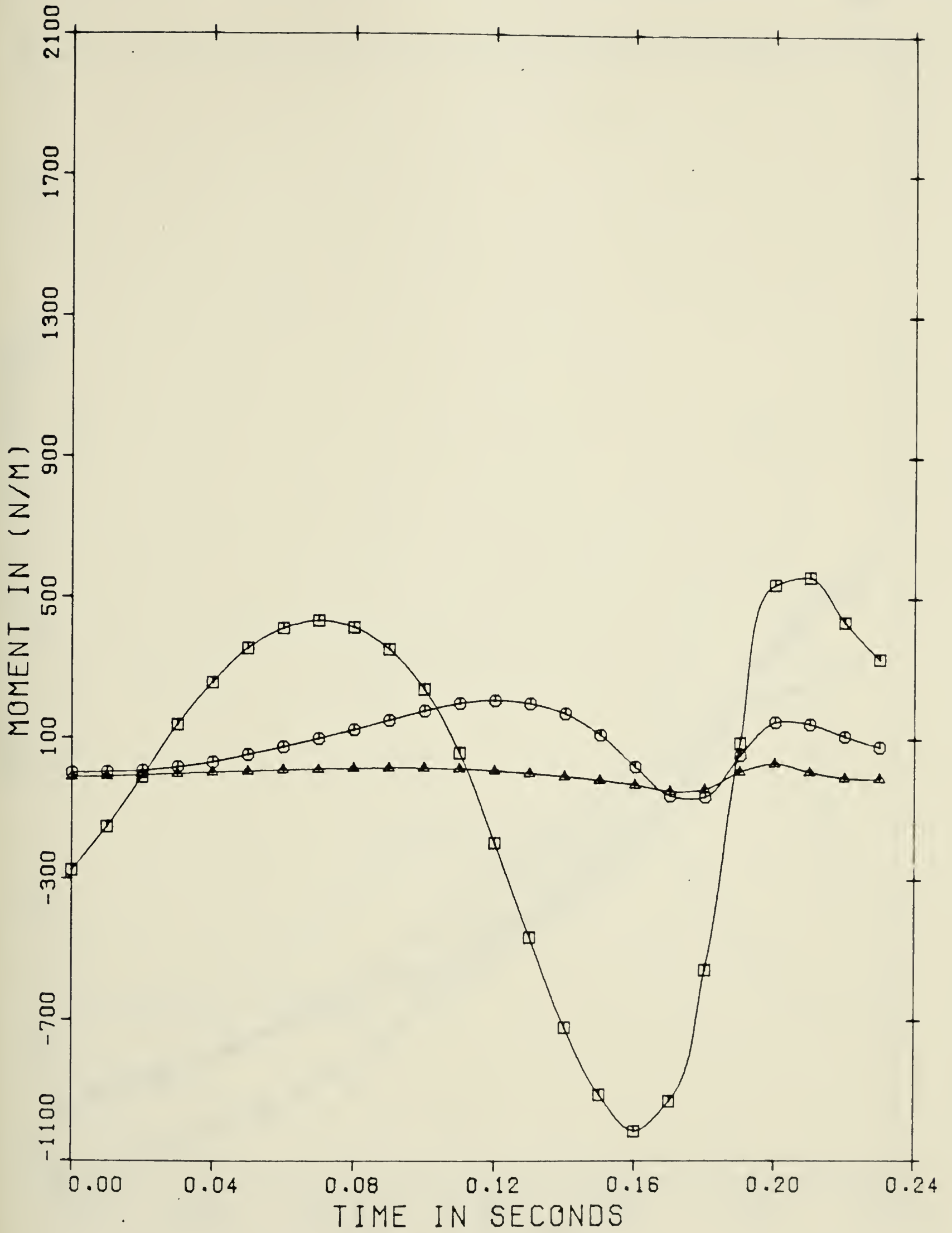




WRIST(△), ELBOW(○), SHOULDER(□)

Figure 14. X and Y Joint Forces for Subject 1.



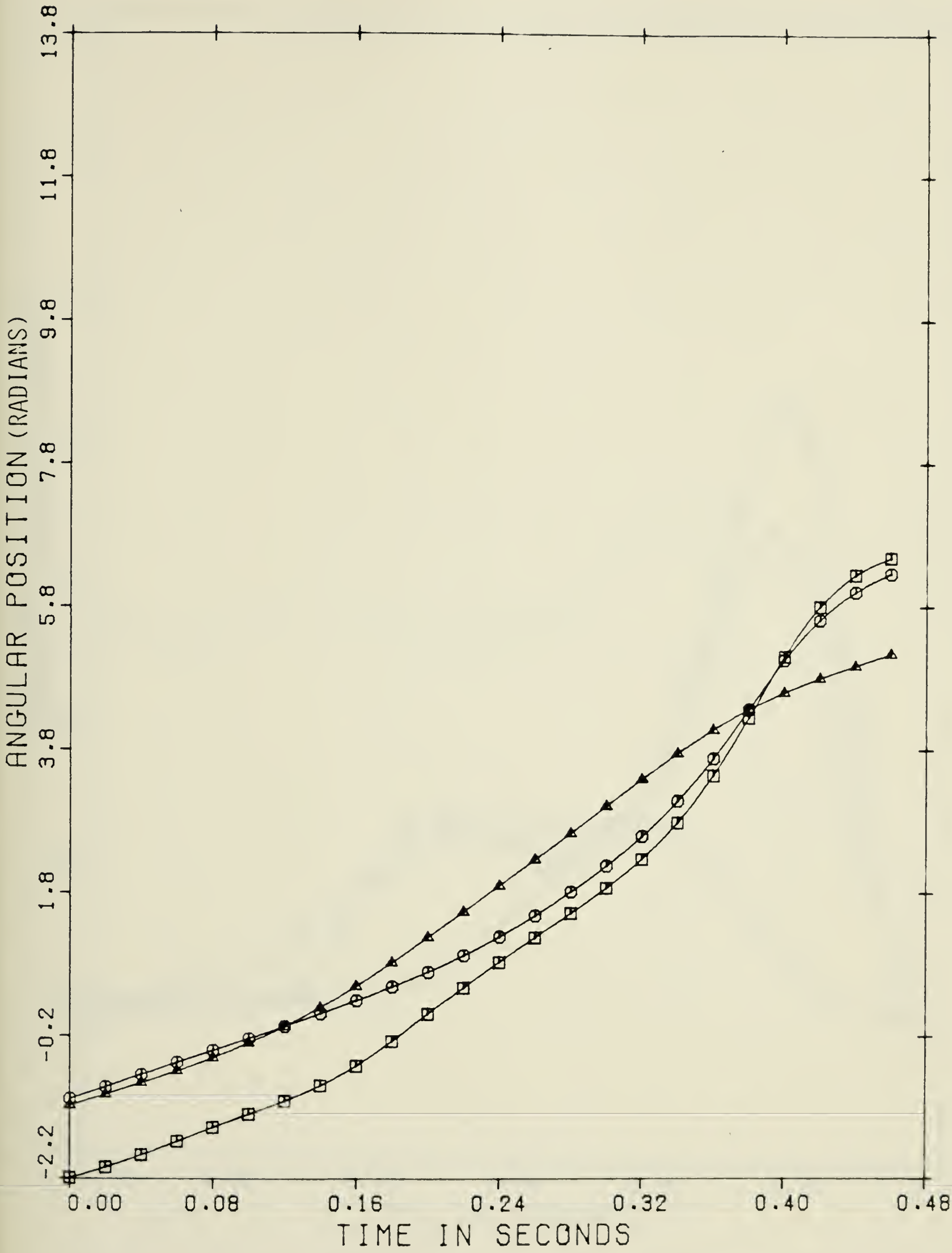


WRIST( $\Delta$ ), ELBOW( $\circ$ ), SHOULDER( $\square$ )

Figure 15. Resultant Moments at the Joints for Subject 1.



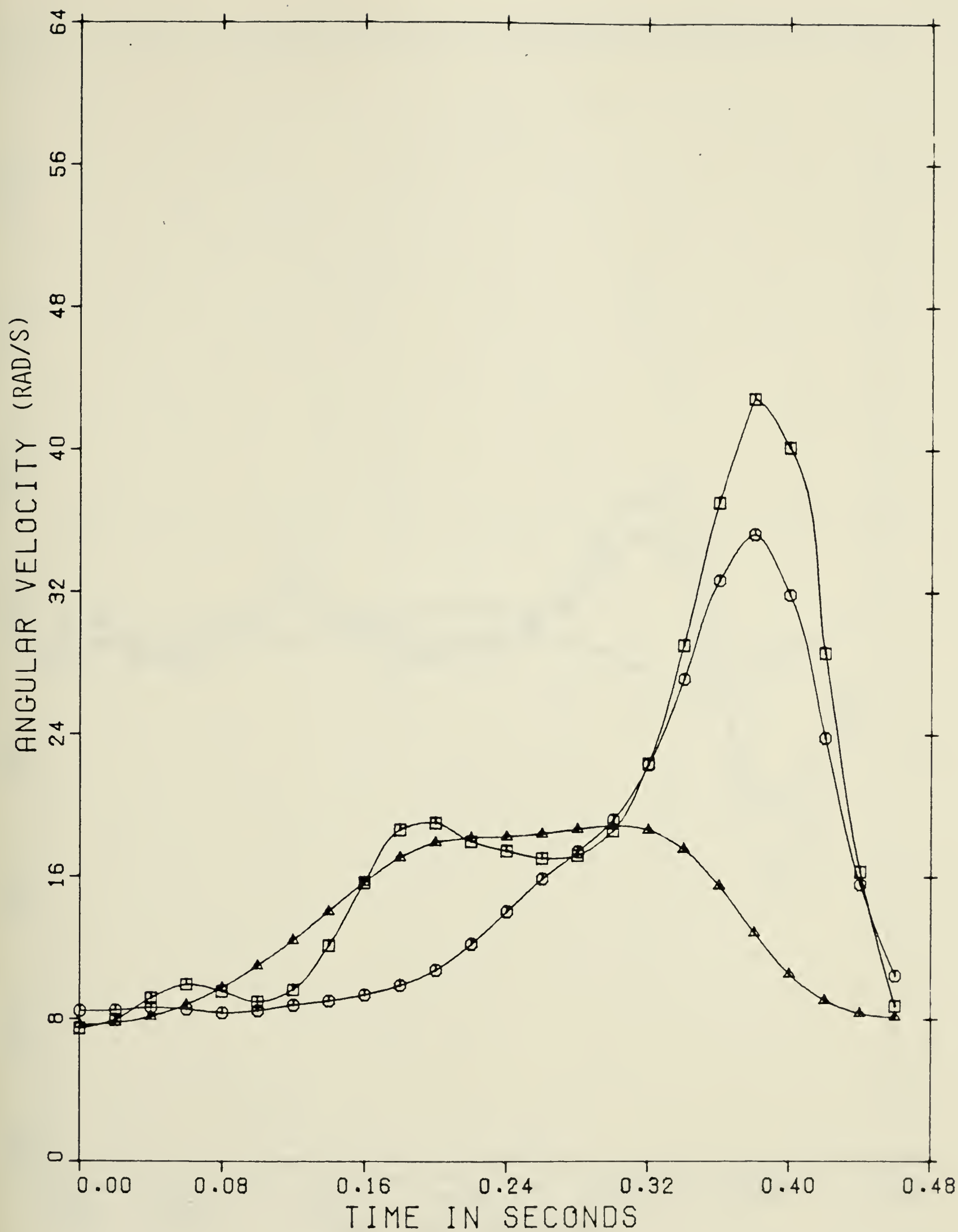




HAND(□), L.ARM(○), U.ARM(△)

Figure 16. Angular Position vs Time of the Arm Segments for Subject 1.





HAND( $\square$ ), L. ARM( $\Delta$ ), U. ARM( $\circ$ )

Figure 17. Angular Velocity vs Time of the Arm Segments for Subject 1.





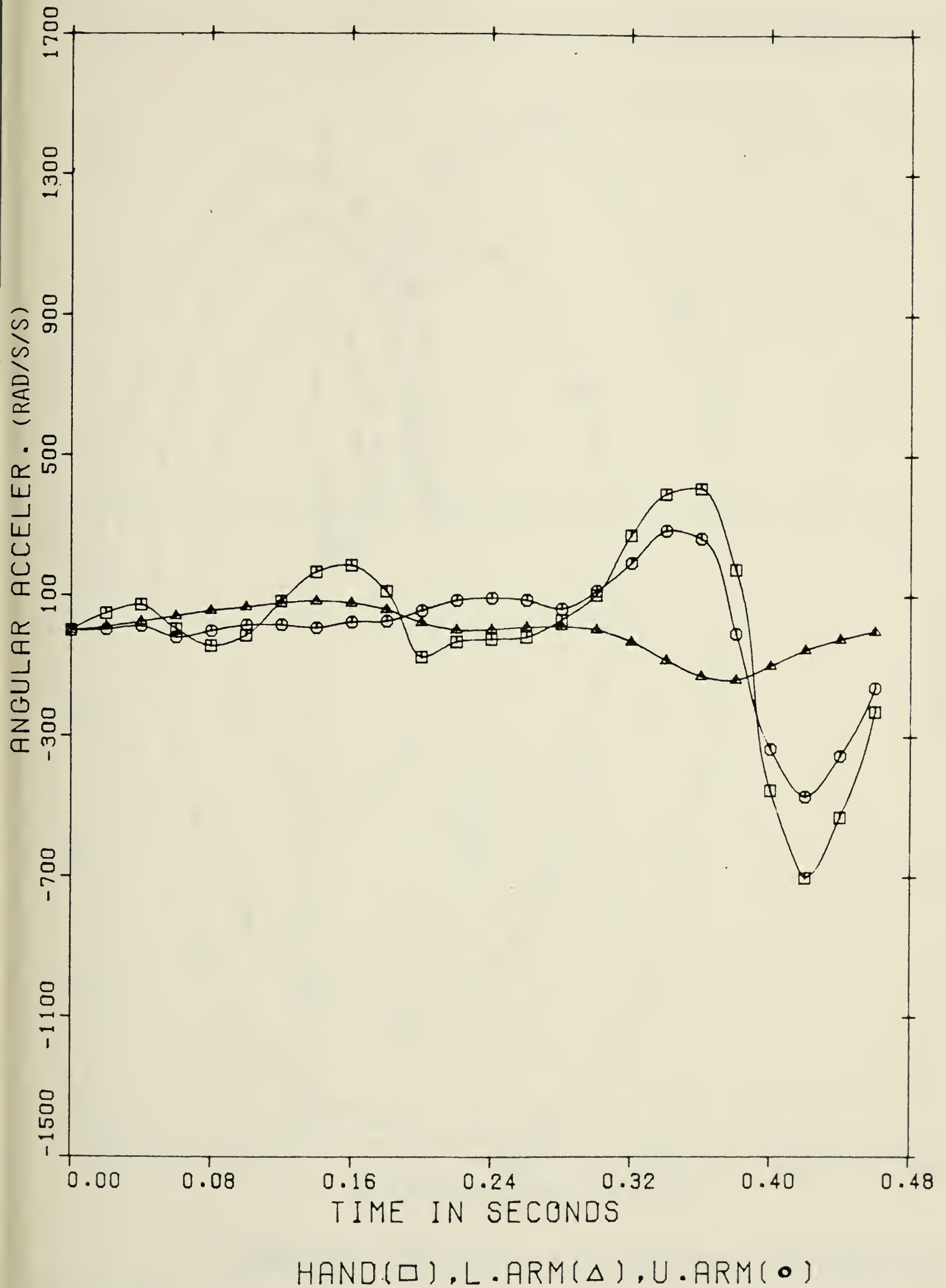


Figure 18. Angular Acceleration vs Time of the Arm Segments for Subject 1.



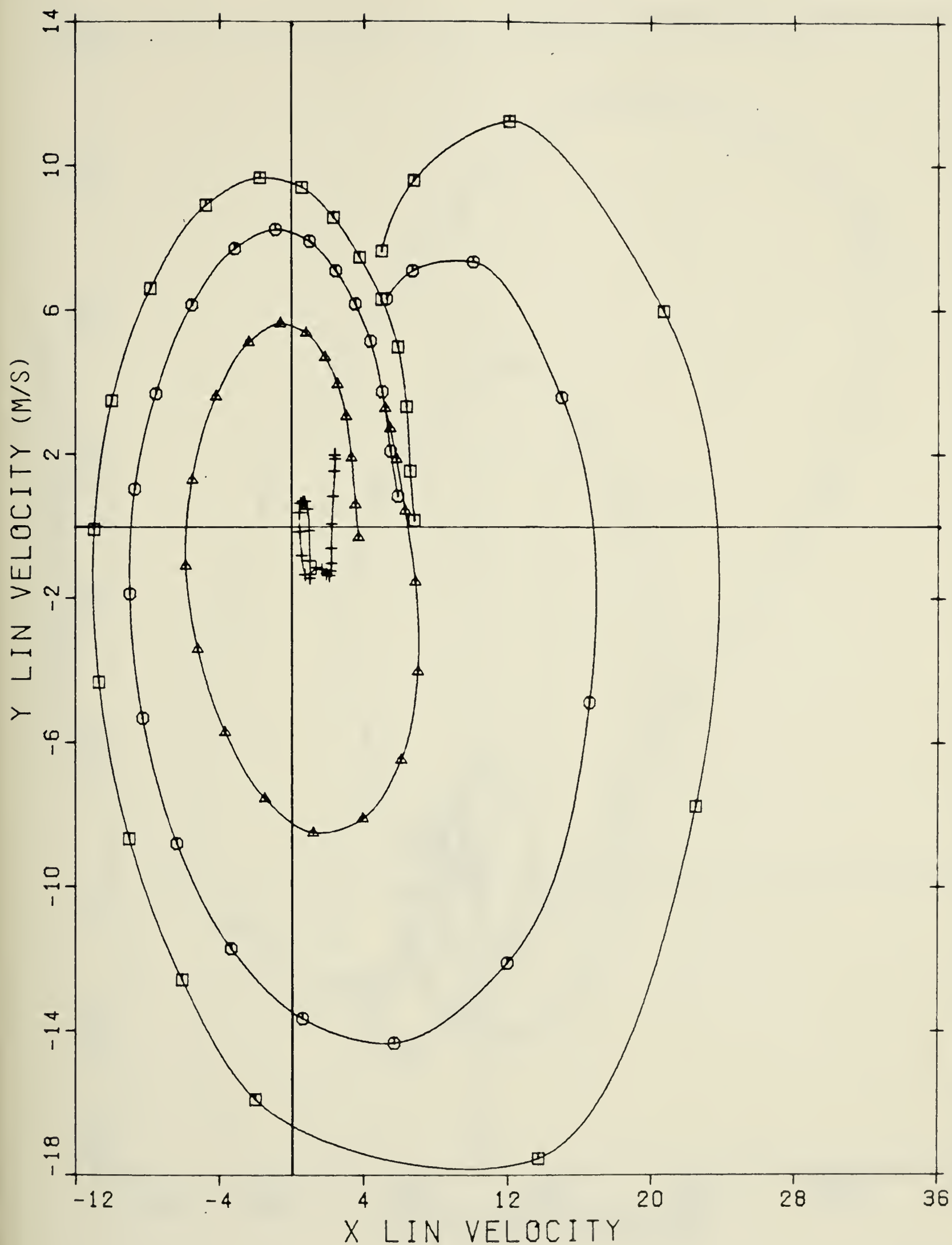
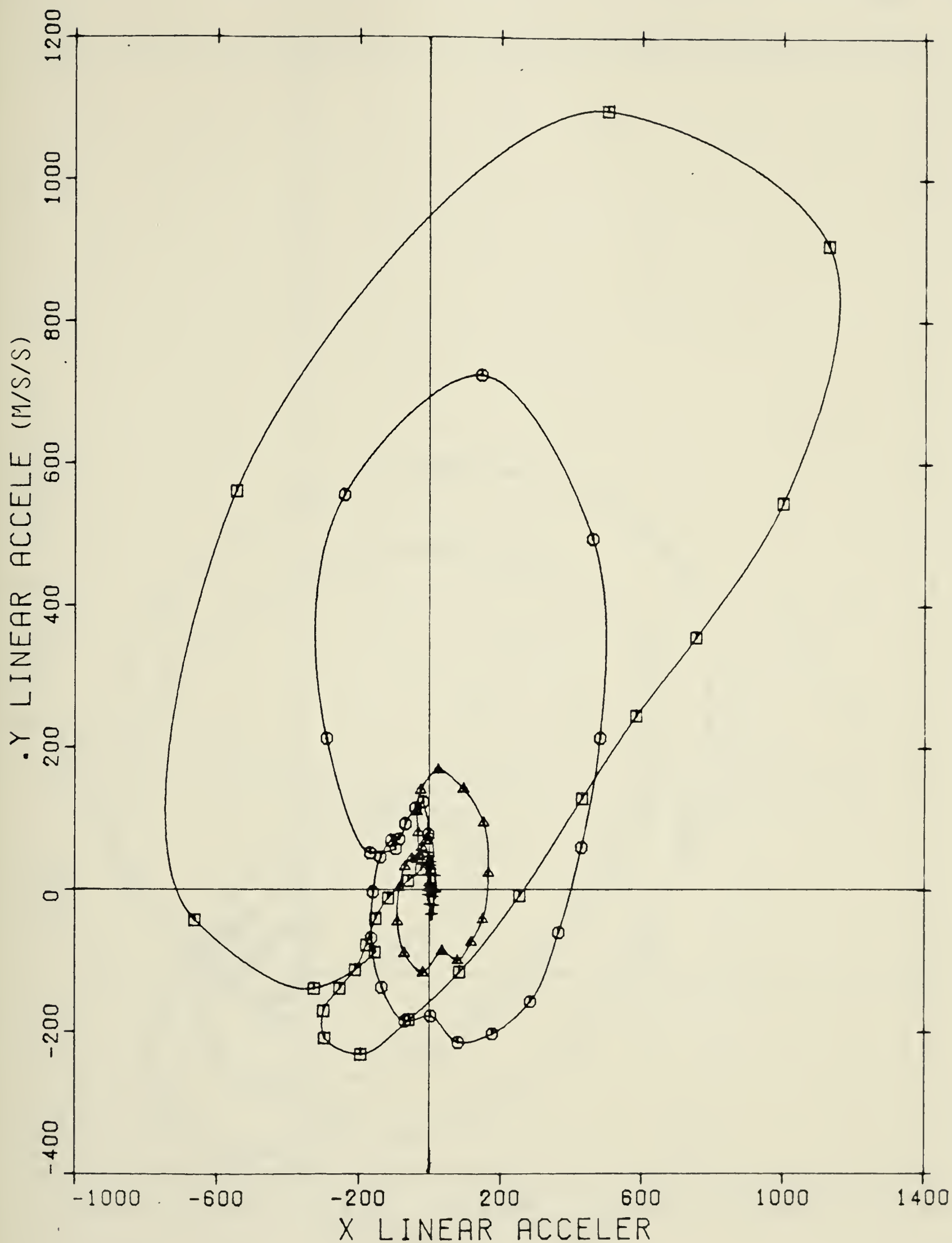


Figure 19. X and Y Linear Velocities of the Segmental Endpoints for Subject 1.



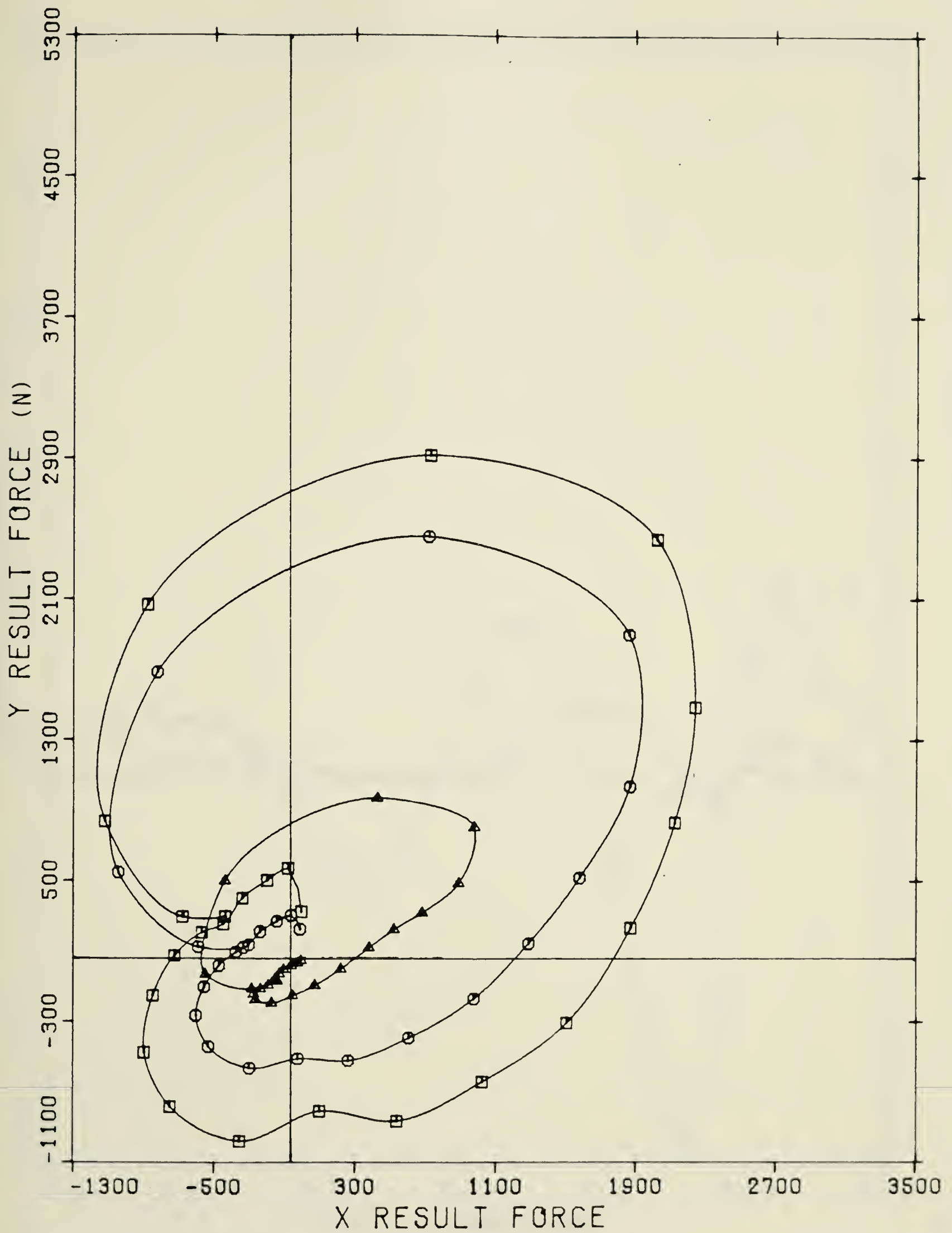


HAND( $\square$ ), WRIST( $\circ$ ), ELBOW( $\Delta$ ), SHLDR(—)

Figure 20. X and Y Linear Accelerations of the Segmental Endpoints for Subject 1.



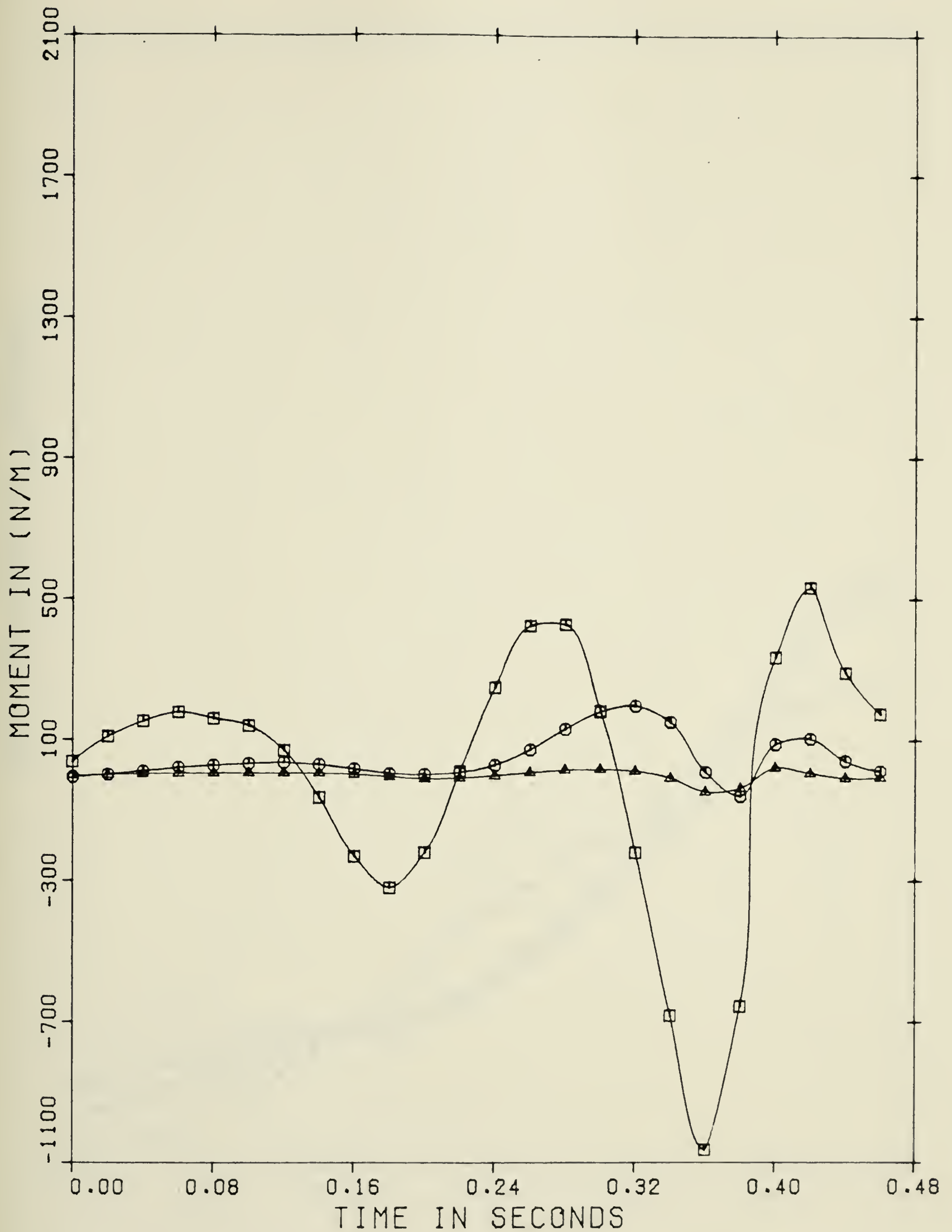




WRIST(Δ), ELBOW(○), SHOULDER(□)

Figure 21. X and Y Joint Forces for Subject 1.



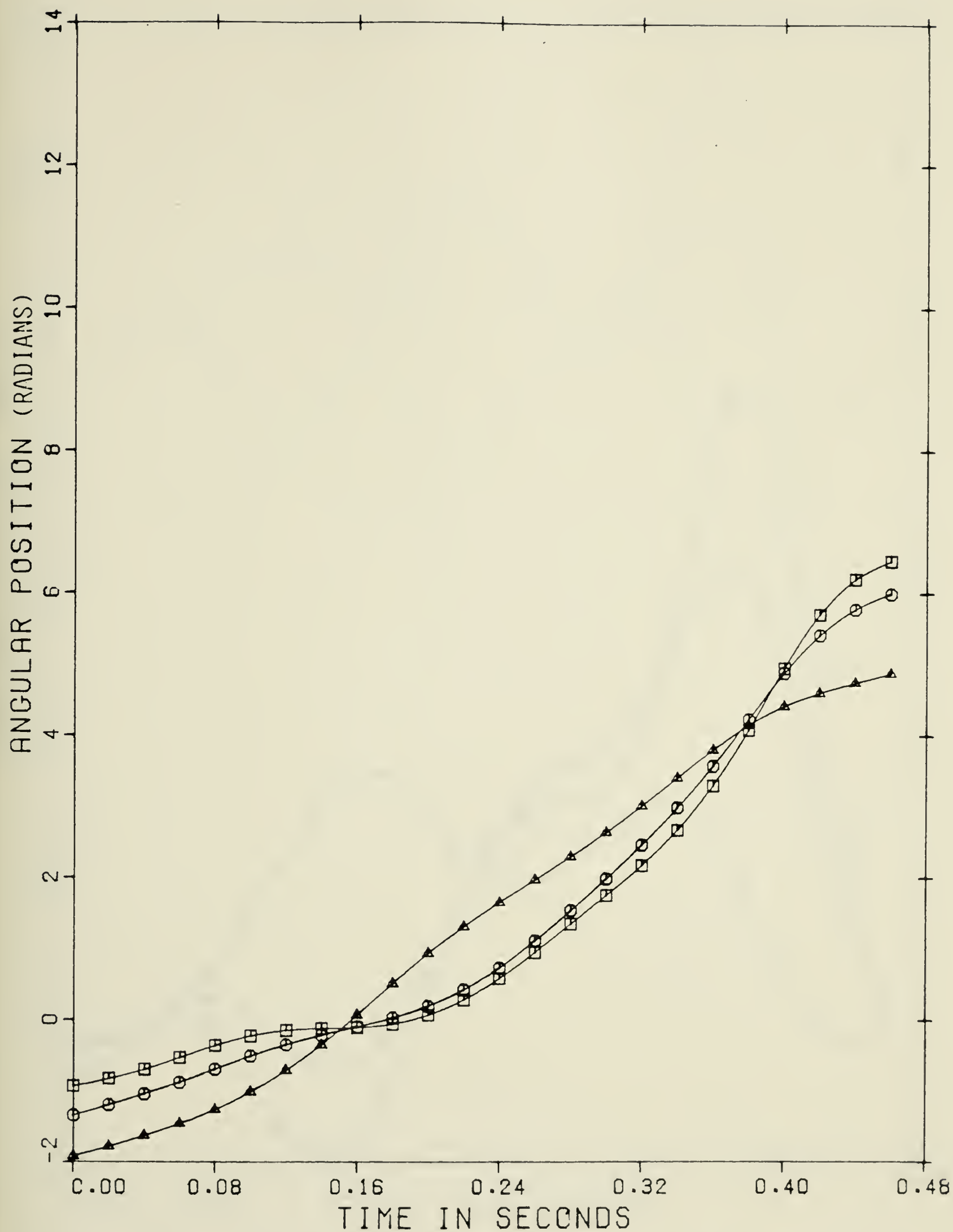


WRIST( $\Delta$ ), ELBOW( $\circ$ ), SHOULDER( $\square$ )

Figure 22. Resultant Moments at the Joints for Subject 1.



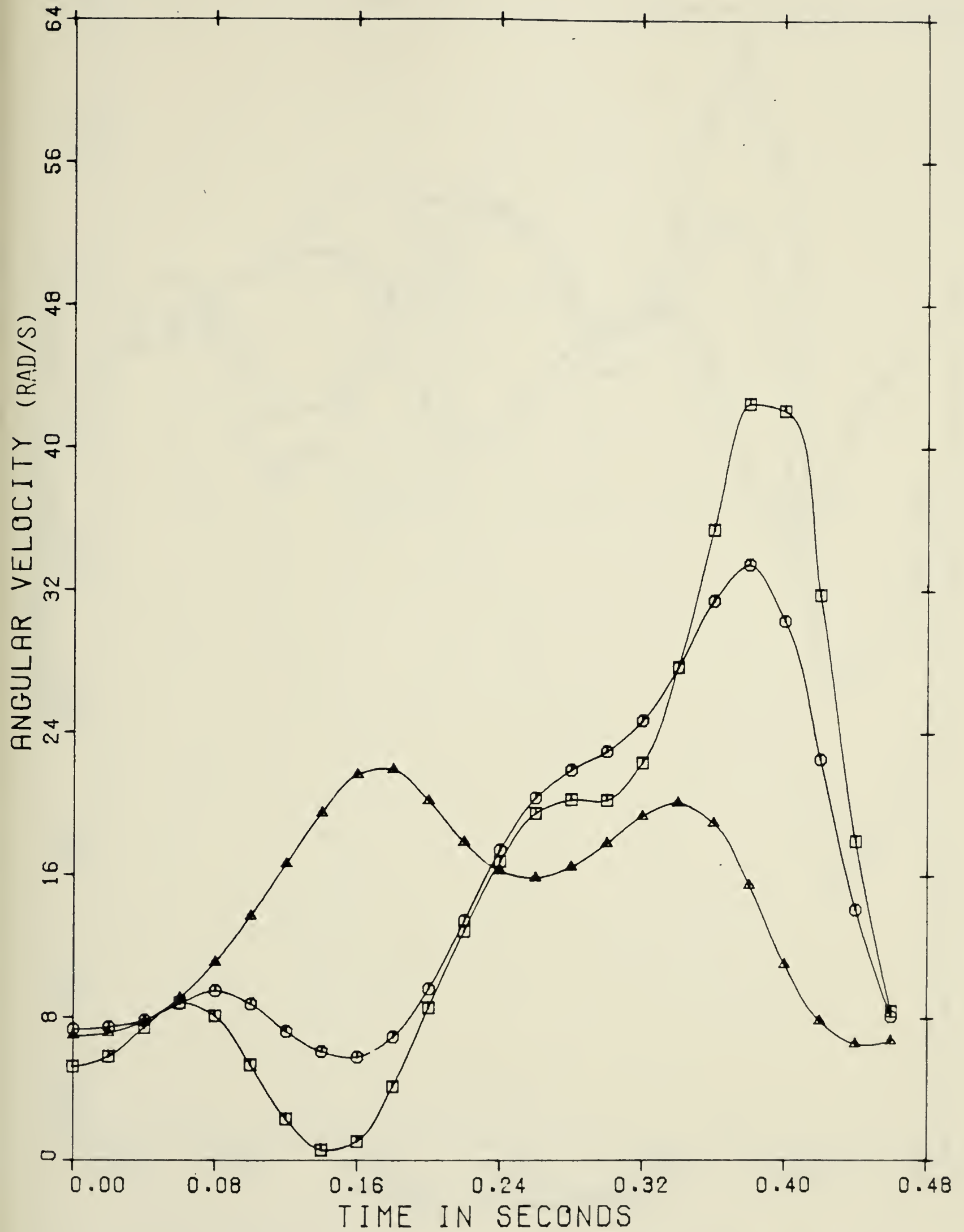




HAND( $\square$ ), L.ARM( $\circ$ ), U.ARM( $\triangle$ )

Figure 23. Angular Position vs Time of the Arm Segments for Subject 2.





HAND( $\square$ ), L.ARM( $\circ$ ), U.ARM( $\Delta$ )

Figure 24. Angular Velocity vs Time of the Arm Segments for Subject 2.



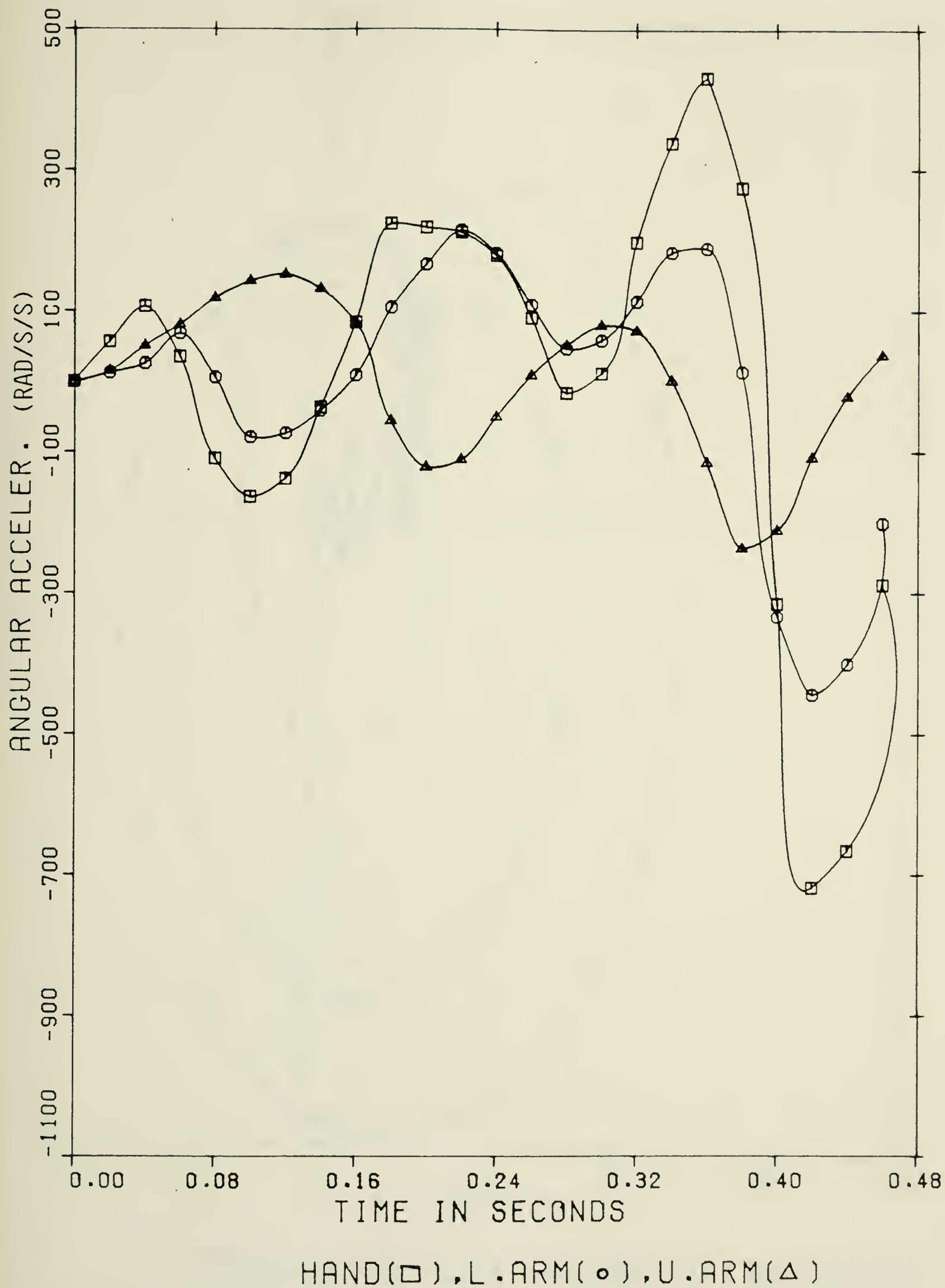


Figure 25. Angular Acceleration vs Time of the Arm Segments for Subject 2.





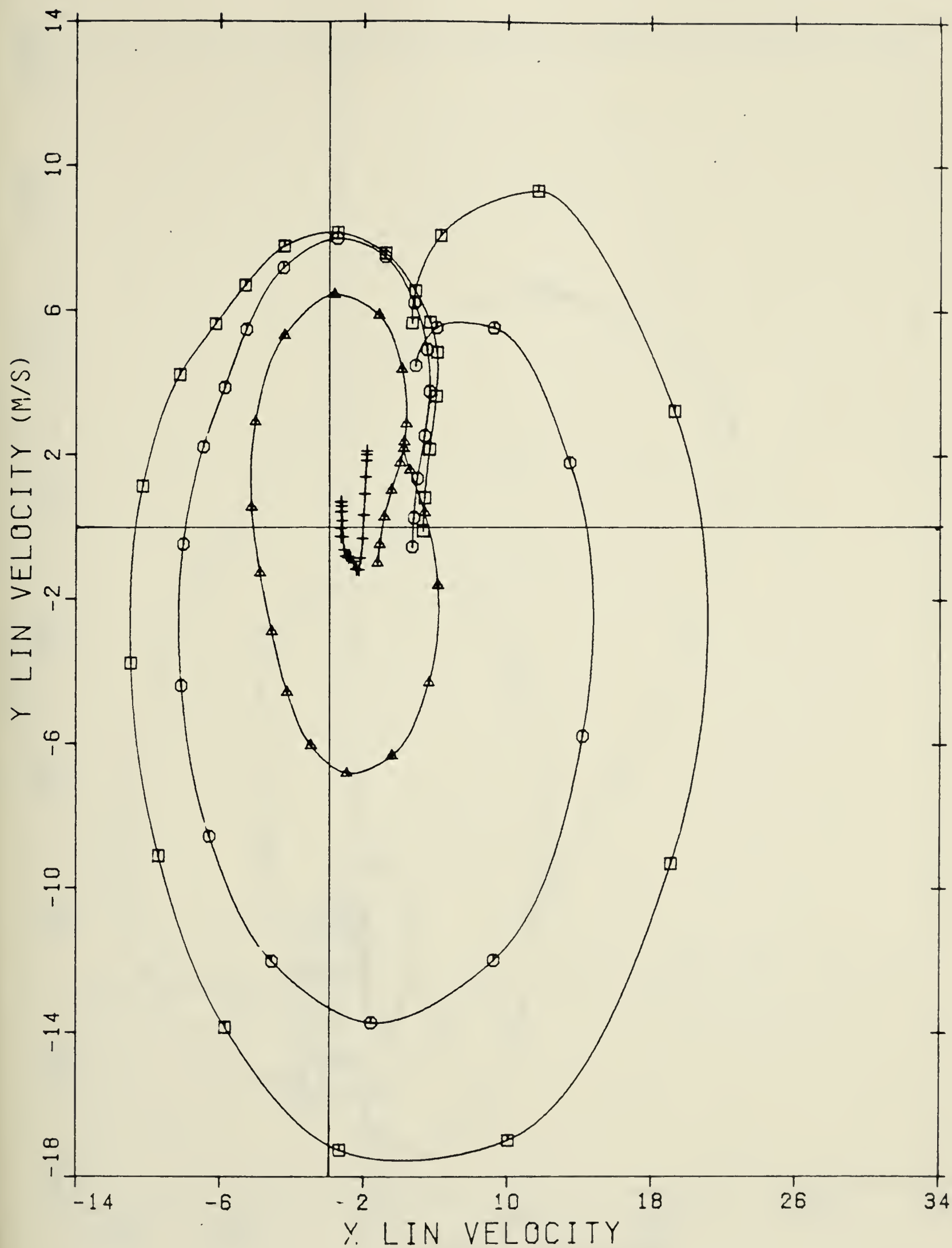


Figure 26. X and Y Linear Velocities of the Segmental Endpoints for Subject 2.



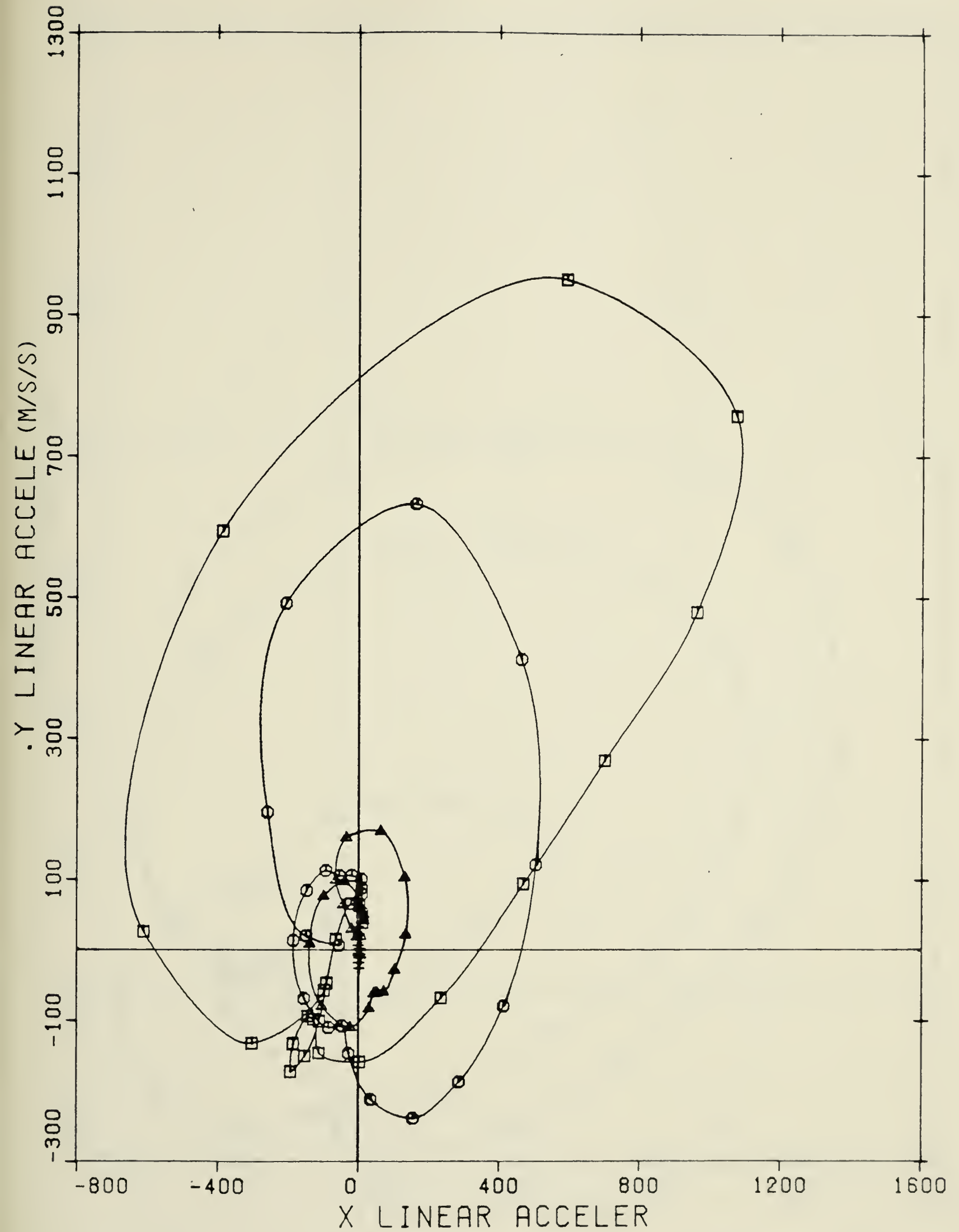
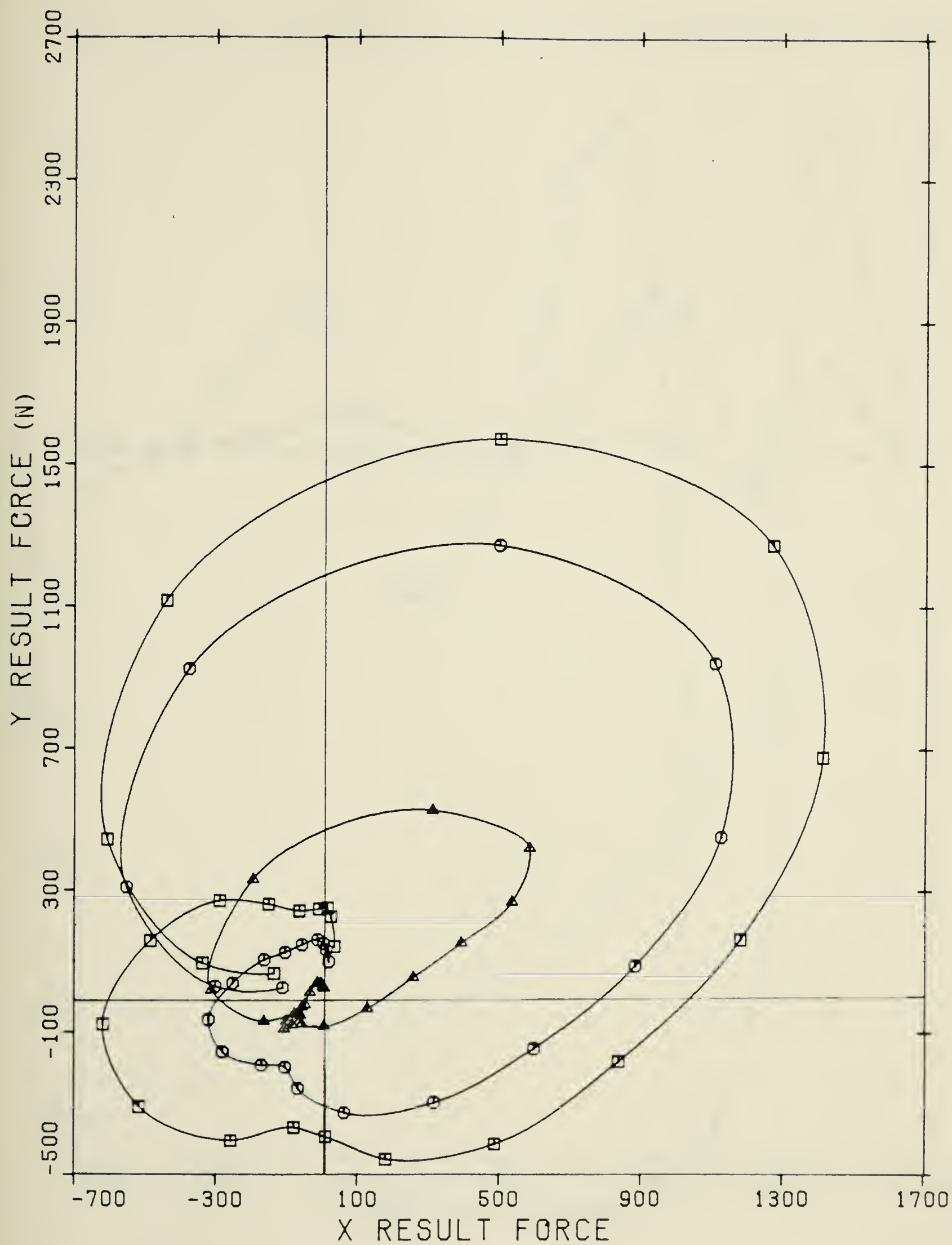


Figure 27. X and Y Linear Accelerations of the Segmental Endpoints for Subject 2.



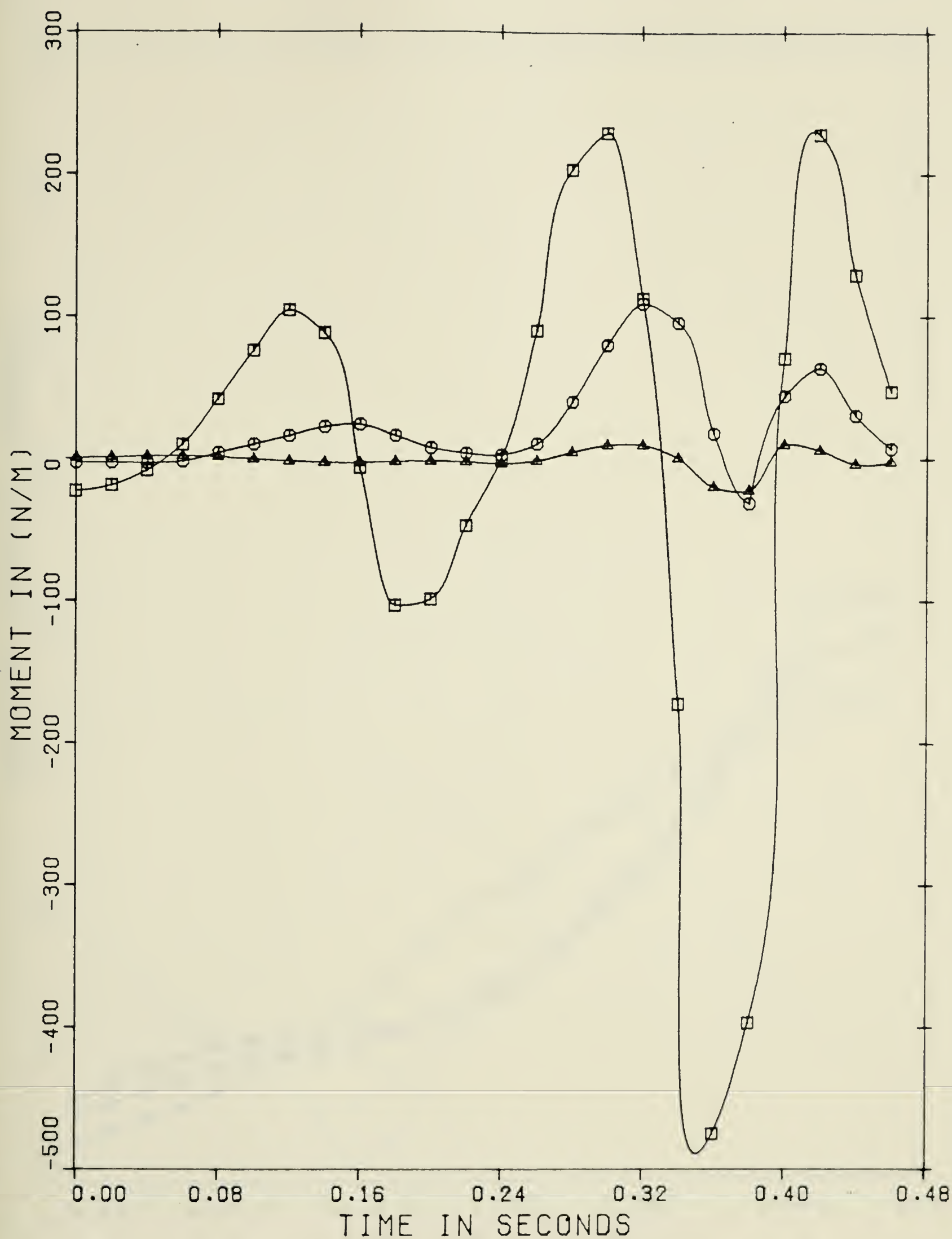


WRIST(△), ELBOW(○), SHOULDER(□)

Figure 28. X and Y Joint Forces for Subject 2.







WRIST( $\Delta$ ), ELBOW( $\circ$ ), SHOULDER( $\square$ )

Figure 29. Resultant Moments at the Joints for Subject 2.



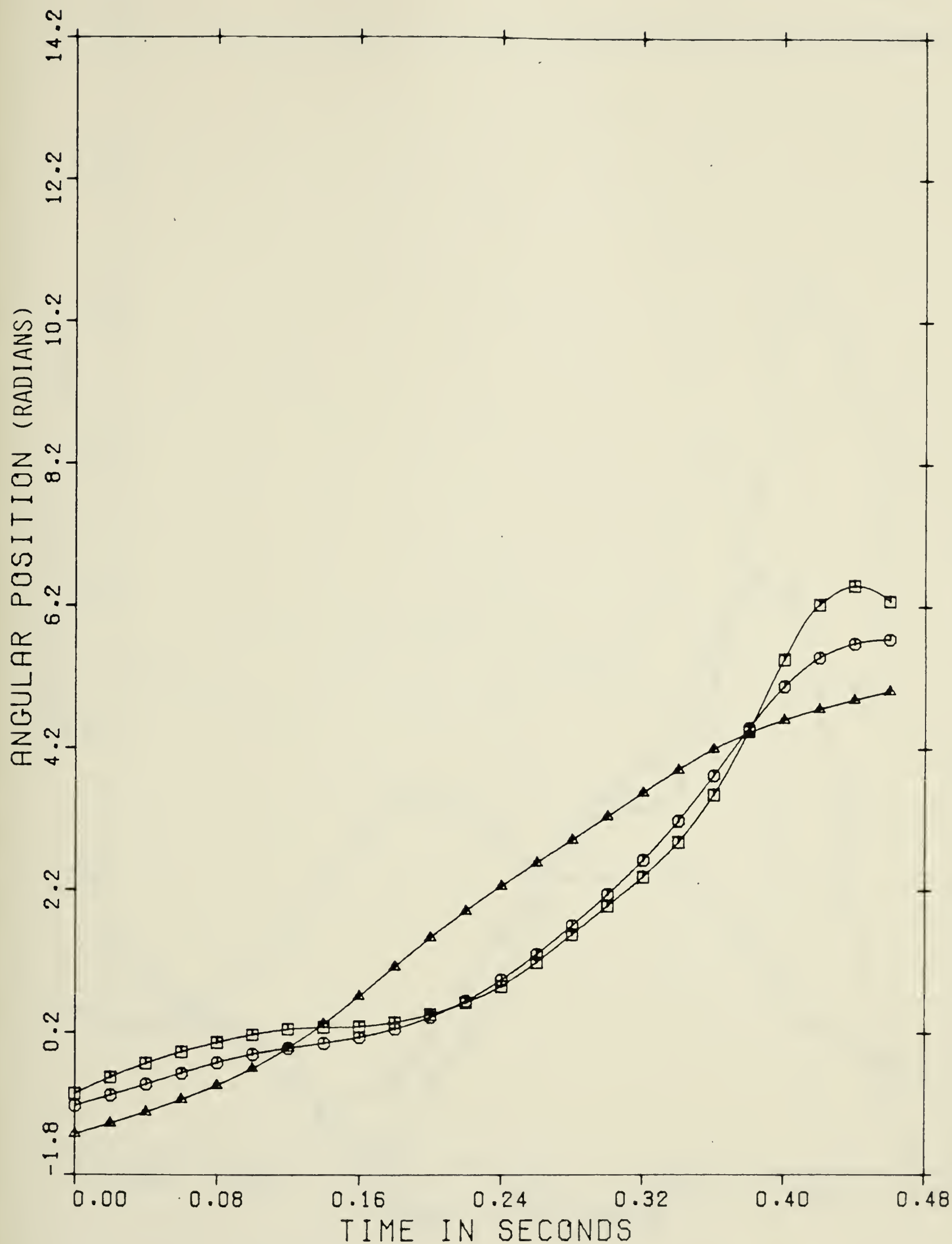


Figure 30. Angular Position vs Time of the Arm Segments for Subject 3.



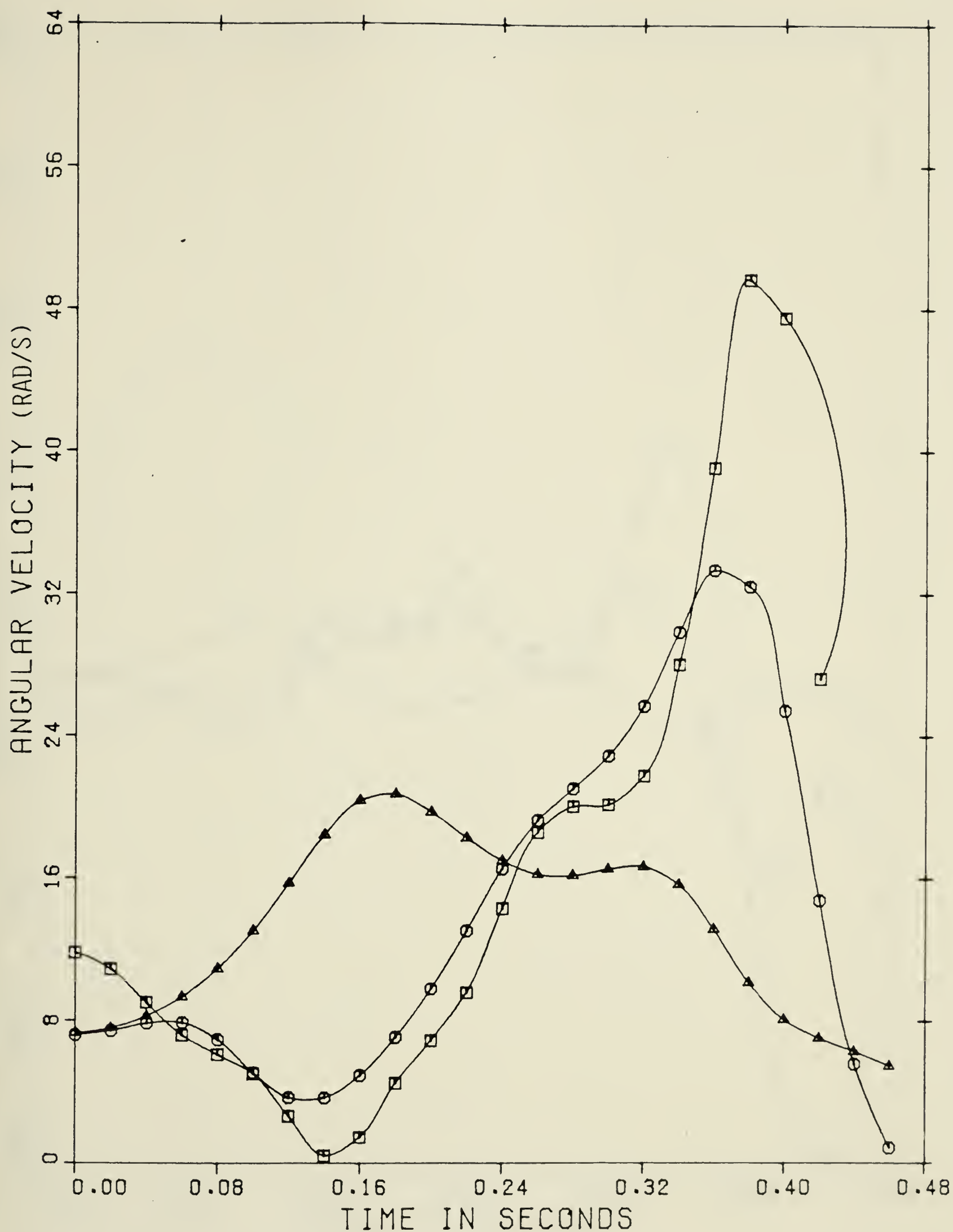


Figure 31. Angular Velocity vs Time of the Arm Segments for Subject 3.





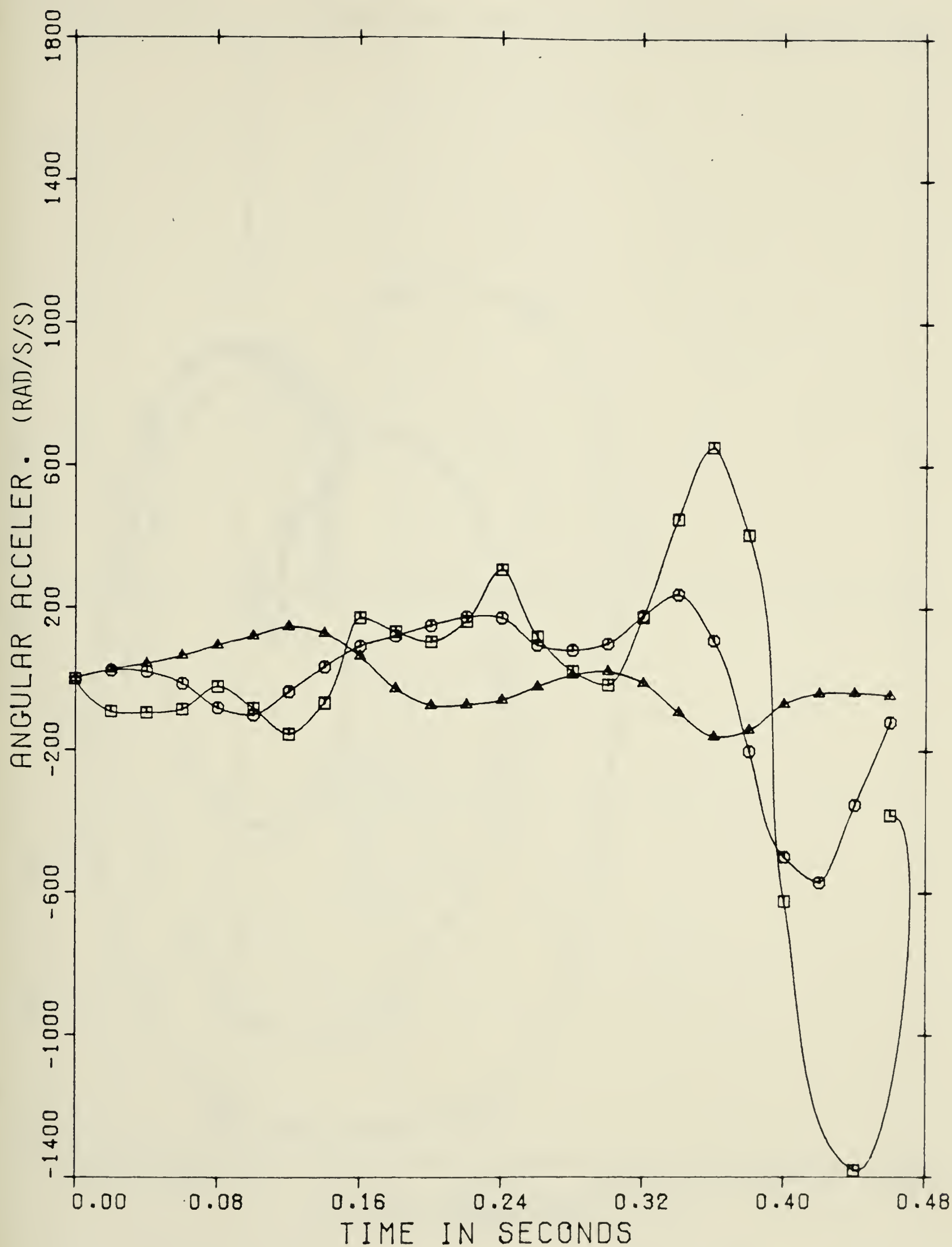


Figure 32. Angular Acceleration vs Time of the Arm Segments for Subject 3.



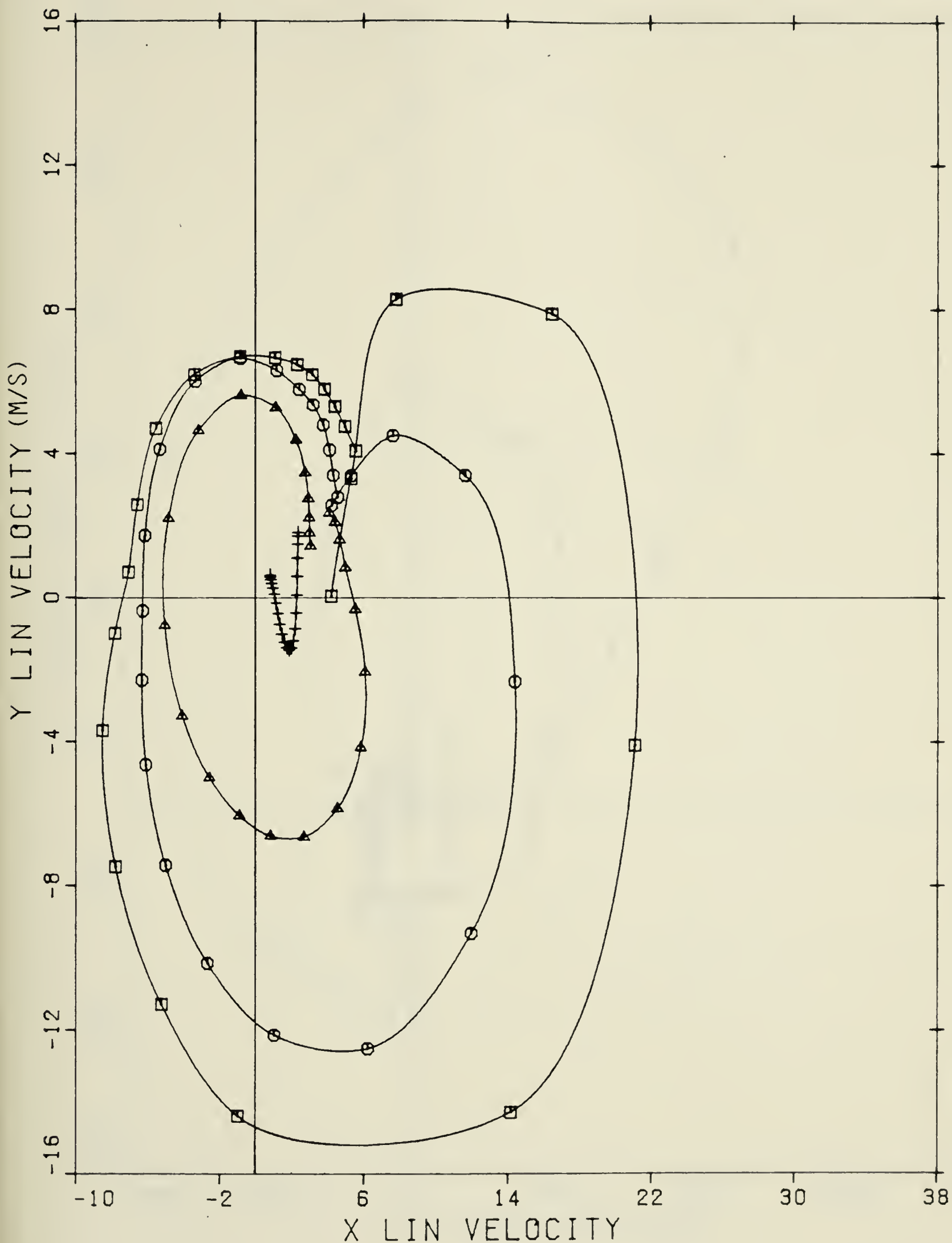
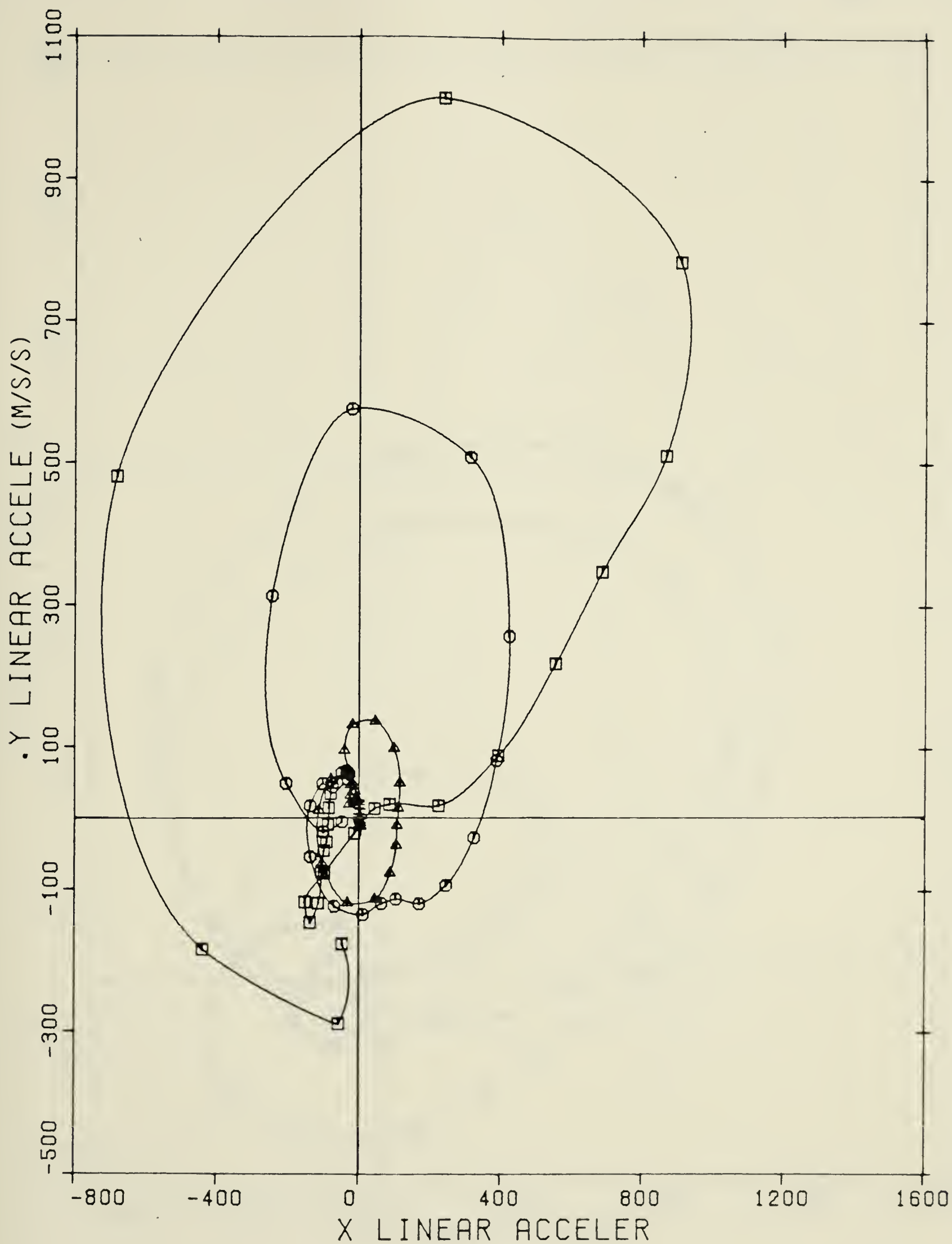


Figure 33. X and Y Linear Velocities of the Segmental Endpoints for Subject 3.



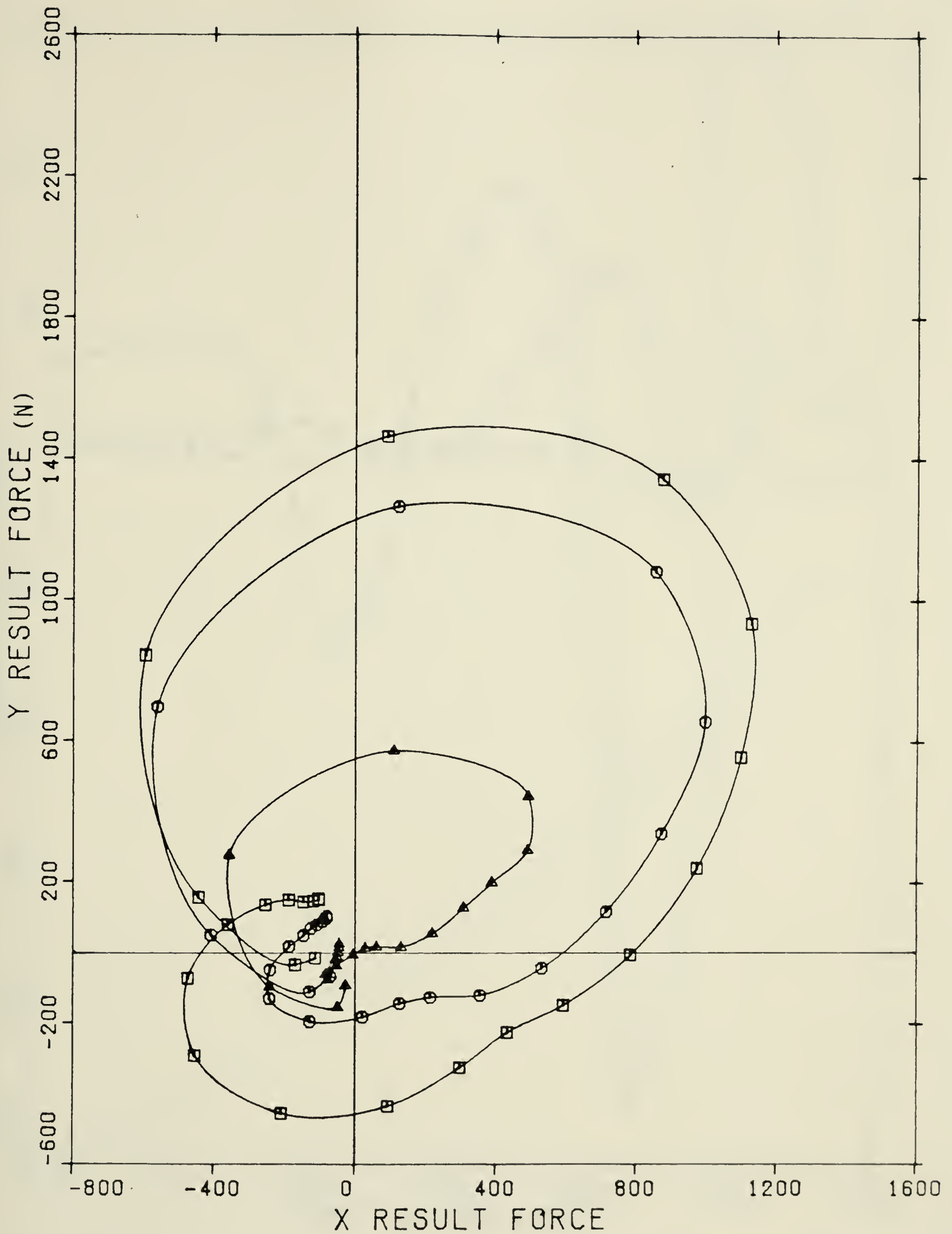


HAND(□), WRIST(○), ELBOW(Δ), SHLDR(—)

Figure 34. X and Y Linear Accelerations of the Segmental Endpoints for Subject 3.







WRIST(Δ), ELBOW(◦), SHOULDER(◻)

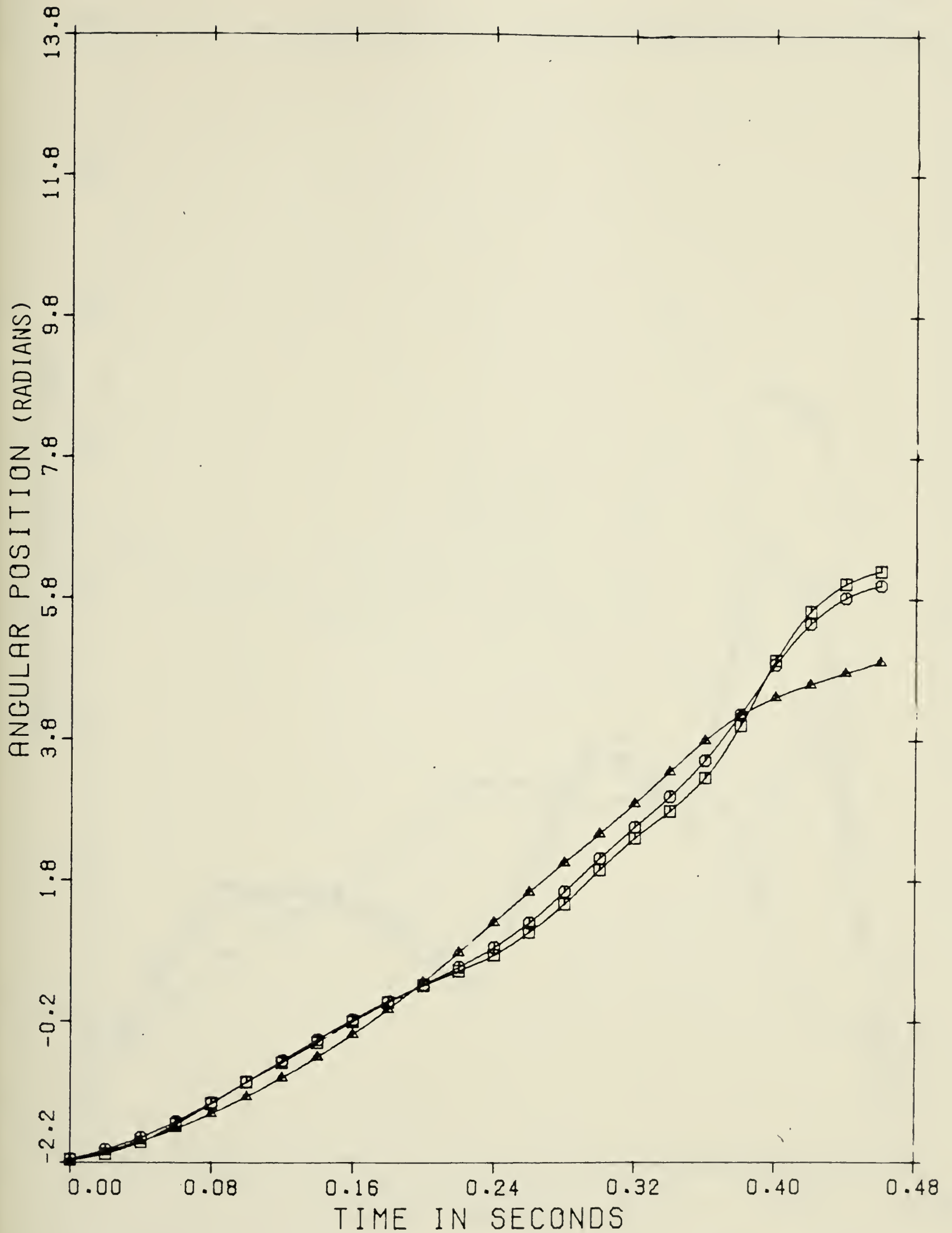
Figure 35. X and Y Joint Forces for Subject 3.





Figure 36. Resultant Moments at the Joints for Subject 3.





HAND( $\square$ ), L.ARM( $\circ$ ), U.ARM( $\Delta$ )

Figure 37. Angular Position vs Time of the Arm Segments for Subject 4.







HAND( $\square$ ), L.ARM( $\circ$ ), U.ARM( $\triangle$ )

Figure 38. Angular Velocity vs Time of the Arm Segments for Subject 4.



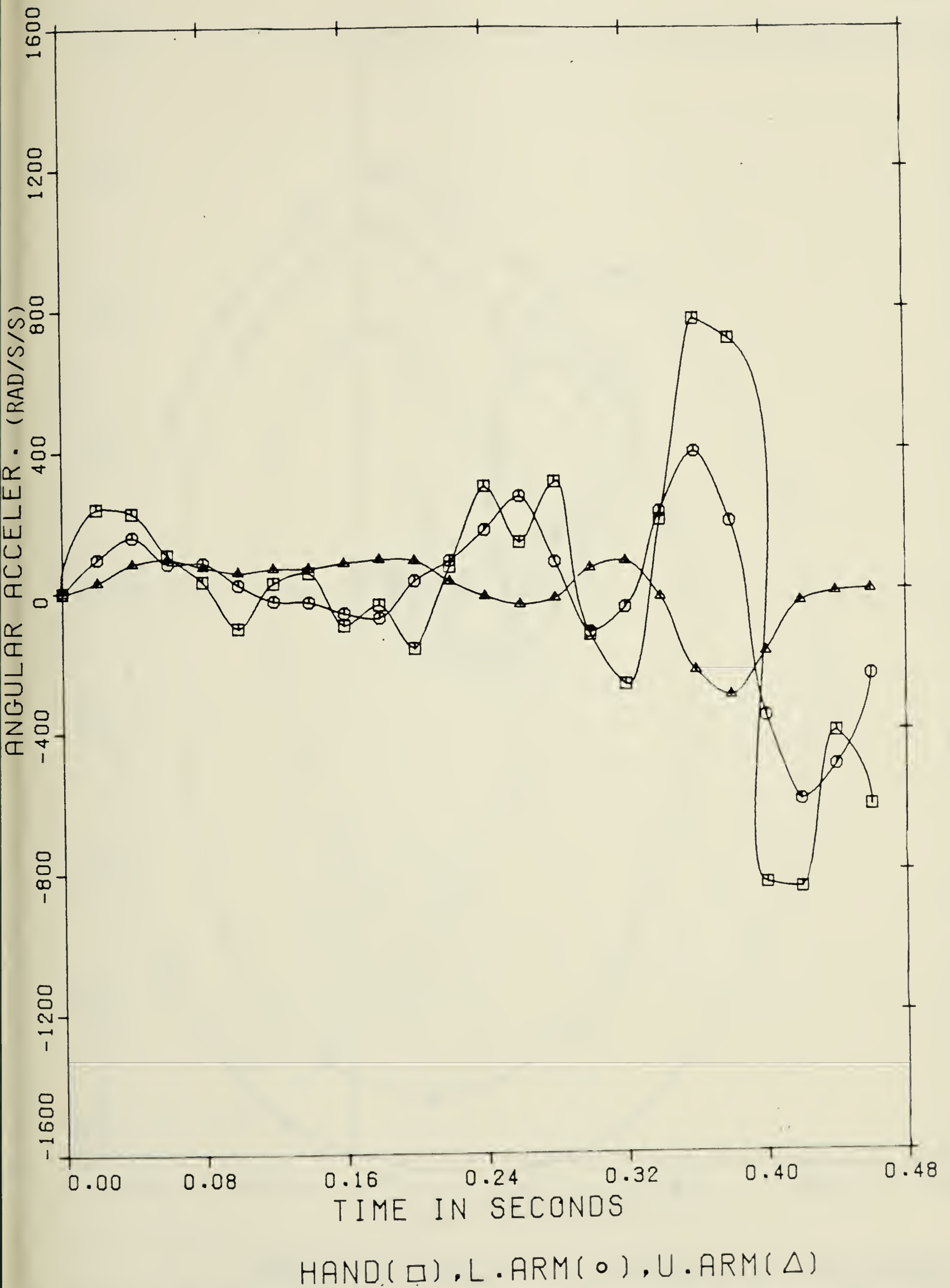
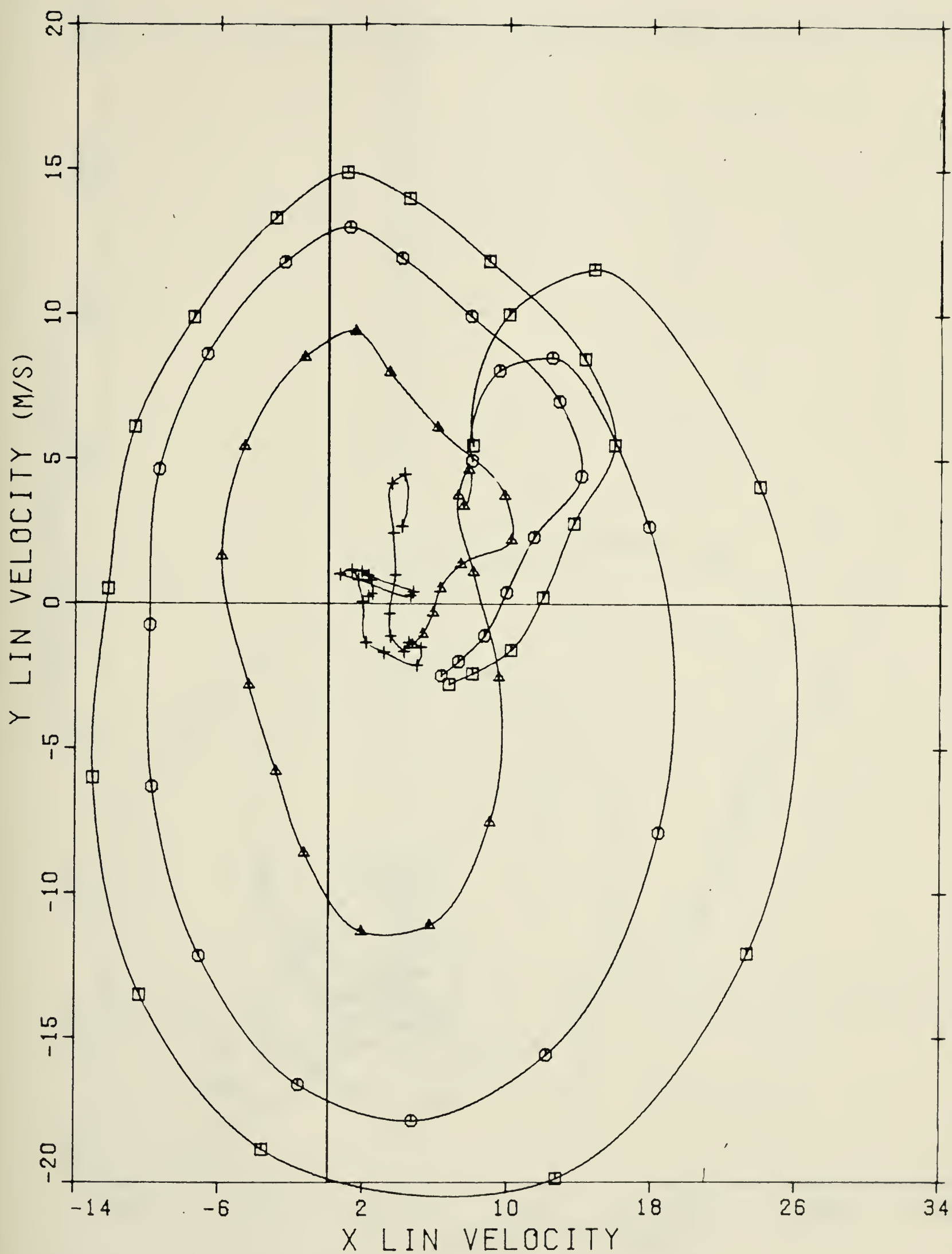


Figure 39. Angular Acceleration vs Time of the Arm Segments for Subject 4.



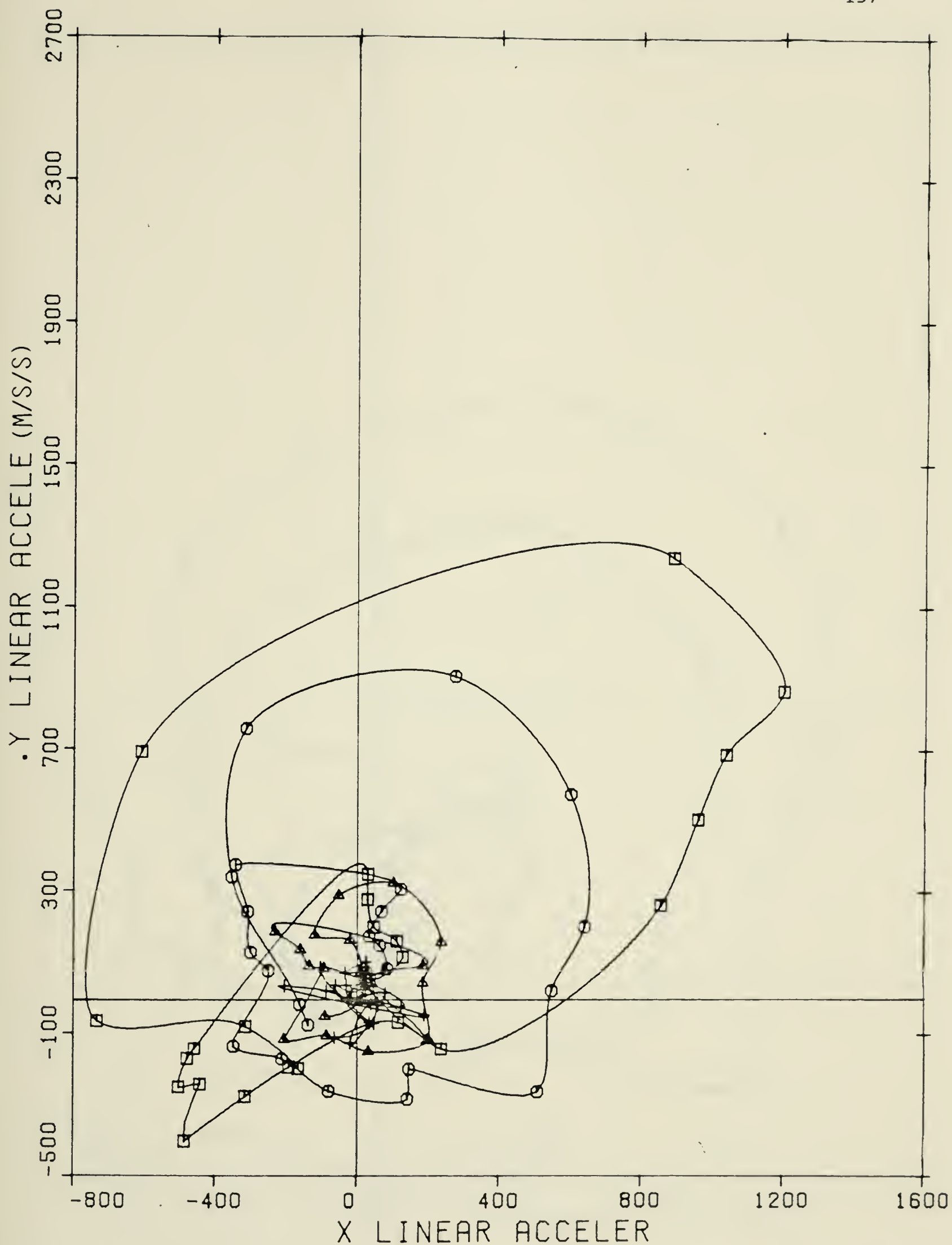


HAND( $\square$ ), WRIST( $\circ$ ), ELBOW( $\Delta$ ), SHLDR( $+$ )

Figure 40. X and Y Linear Velocities of the Segmental Endpoints for Subject 4.







HAND( $\square$ ), WRIST( $\circ$ ), ELBOW( $\Delta$ ), SHLDR( $+$ )

Figure 41. X and Y Linear Accelerations of the Segmental Endpoints for Subject 4.



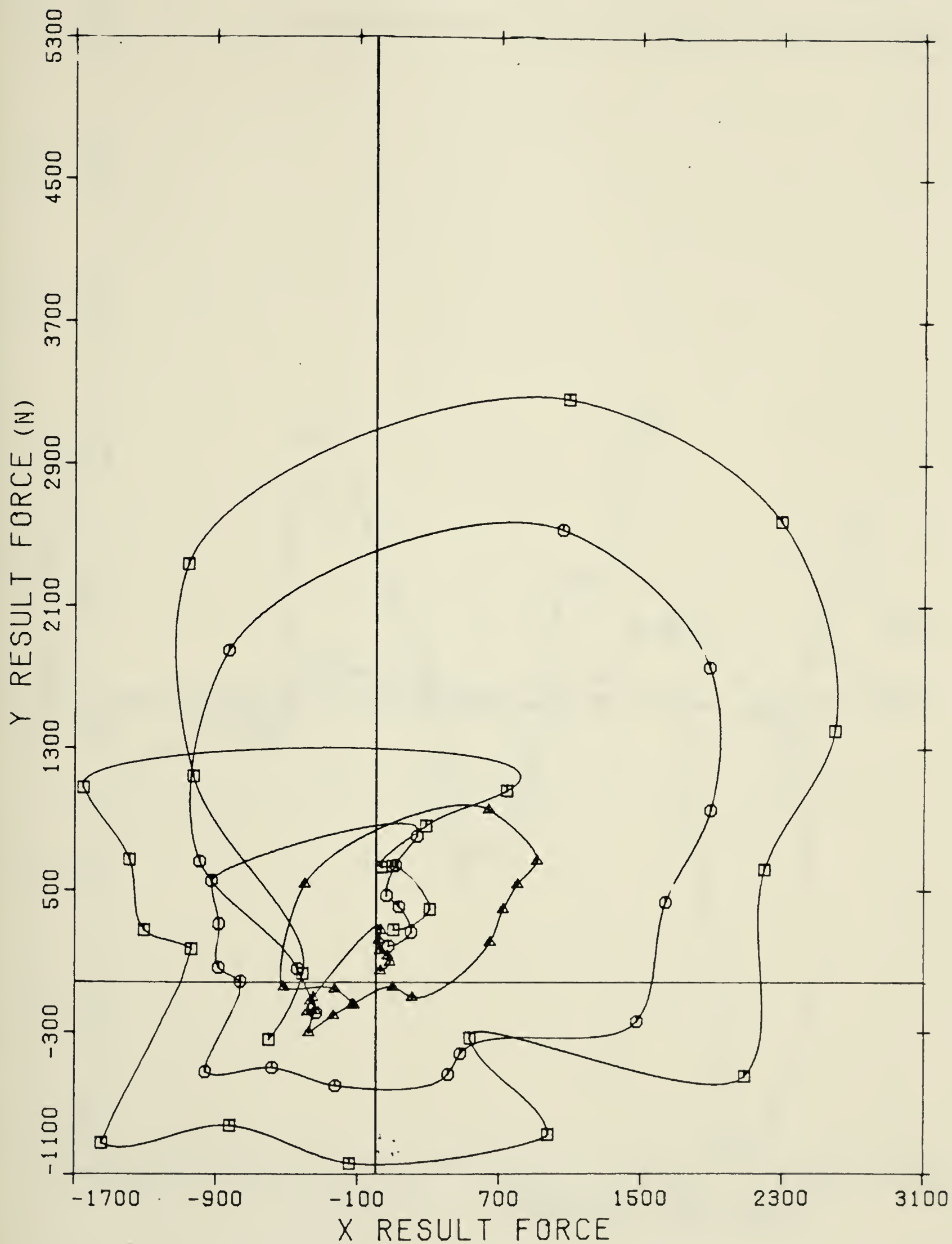
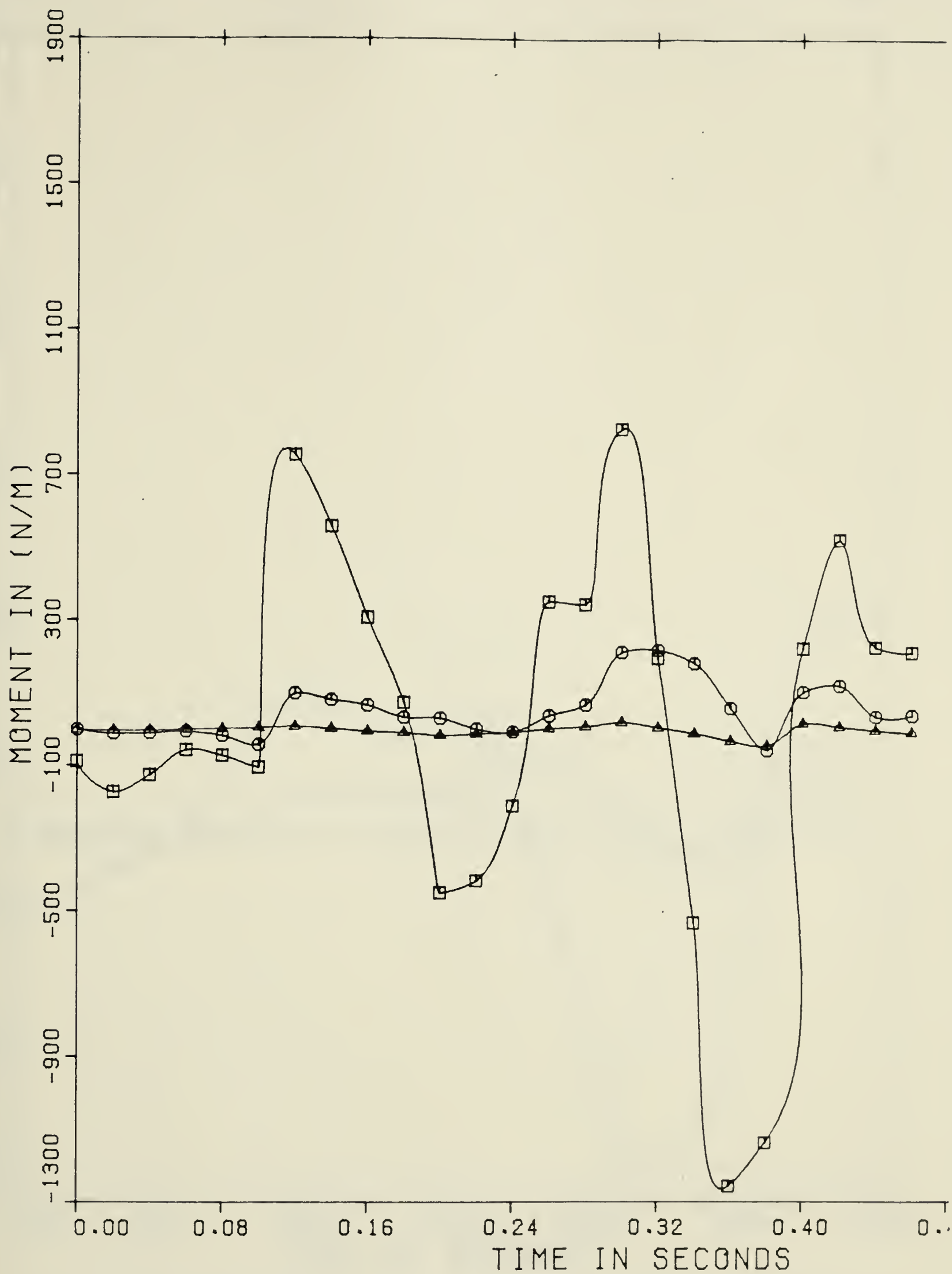


Figure 42. X and Y Joint Forces for Subject 4.



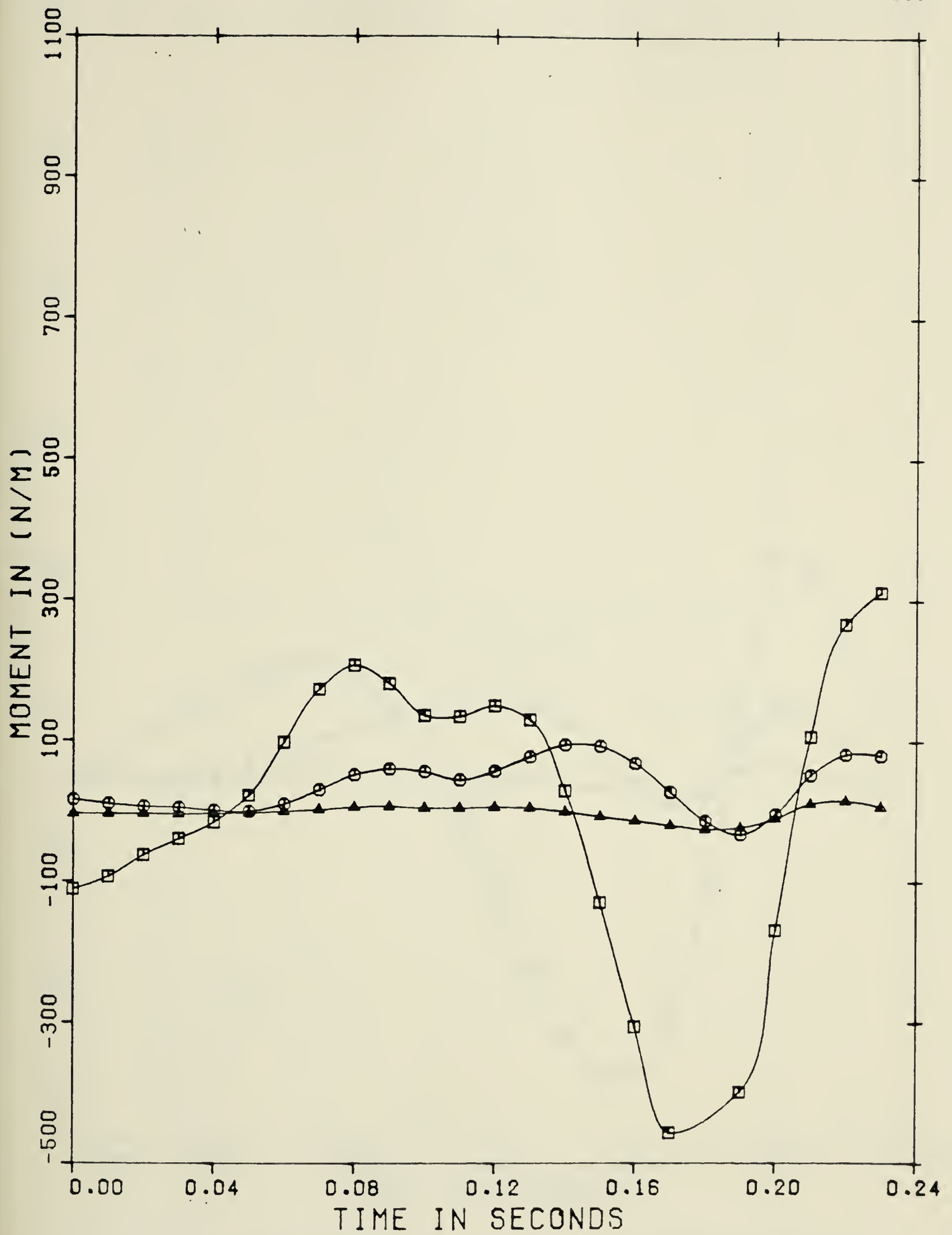


WRIST( $\Delta$ ), ELBOW( $\circ$ ), SHOULDER( $\square$ )

Figure 43. Resultant Moments at the Joints for Subject 4.







WRIST( $\Delta$ ), ELBOW( $\circ$ ), SHOULDER( $\square$ )

Figure 44. Resultant Moments at the Joints for Subject 2.



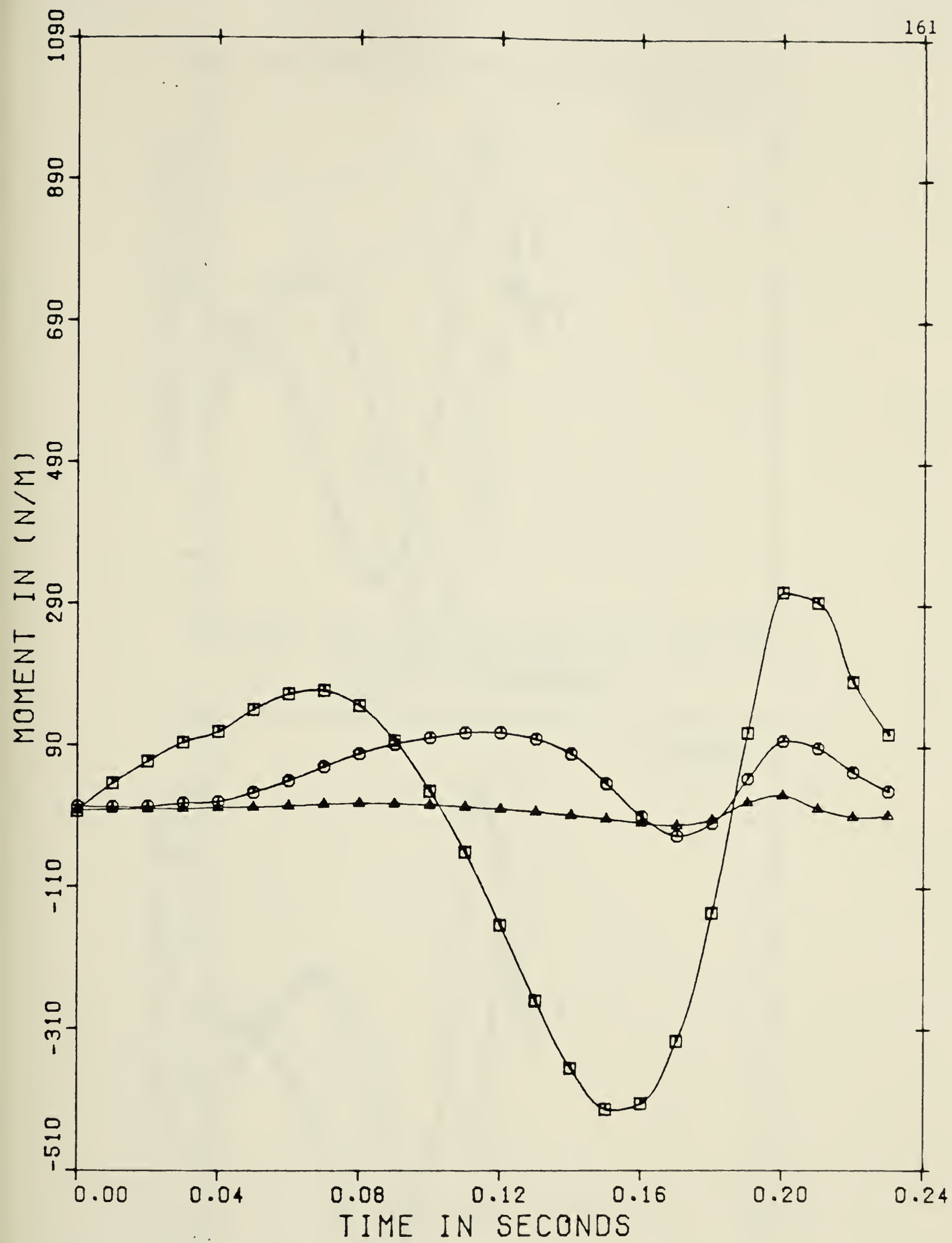


Figure 45. Resultant Moments at the Joints for Subject 3.



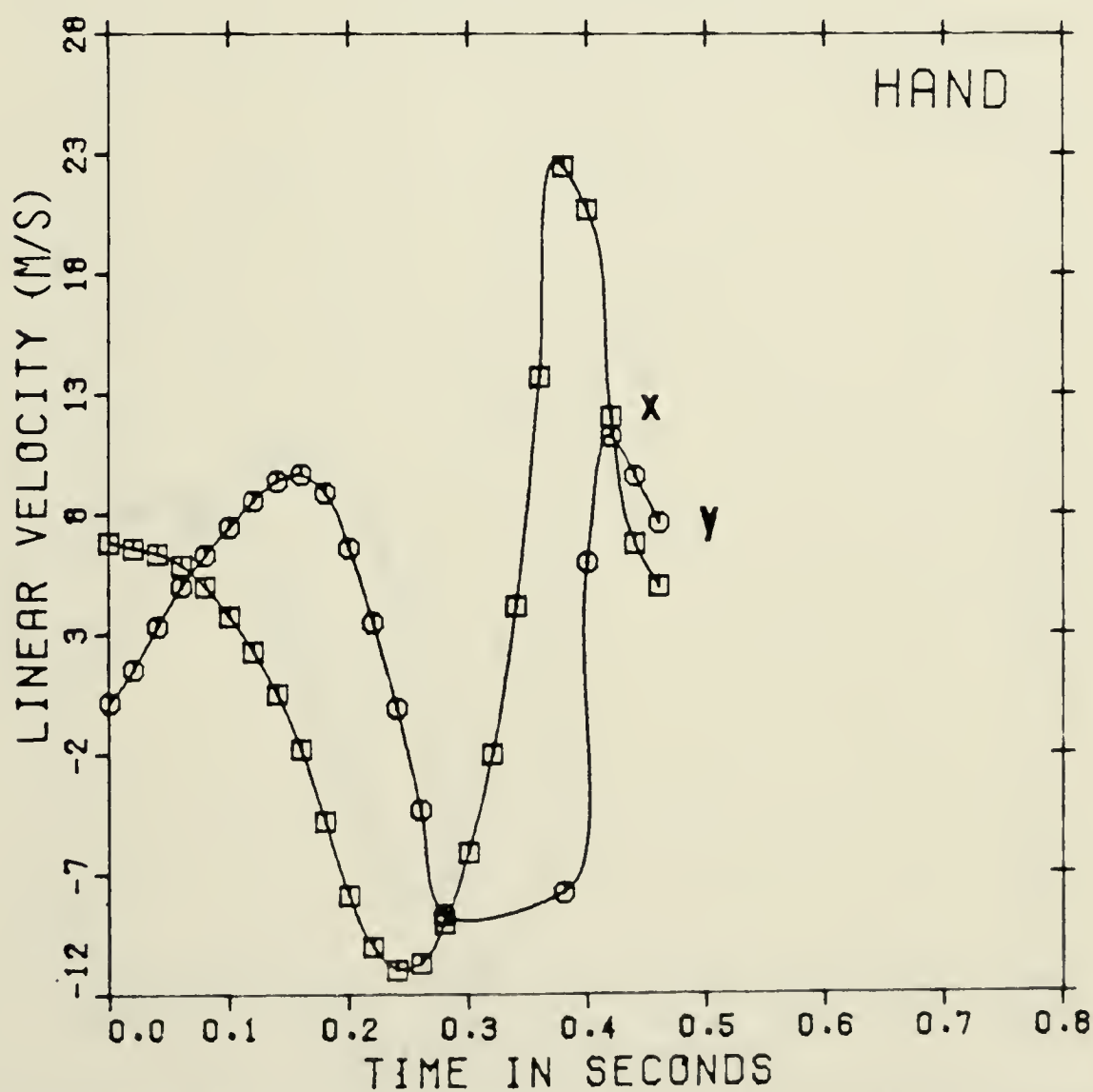
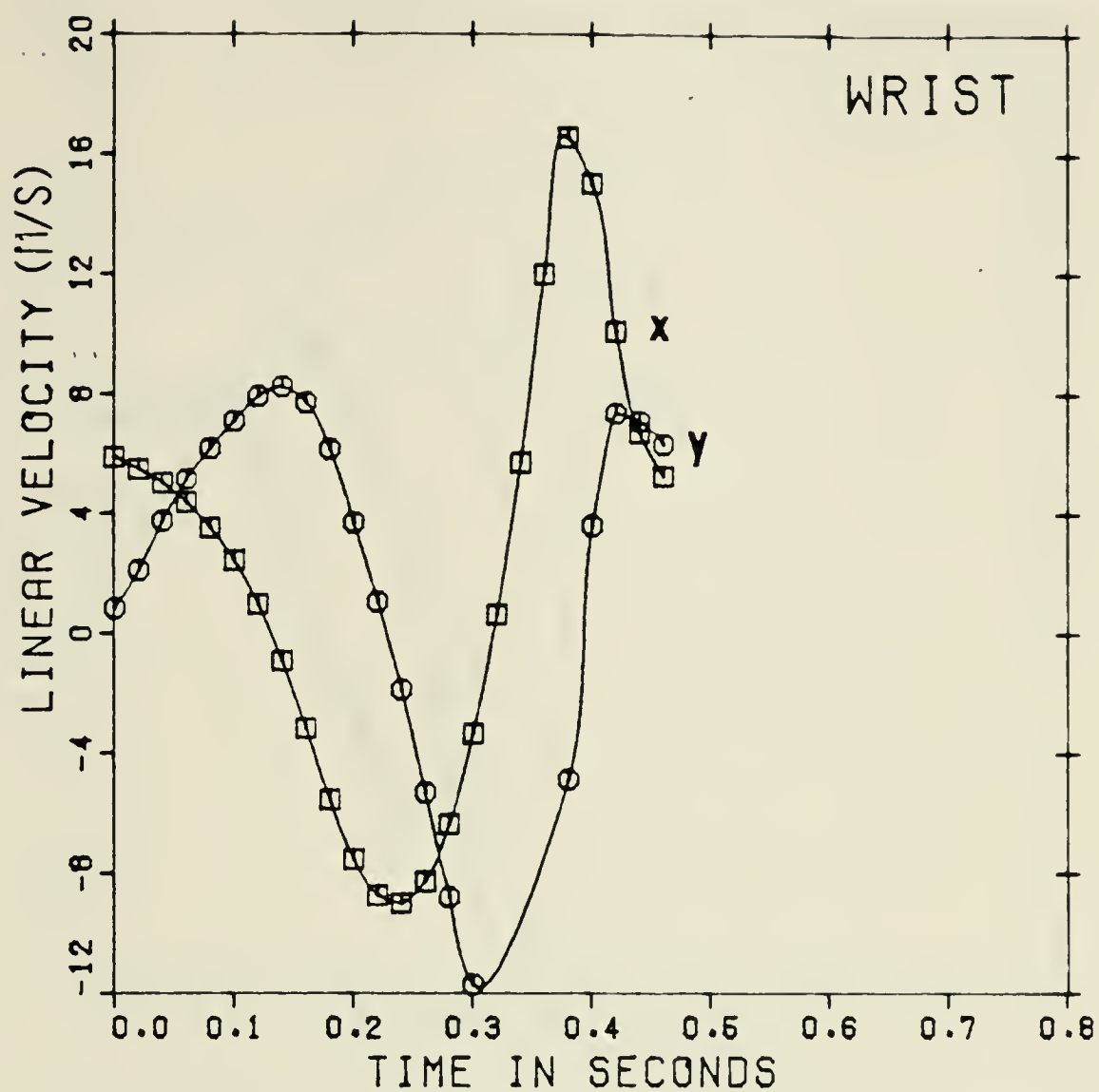


Figure 46. Hand and Wrist Linear Velocities for Subject 1.





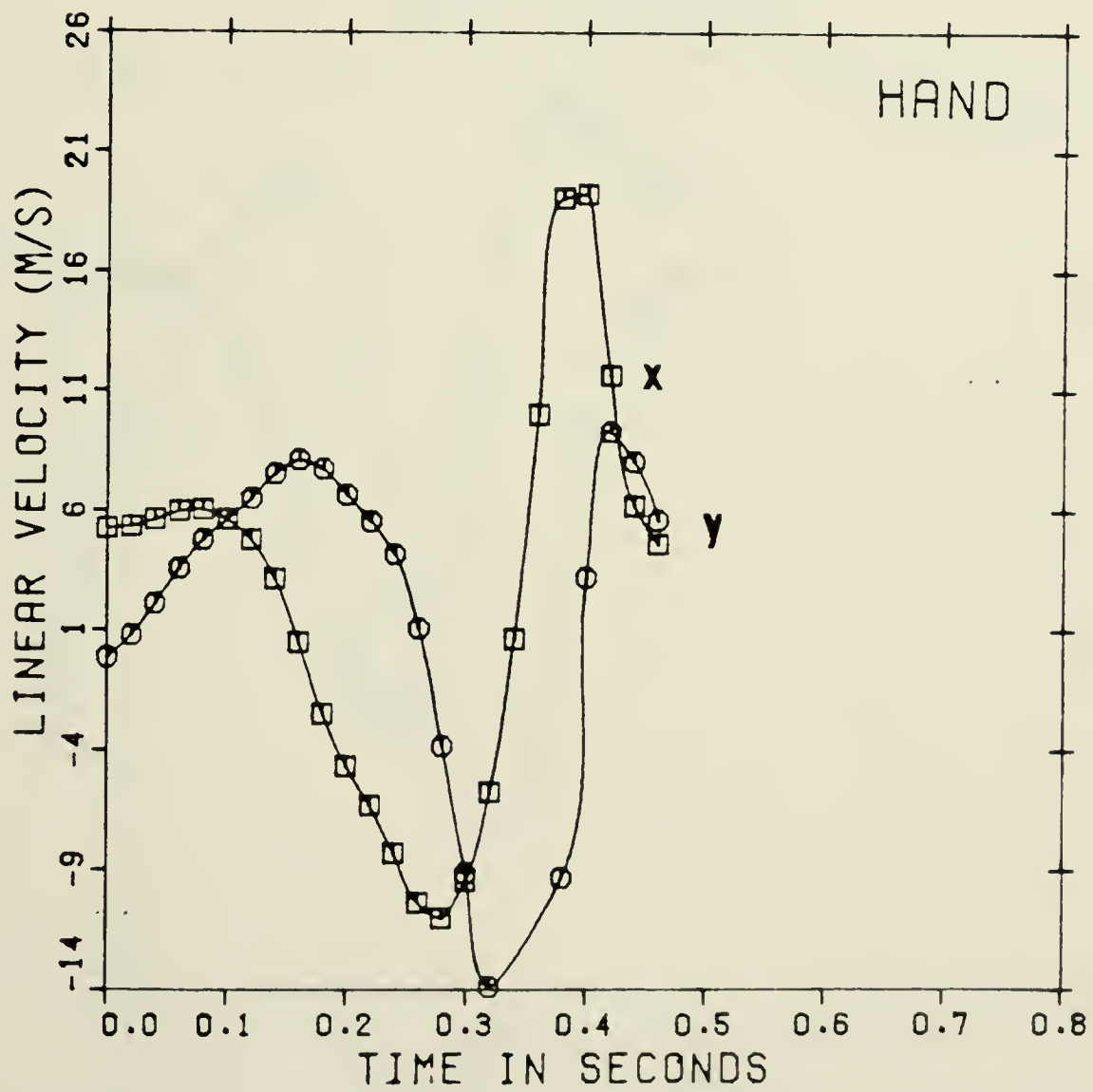
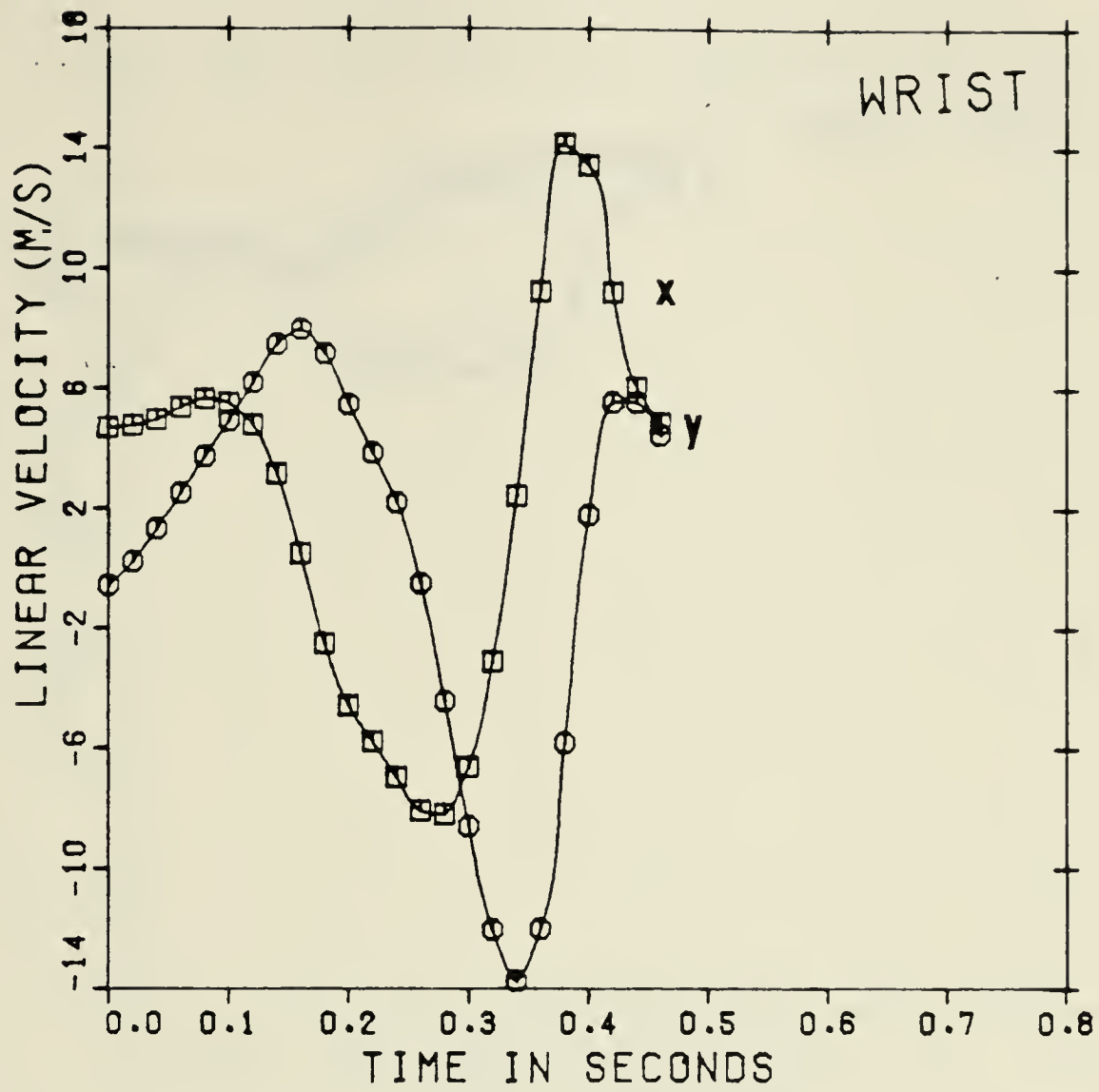


Figure 47. Hand and Wrist Linear Velocities for Subject 2.



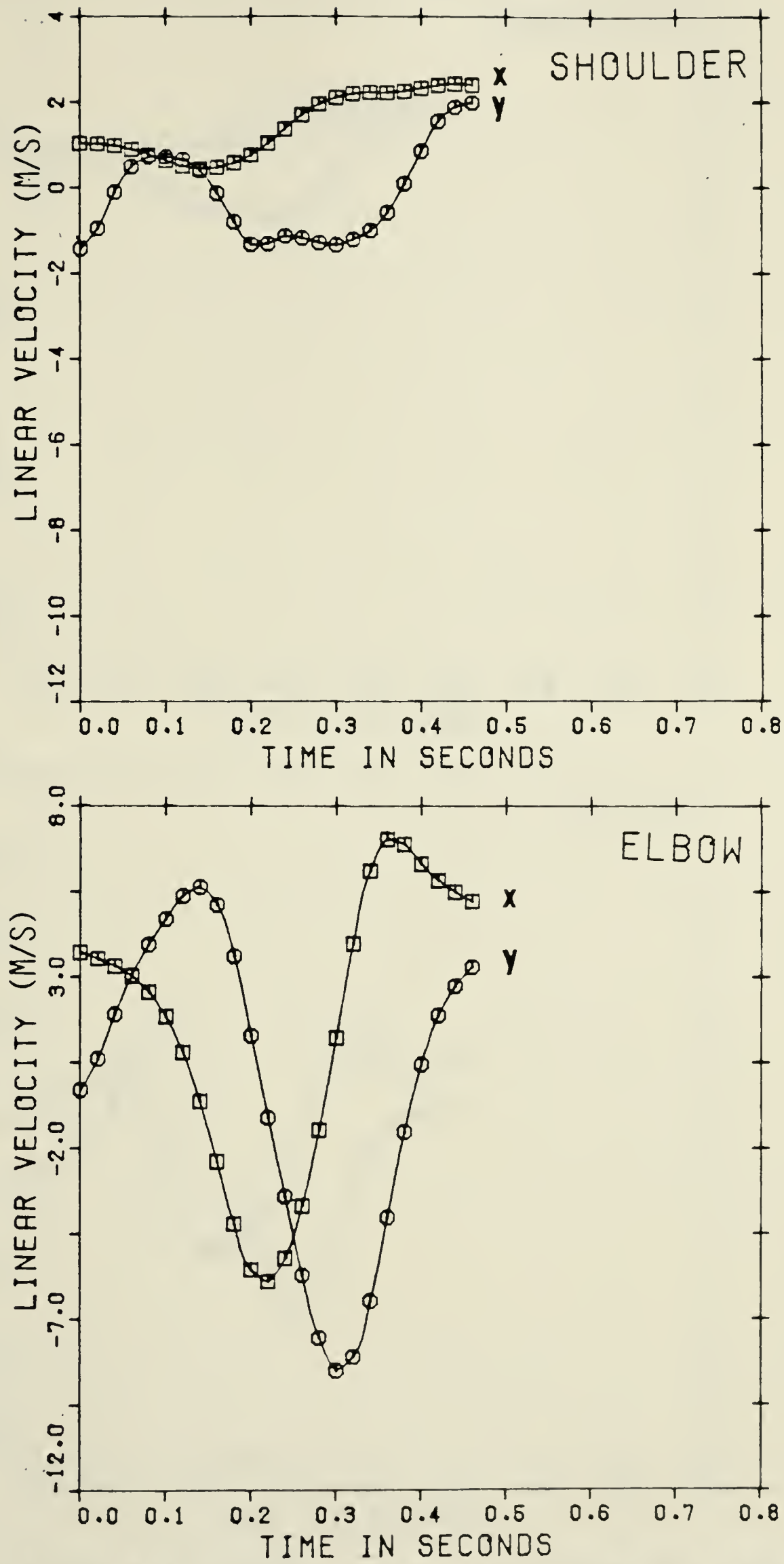


Figure 48. Elbow and Shoulder Linear Velocities for Subject 1.



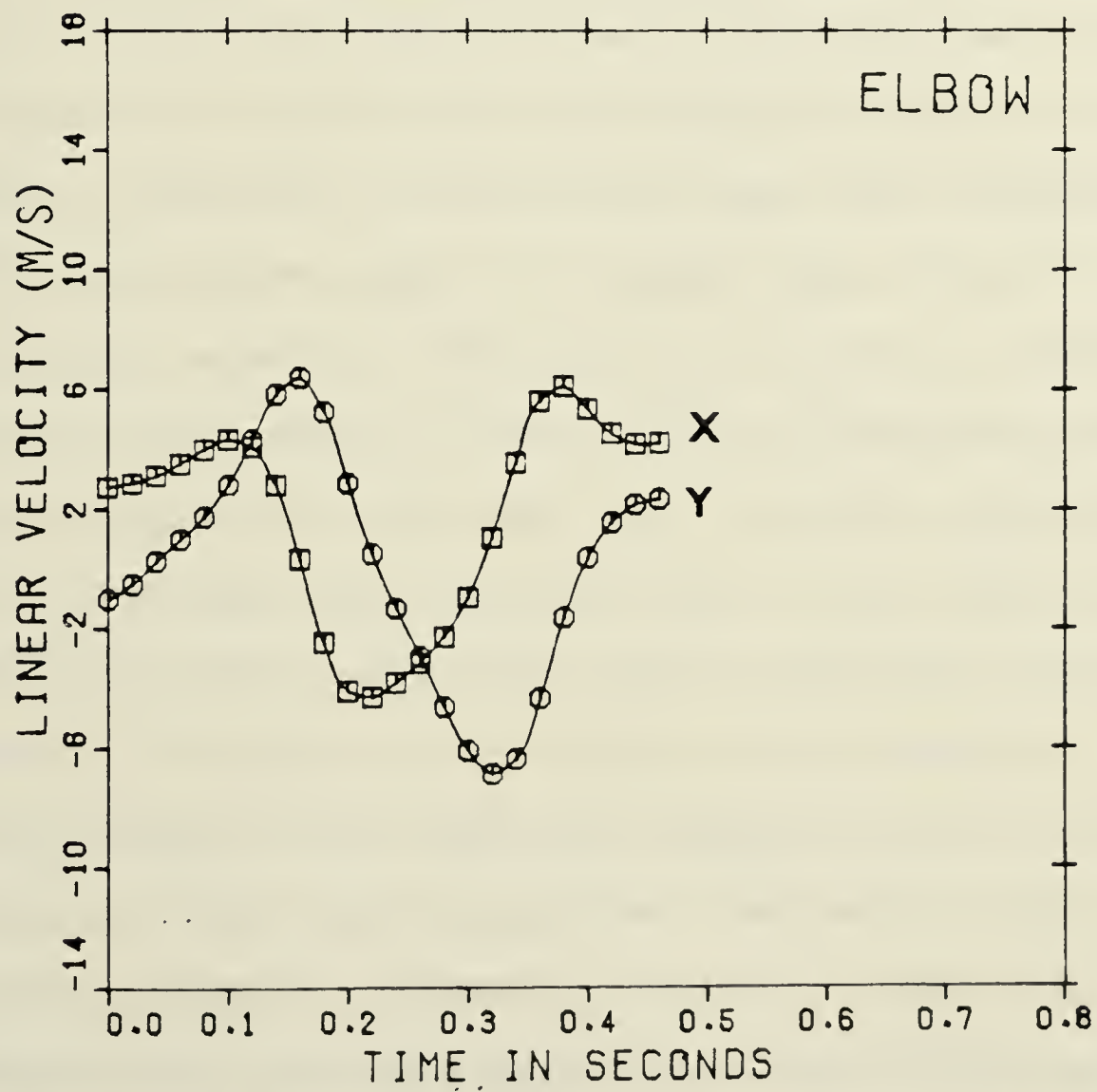
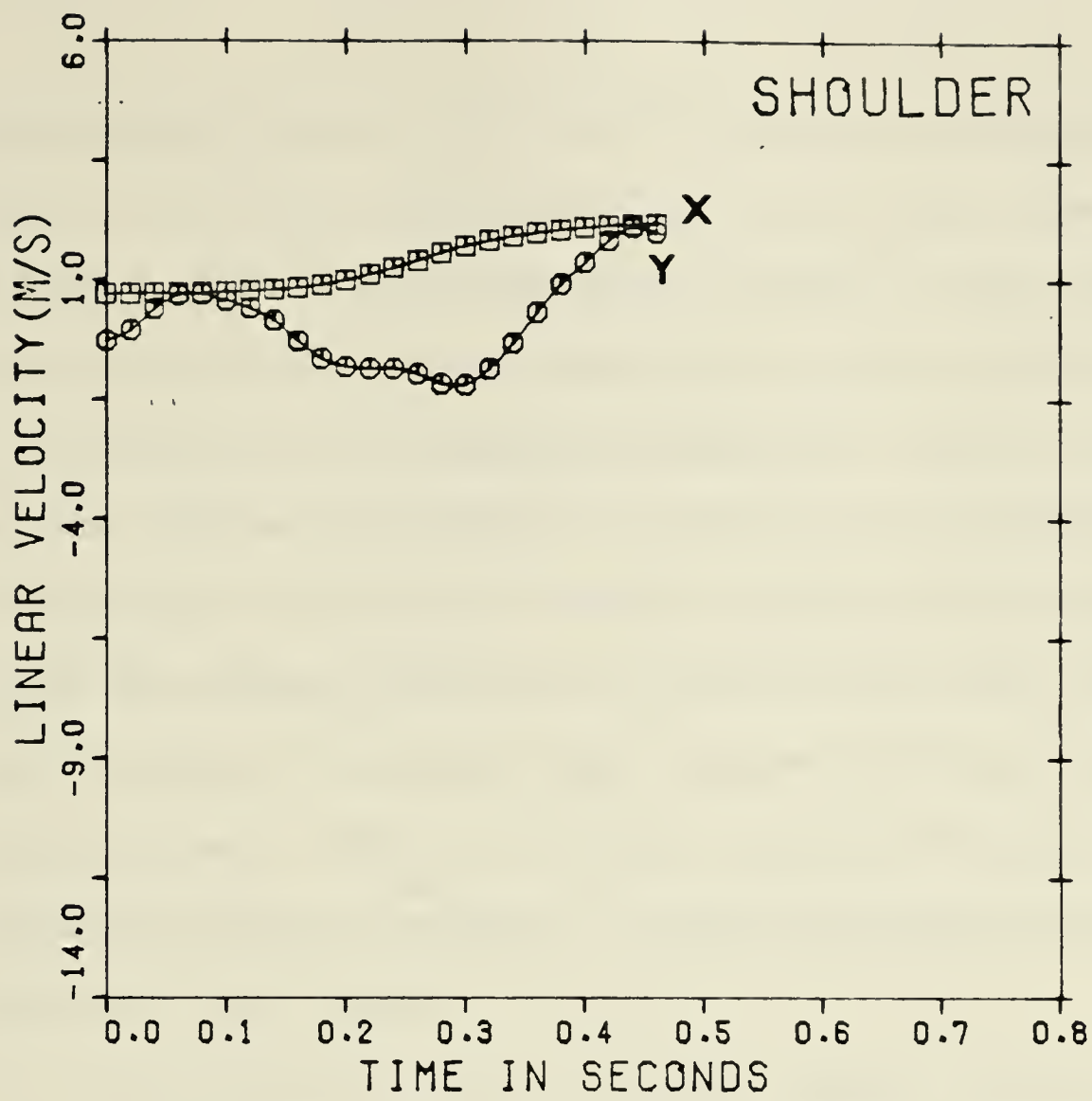


Figure 49. Elbow and Shoulder Linear Velocities for Subject 2.





displacement curves for the four pitches analyzed in detail, which were differentiated by the time scale along the abscissa. The marked similarity between these curves for any particular pitch was an indication of the reliability of the digitizing of the segmental endpoints; and the similarity between curves of different pitches was an indication of the similarity in technique between highly skilled performers. Since the curves produced for each pitch with different time scales were so similar, only one set of these curves are included here. Figures 9-16 and Figures 17-23 all represent the same pitch of subject 1, but digitized separately over a different time scale.

The curves for each of these angular displacements are very similar for each of the pitches analyzed in that all curves for each of the three segments exhibits an upward slope indicating an increasing angle when graphed against time. The wrist began at a lesser angle than the two proximal segments, which in this case was a larger negative number--all angles in this study were measured from the right horizontal. The two upper segments remained at almost the same angle for the first part of the wind-up motion, since the elbow joint was almost completely extended for the first .12 seconds of the motion. This resulted in the displacement curve which was characterized by nearly parallel lines for the proximal segments in the early part of the pitch. The curve for the hand segment inclination shows some variations during this time, which were likely



due to the rotations which were occurring in the upper segments. Since these rotations were not measureable in a single plane, they were apparent only as they affected the position of the hand segment during the windup.

After the first .18 seconds of the windup, there was a shift in the relative positions of the segments--there was an increased flexion in the elbow joint so that the upper and lower arm segments no longer exhibited the same angular position. As these two displacement curves were moving further apart, the hand segment was altering its' position so that it came to lie at the same angle as the lower arm. This was apparent in the graphs of these curves, in that the lines for these two segments lie almost parallel and in close proximity up to the point of release of the ball, which occurs .40 seconds after the windup starts. At this point the curves for the hand and lower arm segments turn sharply upwards, and in fact the angles of both of these segments pass that of the upper arm segment, as indicated by the crossing of the three lines. These two curves continued to move upward at a rapid rate through the point of release and the early part of the follow through, at which time they were no longer parallel as their angles were changing in relation to the wrist.

The curve of the upper arm inclination was a flatter curve, as it moved upward at a relatively constant rate through release. It was notable that the maximum slope of the displacement curve for the upper arm motion was reached





earlier that that for the two distal segments, indicating that there was a sequential nature to these movements. Pearson, et.al (1963) reported angular displacement-time curves similar to those reported in the present study, although the throwing skill analyzed in that study was only a modified shoulder flexion movement, not a ballistic throwing motion. Miller and Nelson (1973) also reported displacement-time curves for the leg segments during kicking, and these segments also exhibited the above pattern. Roberts and Metcalfe (1968) reported displacement-time curves of a kicking skill in which there are some opposing motions occurring in the leg segments. They noted that as the thigh segment moves forward to begin the kick, the leg segment is still moving backward, so that there is little net rotation of the leg segment at this point in the skill.

### Angular Velocity

The angular velocity of each of the segments was also graphed against time for this skill. The most notable finding from the velocity graphs (Figures 10, 17, 24, 31, 38) is the timing of the peak velocities for each of the segments. In all the pitches studied in detail, the peak angular velocity for the upper arm segment was reached from .04 to .06 s earlier than that for the lower arm segment. As the peak velocity for the proximal segment was reached, the next segment (the lower arm) began to increase velocity rapidly, so that the velocities of each of the segments were added





successively. The other notable finding was that the peak velocities of the lower arm and the hand segment occur at almost the same instant in time, or during the same .01 second interval between frames in this study. There was a slight difference in this finding between the four subjects tested. Subject 1 attained the peak angular velocities of these two segments .01 seconds apart (Figure 10), so that the lower arm segment attained this peak first. However, in the graph of Subject 1 over the longer time period (Figure 17), these two peaks appear to occur at the same instant, or over the same .02 second time interval. These peaks occur at the same time for subjects 2 and 4 (Figures 24,38), and subject 3 again exhibited an early peak of the lower arm segment (Figure 38). to the time of peak velocity of the upper arm segment. This finding is in agreement with that of Koniar(1971), who also noted that a skilled performer will reach maximum velocity of the segments at virtually the same instant. The angular velocity of the hand segment begins to increase sharply .04 seconds before release of the ball, so that it surpasses the angular velocity of the lower arm at a point just prior to release (.02 sec).

The shape of the velocity curve for the upper arm segment showed a gradual increase in velocity for the first .16 seconds of the pitch, at which time this segment maintained a rather constant velocity up to a point some .06 seconds before release. At this point, this velocity curve exhibited a sharp drop, indicating a rather rapid loss in



angular velocity (Figure 10). This is a most interesting finding, in that it indicated that THE UPPER ARM SEGMENT ACTUALLY LOSES ANGULAR VELOCITY PRIOR TO RELEASE OF THE BALL, and in fact is in agreement with the findings of Plagenhoef(1966) who also noted that the proximal segments slow down prior to release of the ball in throwing skills. He stated: "The velocity of a given segment can be increased by decelerating the adjoining segment. (In whole body motions where a peak velocity is desired in the hands, the properly-timed stopping action of each segment in sequence from foot to hand produces the best results) (1966:110)." This finding is also in agreement with that of Roberts and Metcalfe(1968:316), when they stated: "When knee extension starts and accelerates, the leg gains speed. Meantime, the thigh begins to slow and almost stop....The thigh slows or stops before contact so that it is contributing little, in a kinematic sense, to foot speed at contact. Thus it seems reasonable to assume that it does make some active contribution to the speed of lower leg rotation."

This description raises interesting questions regarding the mechanisms of momentum transfer between segments of the body. It is likely that this slowing down of the proximal segments has a dual effect on the skill being performed. Firstly, there is likely a transfer of momentum effect from one segment to another, so that as the proximal segment is slowed down prior to release it's momentum is partially transferred to the distal segment. This transfer of momentum





then serves to increase the angular velocity of this segment. Also the slowing of the proximal endpoint of the lower arm segment, which possesses a certain amount of angular momentum from previous movements, will cause the remainder of the segment to increase in angular velocity around this point due to this momentum. Another factor which may explain this segmental slowing was suggested by Roberts and Metcalfe (1968) as a neuromuscular mechanism. Since the distal segments trail the proximal segments for the first part of most ballistic movements due to the inertia of these segments, this puts the agonist muscle groups on a stretch. This stretch excites the muscle spindles and the joint receptors and causes a more forceful contraction of these muscles during the subsequent joint movements.

The curve of the elbow velocity exhibited a rather gradual increase in angular velocity for the first .20 seconds of the motion, at which point the elbow flexion occurred rapidly through the point of release. The curve which showed little smoothness was that for the velocity of the hand segment--there were two other notable peaks in the angular velocity of this segment prior to release. As was stated earlier, these irregularities are undoubtedly due to the rotations which were occurring in the two proximal segments around their longitudinal axes--since this analysis was carried out only in the X-Y plane, these rotations were not measurable even though they did have an effect on the position of the hand segment. It is notable, however, that





although the velocity-time curve for the hand segment is quite irregular in shape, the same shape is apparent in all the graphs for this segment (Figures 17,24,31,38). All of these curves have three peaks, corresponding the three separate positions of this segment. The first peak occurs as the hand is being raised in front of the body during the first part of the windup--the rotation of the forearm causes an apparent change in this angle. The second peak occurs as the hand is being lowered from a position at the top of the backswing--as the arm is being flexed, the wrist becomes hyperextended and causes a relatively rapid change in the angle. The final peak occurs, as stated earlier, at the instant of release as the wrist is seen to exhibit rapid flexion, as viewed from the X-Y plane. Since this set of data was analyzed only in the X-Y plane, from the view of only one camera, the movement of the wrist appeared to be flexion. However, the movements of the tape markers on the arm segments indicated that these movements were actually rotations of the segments around their longitudinal axes, which could not be accurately quantified in this part of the analysis.

#### Angular Accelerations

The acceleration-time curves for the three segments of the upper extremity during the softball pitch show a more marked distance between their peak values than did the



velocity curves (See Figures 11,18,25,32,39).; The peak acceleration for the upper arm segment is reached first, at a point .06 seconds prior to release of the ball; this is followed by the peak for the lower arm segment .05 seconds later, and then the peak acceleration of the hand segment occurred .01 sec prior to release of the ball. It is interesting that there is such a measurable lag between the peak accelerations of each of these segments, but as is apparent from the graphs the accelerations are added successively from the proximal to the more distal segments through release of the ball.

After each segment reached its' peak acceleration value, the curves dropped sharply, indicating a deceleration or loss of velocity. Otherwise, the curves for the two proximal segments are similar to those seen in the velocity-time curves; and once again the most marked deviations are seen in the graphs for the hand segment. However, because the process of differentiation magnifies any deviations in the data, the original slight deviations have become very large deviations in the acceleration curves--and those which have no real effect on the skill as it is being presently analyzed since they are due to rotations which were not measureable (Figures 25,32,39).

Another interesting point in the angular acceleration curves is the timing of the peak velocity in the skill compared to the timing of the peak accelerations. The acceleration peaks are reached first, and after the period



of maximal acceleration has passed, the velocity curve reaches it's peak. At the time of these maximal velocities, then, the respective segments are already in a period of deceleration, as noted by the downward slopes of the acceleration curves. This is quite reasonable in terms of the attainment of maximal velocity on the ball at release, in that the segments should have all completed acceleration phases prior to this point in time.

## Linear Kinematics

### Linear Velocities

The linear velocities of each of the four segmental endpoints have been graphed with the X-linear velocities along the abscissa and the Y-linear velocities along the ordinate (See Figures 12,19,26,33,40). These four segmental endpoints are the shoulder, elbow, wrist and fingertips. This method of graphing linear velocity values enabled the investigator to report the X and Y velocity values on a single curve, and is one which has been used in several recent biomechanical investigations. (Pearson,et.al.,1963; Youm and Yoon, 1977) When the origin is clearly marked on a graph of this type, the resultant velocity vector at each point along the curve may be represented by the vector from the origin to that point. Thus the point in the pitch in which the velocity of any of the segmental endpoints is







maximal is the point at which the distance of that curve from the origin is greatest. Since the linear velocities of the segmental endpoints increase from the proximal to the distal endpoints, the graph appears as a series of circular-shaped curves. The points at which these curves cross the X or Y axes are the points at which one of the velocity components are zero. The point of release of the ball, for example, is close to the point where the curves cross the right horizontal X-axis. At this point the Y-values are zero or minimal, and the X- values of the velocities are maximal. The largest magnitudes of the Y-velocities are negative, and occur at a point where the velocity curves cross the Y-axis, and the X-values are minimal. This point in the actual pitch occurs as the pitching arm is being forcefully flexed from the top of the backswing .

The curve representing the shoulder linear velocities has a characteristic shape unlike the graphs of of the other endpoints. This is of course due to the shoulder moving in a relatively constant path along with the whole body, while the other arm segments follow a circular path around this point in the windup motion for the pitch. In the curves in which the whole pitching motion is being represented, the curve is somewhat U-shaped due to the regular fluctuations of the Y- values of the linear velocity. From zero at the beginning of the pitch, the Y-values first rise during the early part of the delivery (.08 s), then these values drop for the next .18 s, and finally rise for the final part of



the pitch. These Y- value fluctuations are due to the arm and body motions during the delivery of the ball. The values of the X-components of the linear velocity rise gradually as the delivery of the ball progresses to a point .20 s prior to release of the ball, at which point the X-values remain relatively constant through release. This results in a velocity curve which is almost a straight line parallel to the Y-axis, indicating a relatively constant X-value. (See Figures 26,33) The shoulder linear velocity values are a good estimate of the velocity of the body mass center, since their movements are very similar. It is possible that a high X-velocity of the body at release may contribute to the final velocity of the pitch--this would seem to be the case for Subject CM in the present study. Macmillan(1976) has noted that body velocity was not related to kicking foot velocity. This fact suggested that the true role of body velocity in skills of this type is to contribute to the direction of the ball, rather than to it's velocity.

The curves representing the elbow linear velocities (Figures 12,19,26,33,40) are smooth oval shaped curves, indicating regular and constant changes in these velocity components throughout this skill. The maximum X linear velocity values occur at a point .04 seconds prior to release of the ball, at which time there is also a rather large negative Y component of the velocity. The linear velocity curves for the wrist and fingertip velocity components are also smooth and regular oval-shaped curves,





which differ from that of the elbow joint in that there is a smaller Y velocity component at release. The maximal X values of these two curves are reached at a point where the Y- velocity is very close to zero.

### Linear Accelerations

The X and Y components of the linear accelerations for each of the segmental endpoints have also been graphed on a single page for each pitch studied in detail (See Figures 13,20,27,34,41). These graphs are of the same type as those for the linear velocity values, in that their form is that of a series of concentric circle shaped curves representing each of the segmental endpoints. The smallest inner curve represents the linear acceleration values of the shoulder joint, and the curves go on in order to represent the more distal endpoints of the upper extremity. The largest outer curve therefore represents the X and Y acceleration values of the fingertips, which exhibit some irregularities which are undoubtedly due to the rotations of the arm segments during these motions.

The linear acceleration of the shoulder joint is represented by a curve which is almost a straight line. This indicated that the linear acceleration values of the shoulder joint were small compared to those of the other endpoints. The most notable point about the other three acceleration curves is the direction of the acceleration vectors for the various points on the curve. Because the





linear acceleration values for each of these points was composed of both a normal and a tangential component , the directions of these vectors are different from the directions of the velocity or displacement vectors. For example, at release of the ball, the acceleration vector is found in the first quadrant of the graph, so that its' direction is over 45 degrees removed from the direction of the velocity vector for the same pitch. This finding is in agreement with that of Plagenhoef (1971) , who also noted that the resultant direction of accelerations are often quite different from that of the motion occurring. In the present skill, the direction of the velocity vector for the hand at release is in the direction of the path of the hand and ball. However, the direction of the acceleration vector is different from this, and is not pointing in the direction of the motion of the hand. It is also notable that for each of the segments, the acceleration vector becomes further removed from the direction of motion of the arm segments, as the segment becomes more distal. This is of course due to the fact that the acceleration is composed of a tangential component as well as a normal component which is calculated from angular velocity values. The more distal components have higher angular velocity values, and because the normal component is at right angles to the tangential component of the acceleration, these higher values will tend to pull the resultant further and further from the actual direction of motion of the segment.



## Linear and Angular Kinetics

The accuracy of results from experiments of this nature were limited by two important factors: the validity of the anthropometric model used and the methods used to obtain acceleration from displacement-time data (Cavanagh and Gregor, 1975). Assuming that the anthropometric model used is valid for the subjects in the present study, the major problem may be that of the validity of the technique used to produce smoothed acceleration data from which the forces were calculated. However, recent investigators have stated that the cubic spline method of data smoothing produces the most accurate estimates of acceleration of body segments during sports' performances. (Zernicke, et.al., 1975; McLaughlin, et.al., 1976) These estimates are particularly critical in kinetic analyses using the force-mass-acceleration method of calculating forces at the joints and joint moments, as an incorrect estimate of acceleration values at a certain point in the skill will produce inaccurate force and joint couple values.

### Resultant Forces at the Joints

With these limitations of kinetic analyses in mind, the graphs of the resultant forces at the joints are reported in Figures 14, 21, 28, 35, 42. Once again, the X and Y components of the joint forces at each of the three joints of the upper extremity have been plotted on a single graph, which is again formed of three concentric circles. The larger outer





circle in these graphs is formed from the joint forces at the shoulder joint, which are greater in magnitude than those of the other two joints. The next curve represents the forces acting on the shoulder joint, and the final inner curve represents the forces acting on the wrist joint. This order is opposite to that seen in the earlier linear velocity and acceleration curves, in that in these earlier curves the proximal segments were found represented by the inner circles. The reason for this change in the order of representation of the segmental endpoints is that in this kinetic analysis we are now concerned with the product of the mass and the acceleration. Because the proximal segments have a considerably greater mass than the distal ones, the resultant joint forces are also larger for these segments.

It is notable that once again the resultant force vector acting at each of the joints is acting in a direction approximately 90 degrees to the direction of the velocity vectors at these joints, similar to that described earlier for the acceleration curves. As Plagenhoef stated: "Each body segment has a normal and tangential acceleration that produces unpredictable force directions---A slow moving but greatly accelerating segment can have a force direction almost 90 degrees different than if that segment were moving at a uniform velocity (1966:110)". For example, the resultant velocity vector at release for the wrist for subject 1 was calculated to be approximately 90 degrees from the direction of the resultant force vector for this same





joint. This is once again due to the fact that there are two components in the acceleration acting at right angles to one another. Otherwise the force curves are relatively symmetrical for each of the joints. All three of these force curves begin in the fourth quadrant with both X and Y components being negative. This indicated that the initial forces at all three joints point downward and backward (Figures 14,21,28,35,42). The X force then becomes positive, indicating that the force at the joint is now in a forward direction. The Y component of the joint force remains negative for the first .10 s, at which point the Y joint force is reversed and becomes positive--ie. the vector points upward. The forces at the shoulder joint have the largest magnitude, while those at the wrist joint are the smallest, once again due to the greater inertia of the segments of the whole arm.

#### Resultant Moments at the Joints

The graphs of the resultant moments at the joints are reported in Figures 15,22,29,36,43,44,45 and the calculated values from which these graphs have been drawn are reported in Appendix G, Raw Data. These curves have been drawn so that a positive value of the curve represents an anticlockwise, or flexion moment at the joint; and a negative value of the curve represents an extension moment at the joint. The most marked curve in each of these graphs is the large negative moment which represents the slowing



down, or reversal of movement of the upper extremity around the shoulder joint prior to the time of release. This large negative moment occurs at a point .03 to .04 seconds prior to release of the ball, and is closely followed by a large positive moment at the elbow and wrist joints which is representative of their period of rapid flexion prior to release. The moments at the wrist joint are really quite minimal, as can be seen from these figures.

Plagenhoef (1971:40) has stated that: "The magnitude of the moments of force indicates the extent of muscle contraction,--because the eye cannot perceive the change from acceleration to deceleration, nor calculate the effect of gravity relative to the speed of motion, it is also evident that muscle action cannot be determined visually for a simple segment motion except in a very general way." In terms of the muscle action accompanying these moments at the joints of the upper extremity, the large negative moment at the shoulder joint can only be produced by the action of the extensor muscles of the shoulder, causing a reversal, or slowing down of this motion. It is therefore likely that the shoulder flexors (pectoralis major, anterior deltoid, long head of biceps) are most active relatively early in the action, and this activity is reversed .06 seconds prior to release. It is at this point that the shoulder extensors come strongly into the action to reverse the moment at the shoulder joint and cause slowing down of this segment. This slowing down of the proximal segment then facilitates the





rotation of the distal segment, since it's relative rotation is greater when the proximal endpoint is stopped or slowed down. As Ariel(1974:75) has noted, muscle action at one joint can produce muscle action at an adjoining joint just opposite to that indicated by the movement. "The moments indicate the dominant muscle forces and the effect of one segment on the adjoining segment. In any human performance, one segment may affect the adjoining segment in a manner which is undetectable by the human eye. At times, the moments of one segment are so large that they will be the dominating muscle force at the next segment---" (1974:75).

In the moment curves reported in Figures 15,22,29,36,43,44,45,, the large negative moment at the shoulder joint produced an accompanying negative moment at the elbow and wrist joints, even though both these joints are flexing at that point in the pitch. This indicated that the dominant muscle group at release of the ball was the shoulder extensors which were acting eccentrically as a brake to slow down the flexion of the upper arm at the shoulder joint. This is a most interesting finding in light of the fact that the major force producing muscles in this skill were thought to act strongly up to the point of release. These findings indicate that an electromyographic analysis of the active muscles during the softball pitch would be interesting to compare with the moment analysis. It would appear possible from the present analysis that the most important muscle forces in this skill may not be those





of the agonist muscles to these movements, but rather those of the antagonists. Possibly in training highly skilled pitchers in the future, we should be training the shoulder extensors to act as a strong brake to this action, rather than to work for a more forceful agonist contraction.

### Three Dimensional Analysis

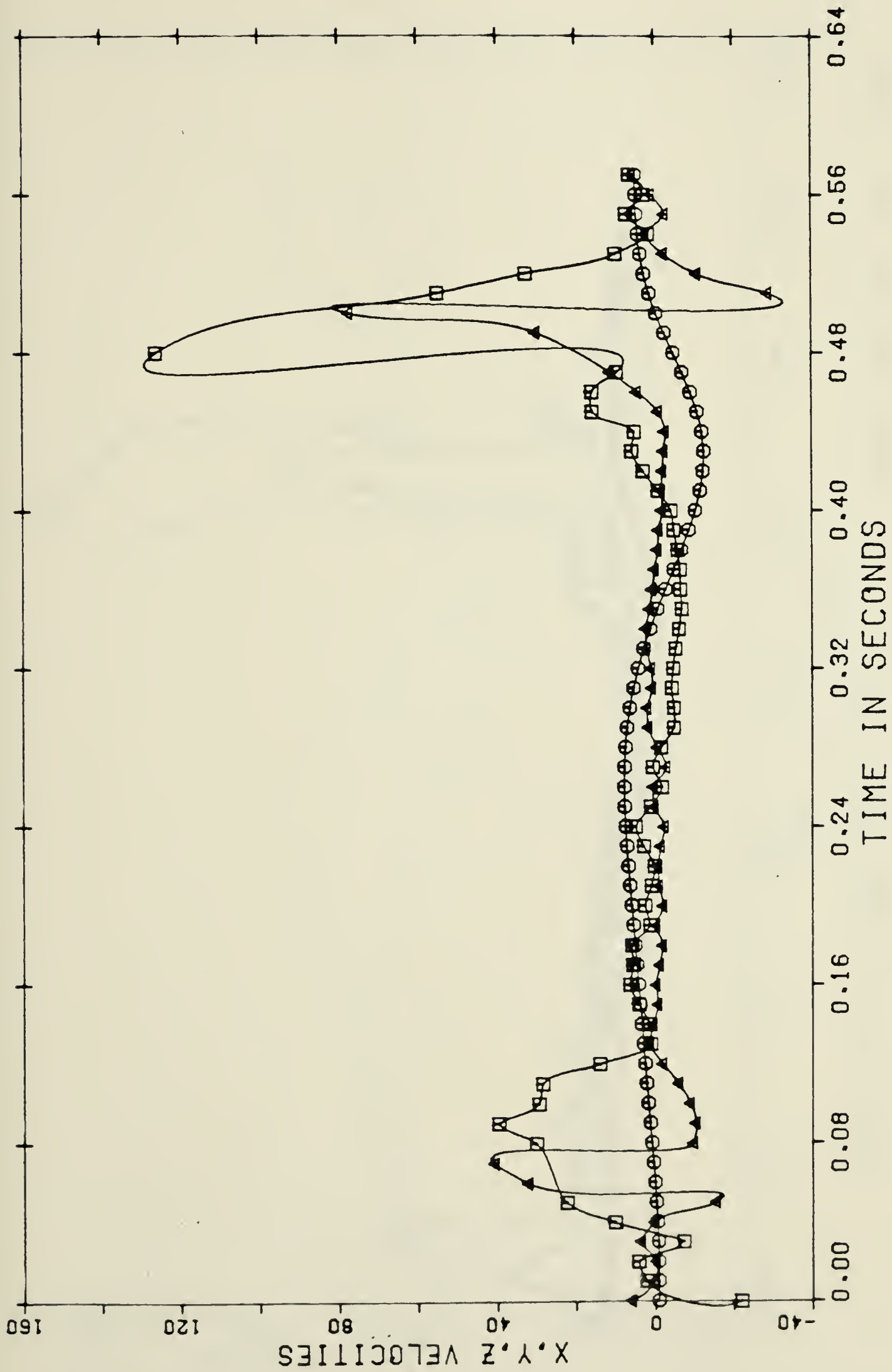
From the digitized film data from the two cameras, it was possible to produce spatial coordinates for each of the segmental endpoints of interest for the pitches of two of the subjects. These spatial coordinates for five segmental endpoints for sixty frames of film are reported in Appendix F. The mathematical probability of the value of each of the computed points being correct is also reported in Appendix F. It should be noted that a number of these computed points have very low probabilities, which are likely due to one of the following sources of error: 1. The error accompanying the digitizing of any points from film data due to location of joint centers especially when the point of interest is not in the camera view as when being hidden by another body part. 2. It was found that many of the digitized data points had been incorrectly altered in the transmission process from the HP cassette tapes to the Ahmdal computer. These were corrected as well as possible, but some of these transmission errors may have escaped detection. 3. The digitizing board is only calibrated to .01 inch, so that the



significant digits were limited to two. 4. On several occasions, one of the frames of data stored on the cassette tape could not be read back, so that both files had to be corrected for this error. 5. The most critical problem was in the synchronization of the frames of each film of this skill. The frames were slightly out of phase with one another, so that even though the frame rates were the same, it was not possible to digitize the points at exactly the same instant in time. However, notwithstanding these errors, the X,Y, and Z coordinates for each of the segmental endpoints of the arm and the ball were calculated over sixty frames of the pitch. Each of these points were then read into a computer program written by the author, in which the X,Y, and Z displacement, velocity and acceleration values were calculated for these points. This procedure was carried out for the best pitch of two of the subjects. Although the raw data was available for the other two subjects, these spatial coordinates were not calculated due to the expense of running the computer program.

The velocity graphs of the spatial coordinates of the shoulder and elbow point are quite similar for each of the subjects (Figures 54,55,56,57). The alternating peaks of the X and Y velocity values of the elbow are characteristic of this skill due to the circular motion of the arm. The velocity curves of the shoulder show little deviation, with the Y component exhibiting the greatest range. The Z component of these velocity curves has a characteristic



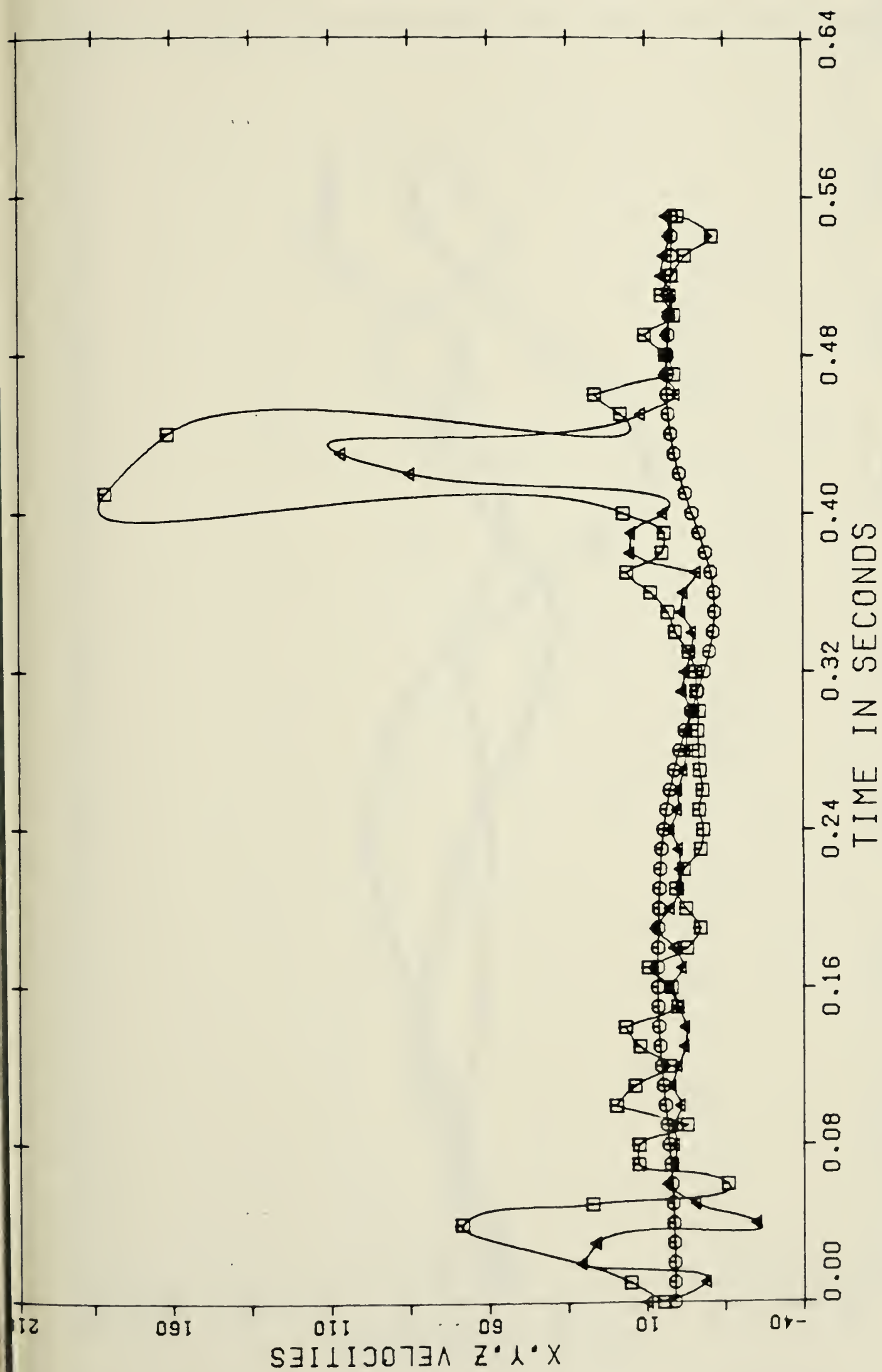


X( $\square$ ), Y( $\circ$ ), AND Z( $\Delta$ ) VELOCITY COORDINATES VS TIME

Figure 50. X, Y, Z Linear Velocities of Hand for Subject 1.



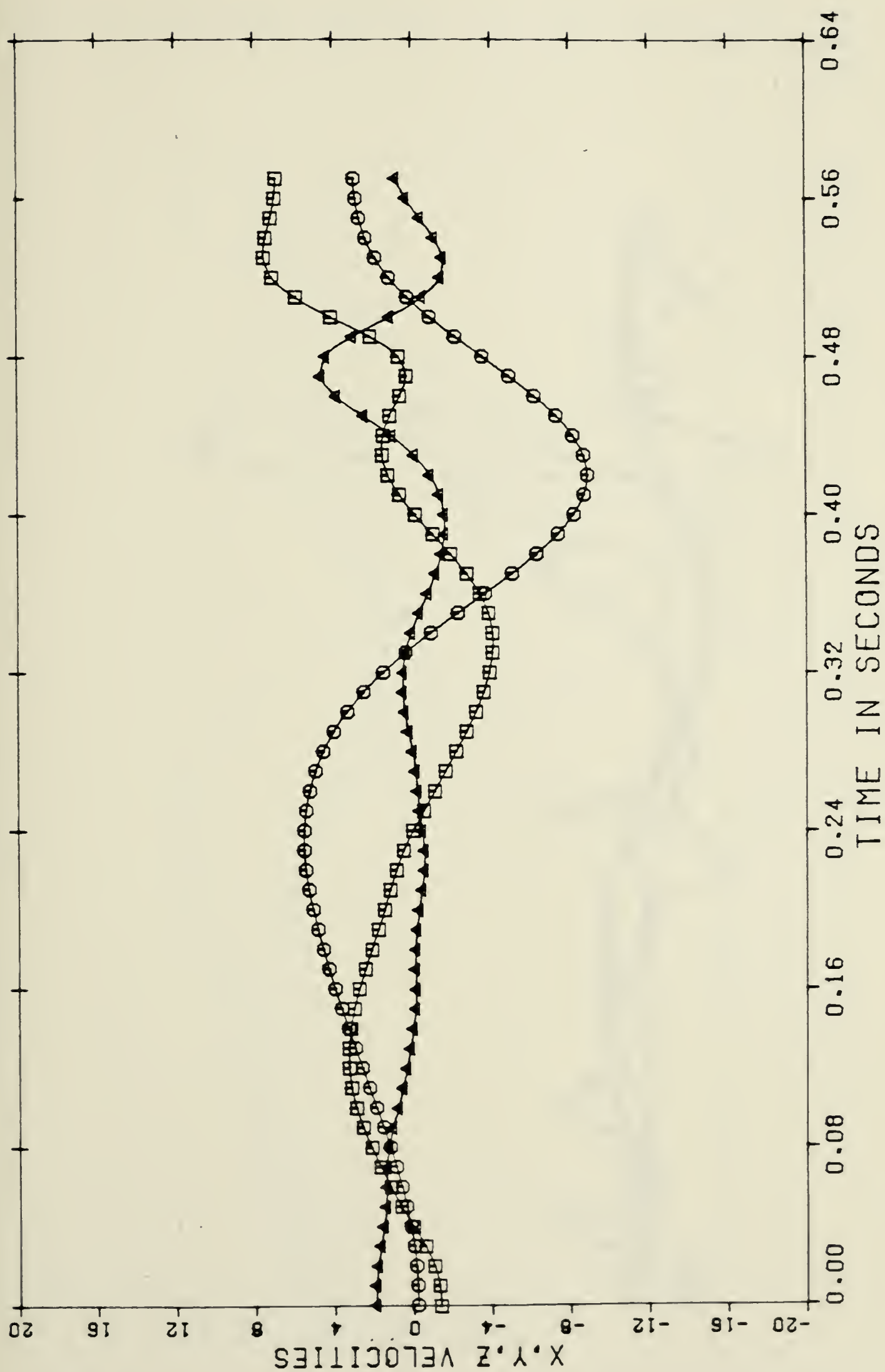




X( $\square$ ), Y( $\circ$ ), AND Z( $\Delta$ ) VELOCITY COORDINATES VS TIME

Figure 51. X, Y, Z Linear Velocities of Hand for Subject 2.

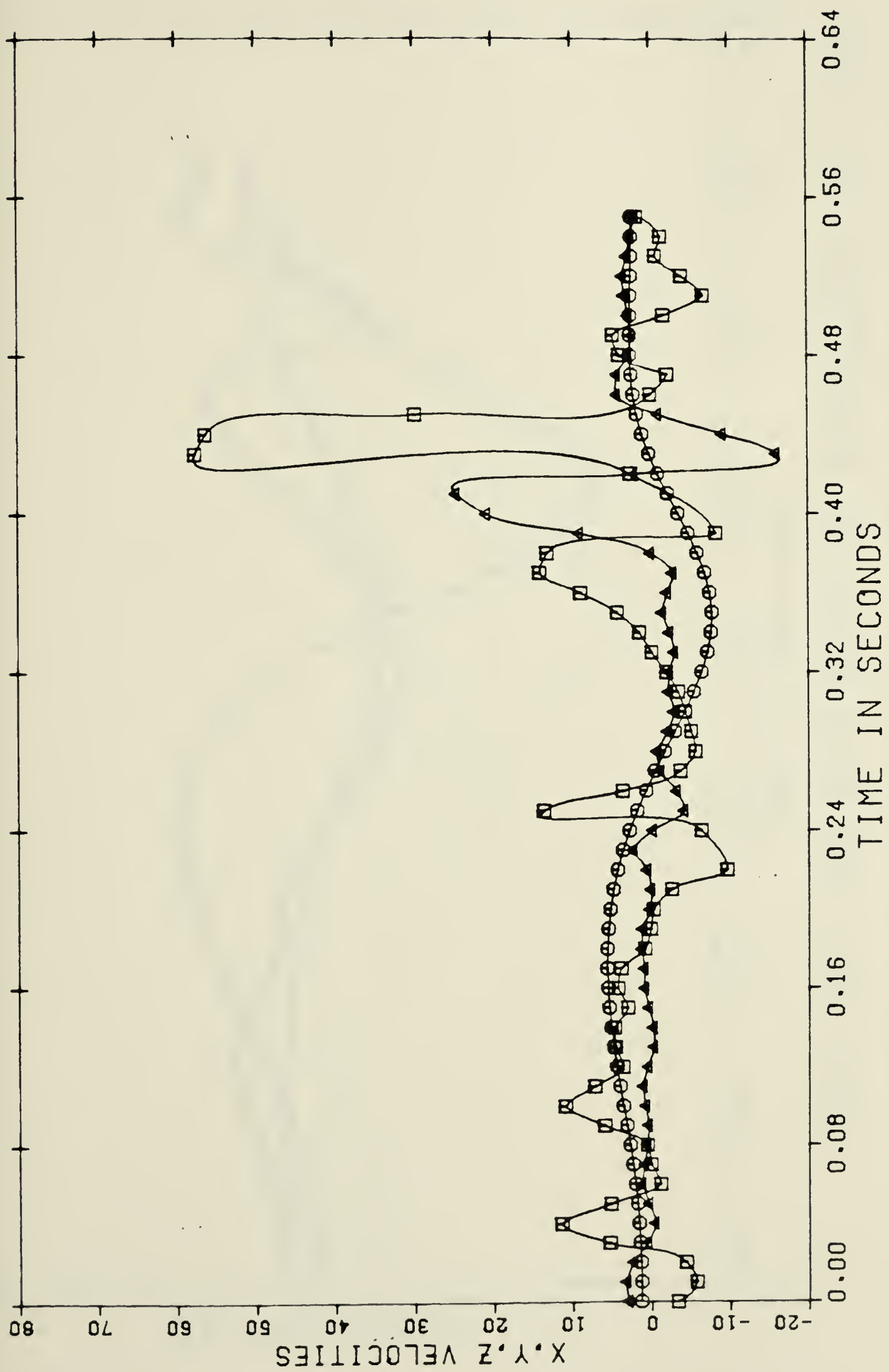




$X(\square)$ ,  $Y(\circ)$ , AND  $Z(\triangle)$  VELOCITY COORDINATES VS TIME

Figure 52. X, Y, Z Linear Velocities of Wrist for Subject 1.



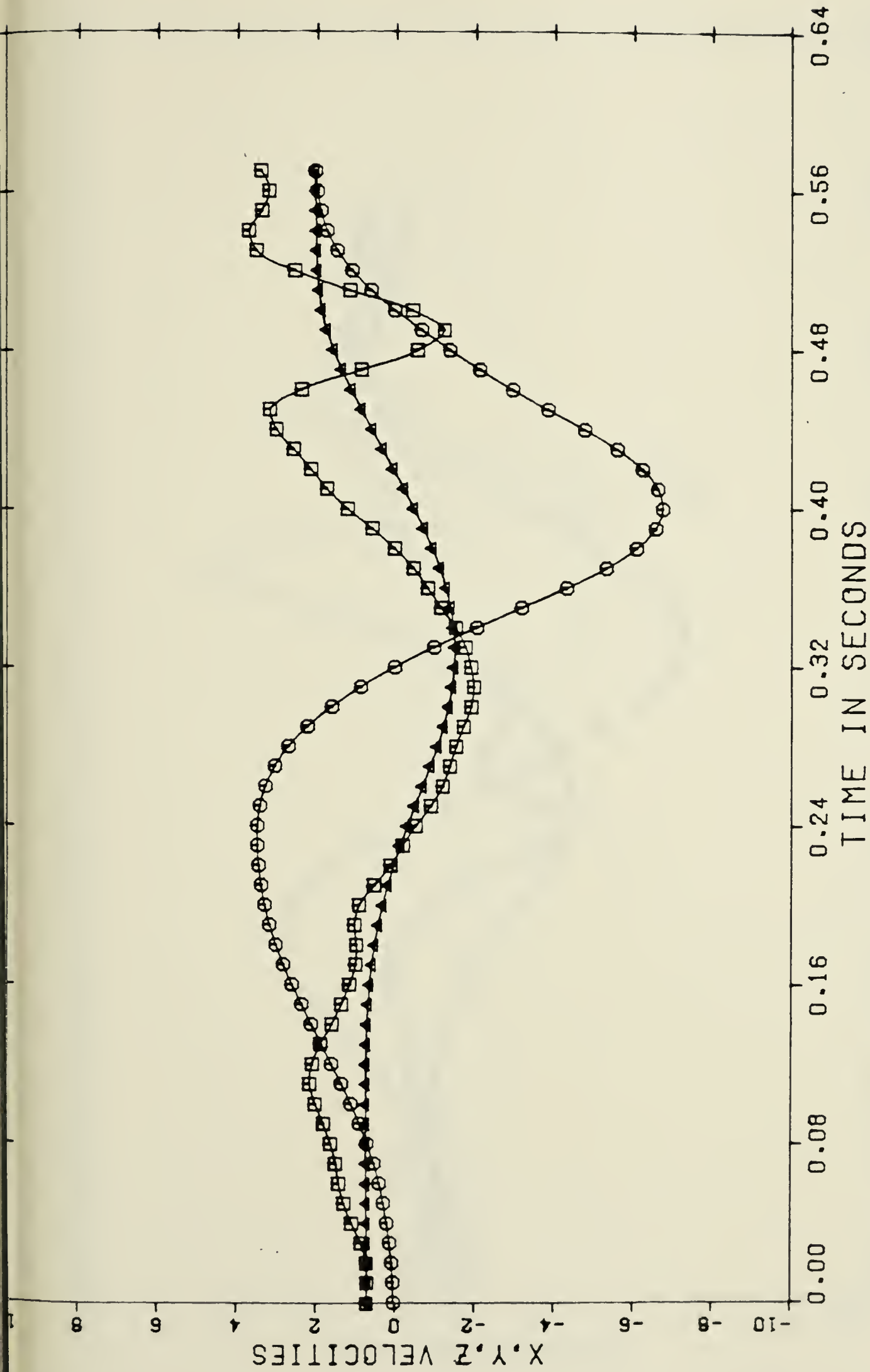


$X(\square), Y(\circ), \text{AND } Z(\Delta)$  VELOCITY COORDINATES VS TIME

Figure 53. X, Y, Z Linear Velocities of Wrist for Subject 2.



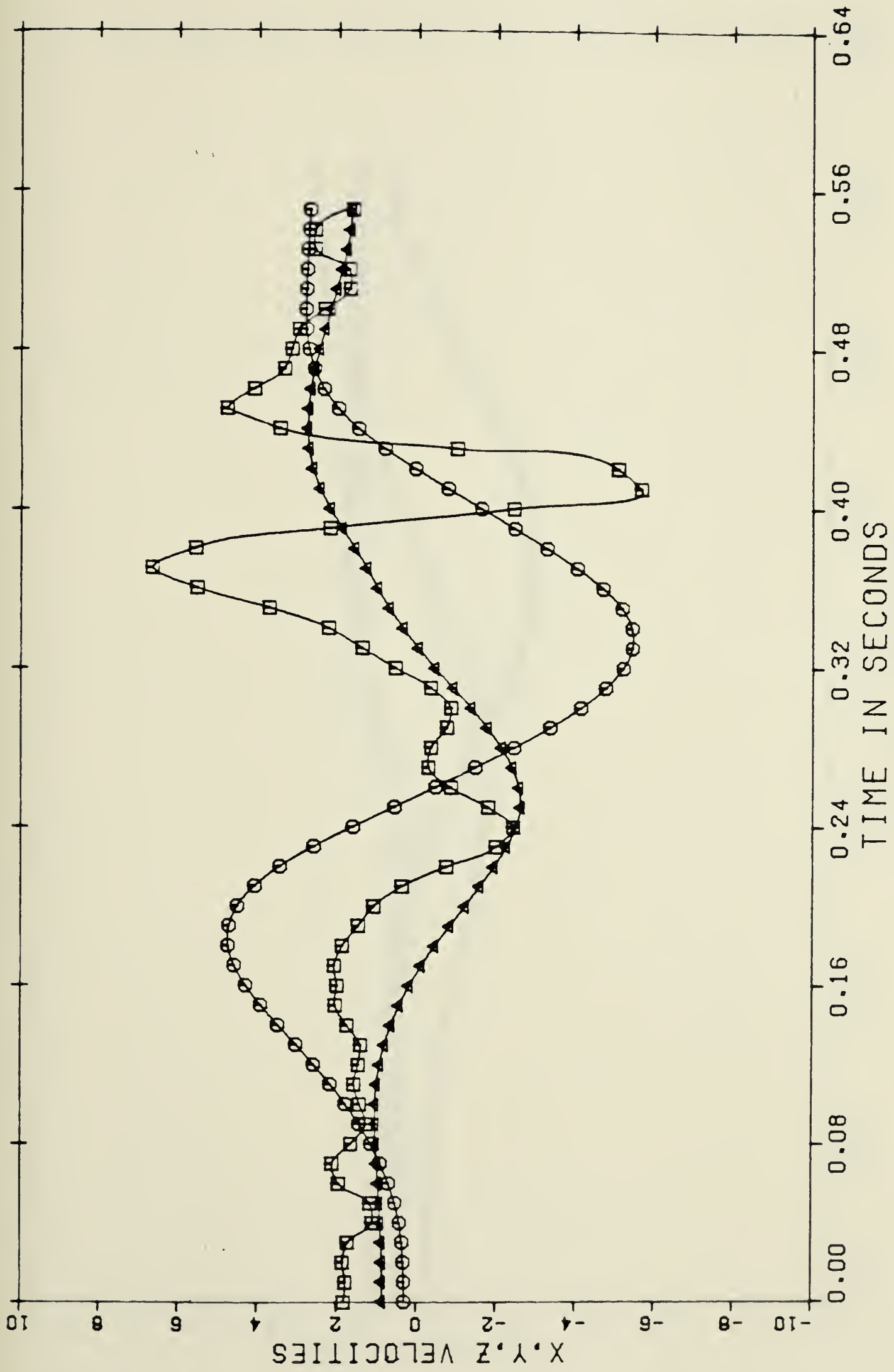




$X(\square), Y(\circ), \text{ AND } Z(\triangle)$  VELOCITY COORDINATES VS TIME

Figure 54. X, Y, Z Linear Velocities of Elbow for Subject 1.

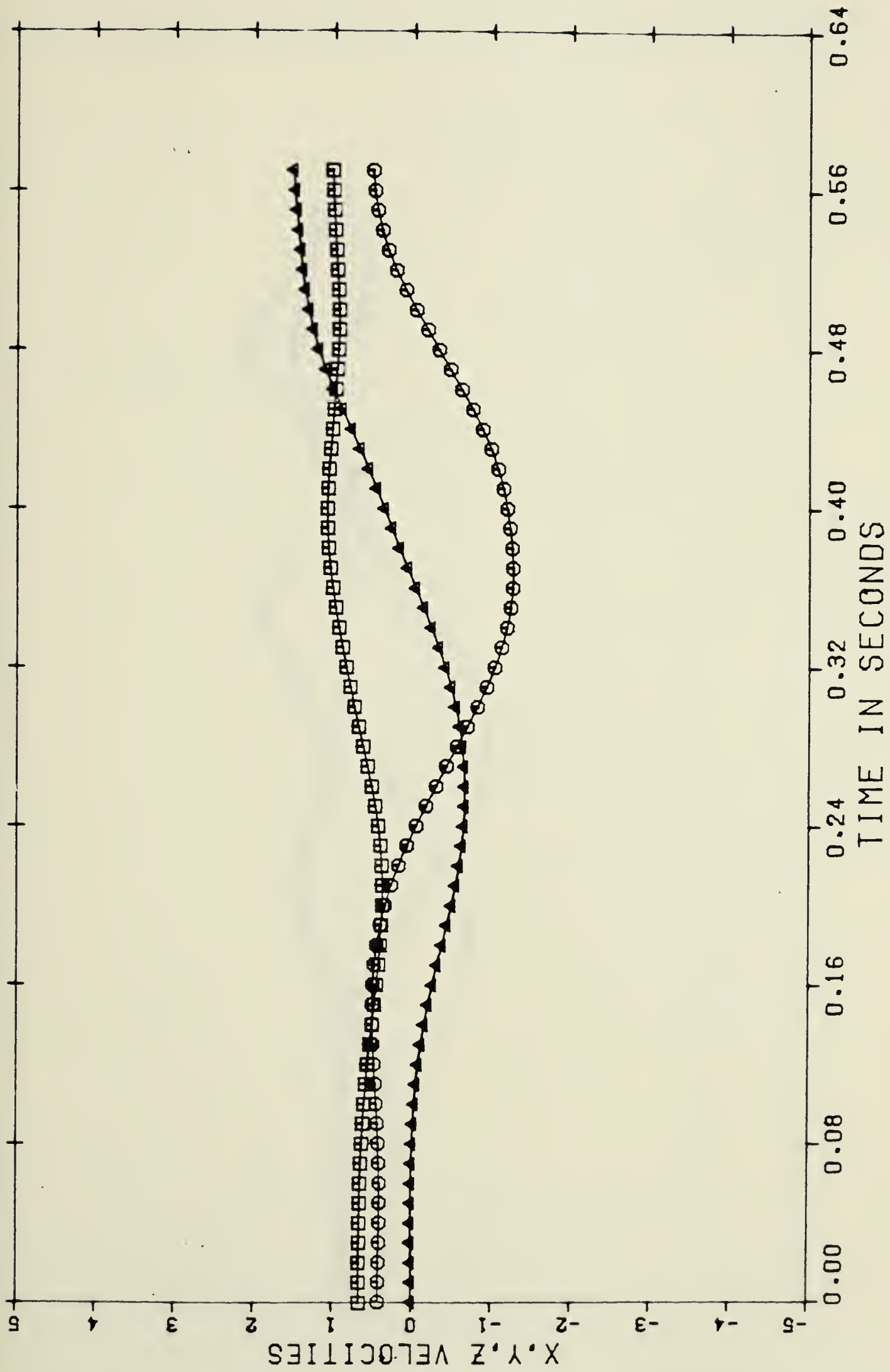




X( $\square$ ), Y( $\circ$ ), AND Z( $\triangle$ ) VELOCITY COORDINATES VS TIME

Figure 55. X, Y, Z Linear Velocities of Elbow for Subject 2.



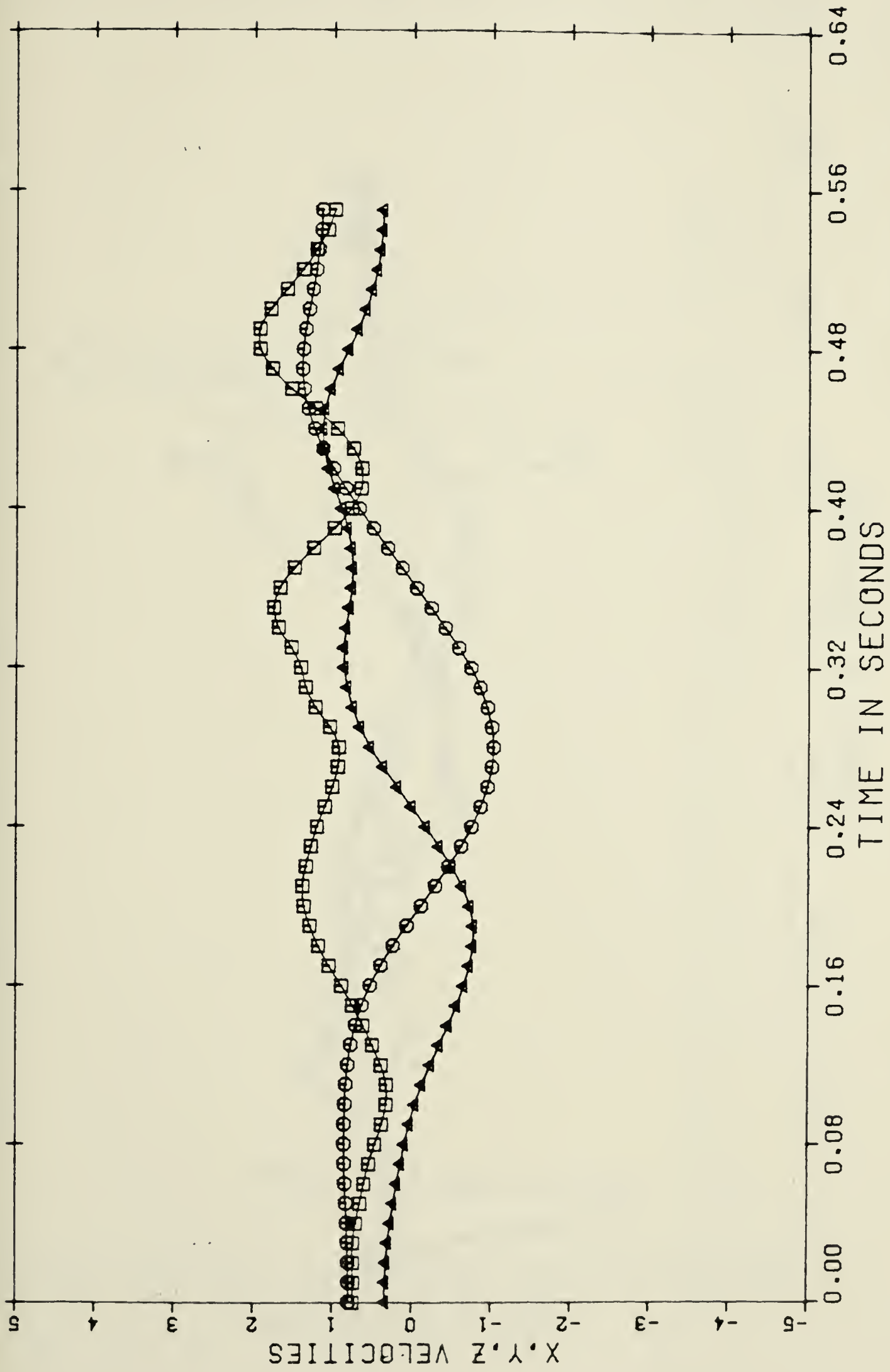


$X(\square)$ ,  $Y(\circ)$ , AND  $Z(\triangle)$  VELOCITY COORDINATES VS TIME

Figure 56. X, Y, Z Linear Velocities of Shoulder for Subject 1.



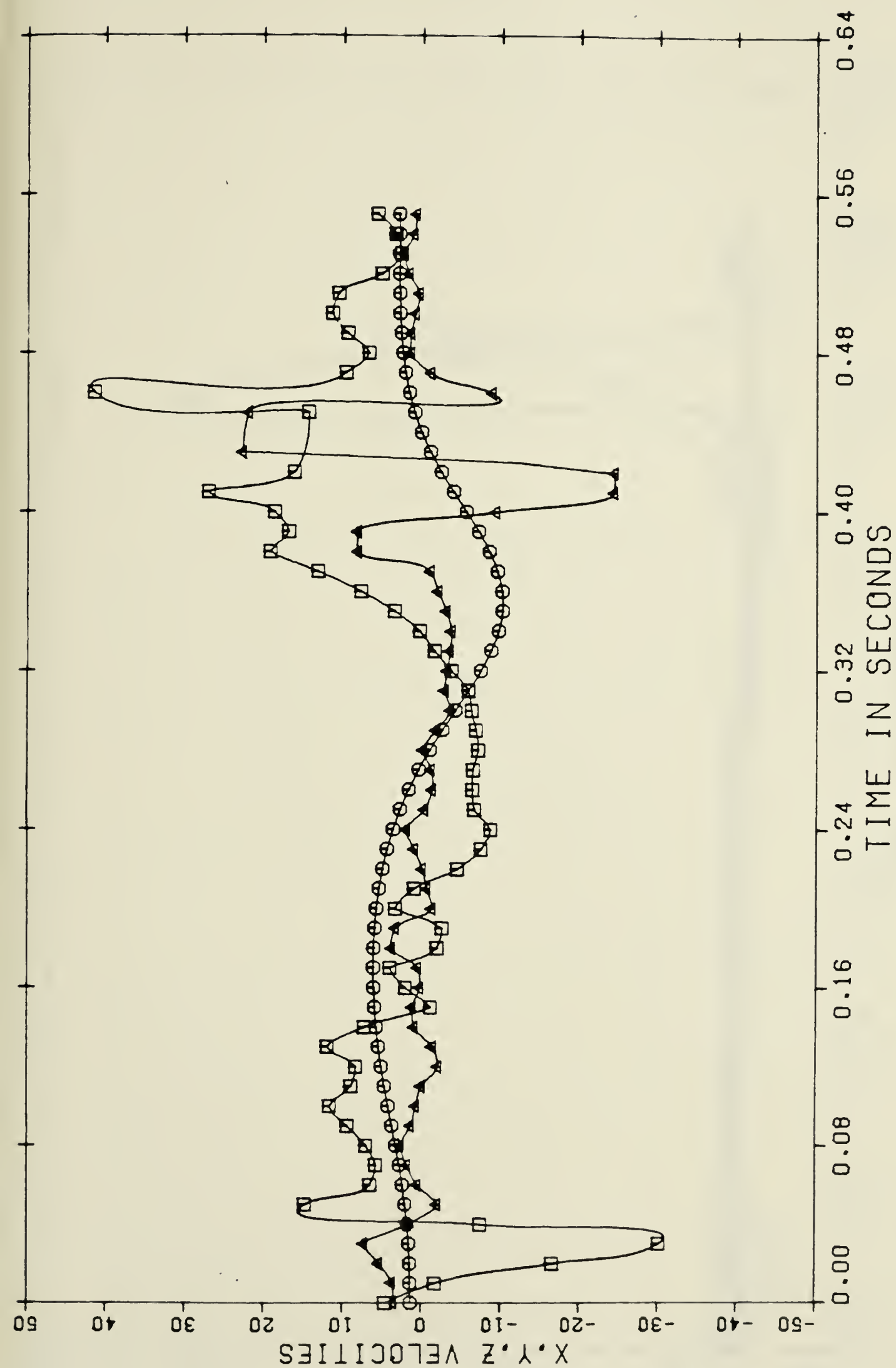




X( $\square$ ), Y( $\circ$ ), AND Z( $\triangle$ ) VELOCITY COORDINATES VS TIME

Figure 57. X, Y, Z Linear Velocities of Shoulder for Subject 2.

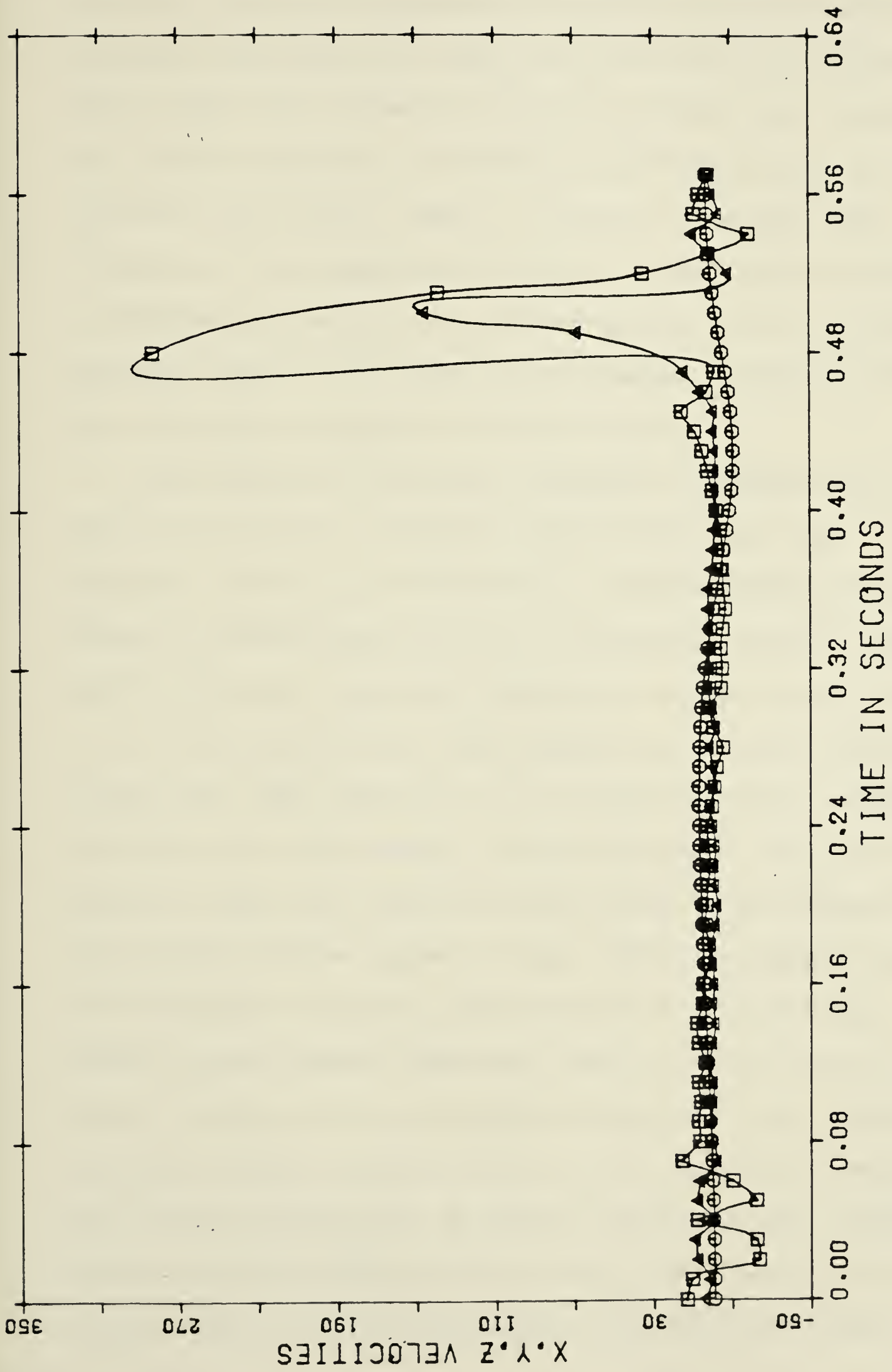




X( $\square$ ), Y( $\circ$ ), AND Z( $\triangle$ ) VELOCITY COORDINATES VS TIME

Figure 58. X, Y, Z Linear Velocities of Ball for Subject 1.





X( $\square$ ), Y( $\circ$ ), AND Z( $\triangle$ ) VELOCITY COORDINATES VS TIME

Figure 59. X, Y, Z Linear Velocities of Ball for Subject 2.





shape for these two endpoints, consisting of a slight rise early in the pitch (increased velocity laterally from the pitcher), followed by a drop .10-.12s prior to release and then a rise into release of the ball. This curve indicates that these endpoints are moving laterally during the actual release of the ball, likely a reaction from the body rotation in the opposite direction to keep the arm moving in a relatively straight line. These curves for the elbow and shoulder joints were found to be similar to those produced from the planar analysis (Figures 48,49).

The curves of the three component velocities for the hand, wrist and ball (Figures 50,51,52,53) are open to question, as they do not exhibit a marked similarity to the curves of these same points in the planar analysis (Figures 46,47). They are generally accurate, in that there is a peak in the X-velocities for these points at the time of release of the ball. The curve of the Y component of the velocities exhibited the same general shape throughout these graphs. However, there are numerous erratic data points which make the velocity curves appear rough, which are likely due to the difficulty in exact synchronization of the films. The graphs of the larger endpoints, which did not move as much between frames, were reasonably consistent. The smaller endpoints showed up more of the error incurred in having each frame slightly out of phase. However, these graphs are useful in illustrating some of the major velocity changes in these points, and in the timing of the peaks of these



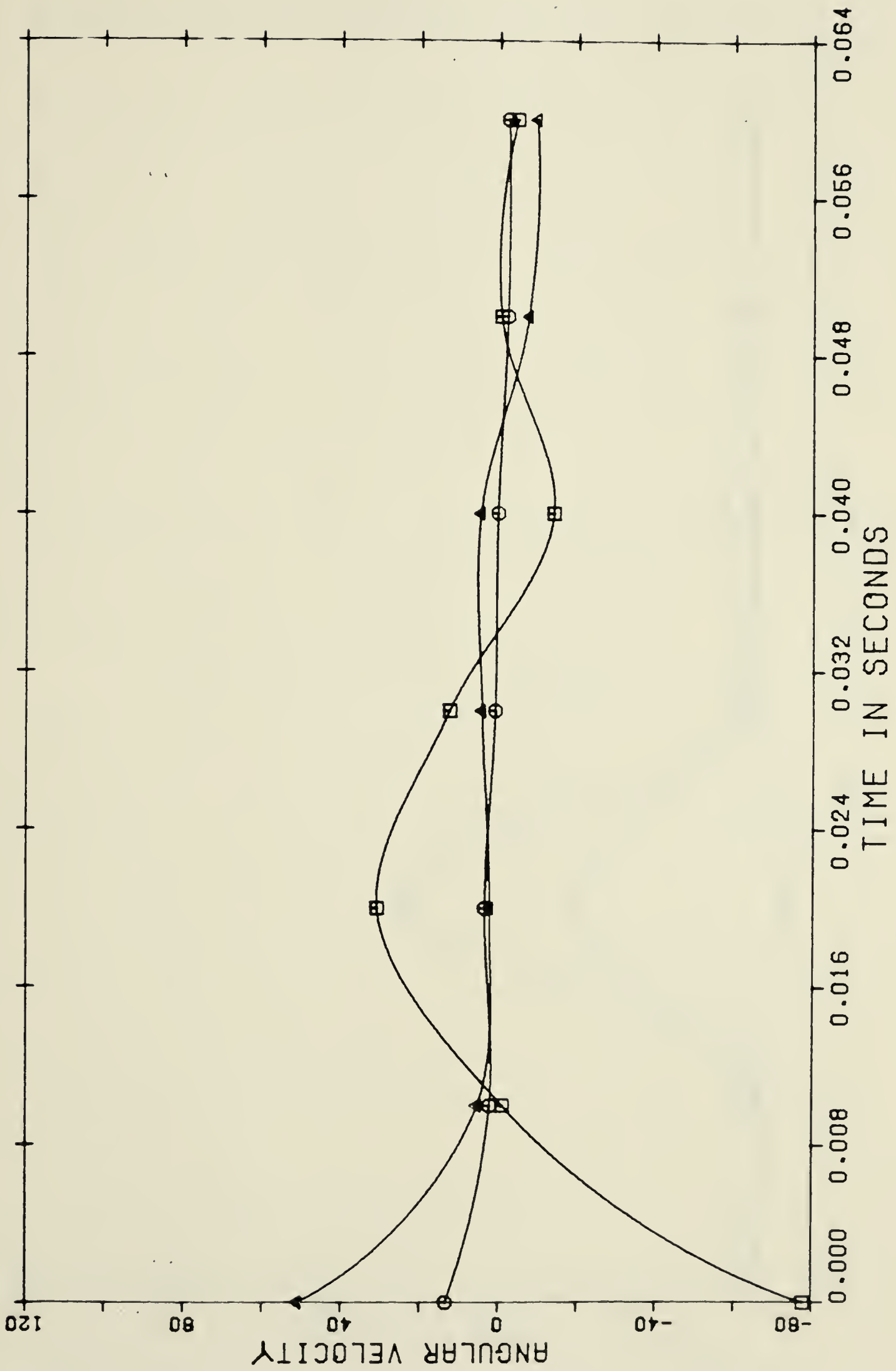
values. Probably the most useful outcome of the three-dimensional analysis was to provide a means of producing spatial coordinates of a high velocity ballistic movement, which had not been done in any other studies located by the author.

### Three Dimensional Angular Velocities

The results of the angular velocity calculations for the lower arm segment are reported in Figures 60,61. Although these values provide reasonable estimates of these angular velocity values, some of the points were not as accurately located as would have been desirable. The determination of these angular velocity values required that there were three non colinear points visible on the segment of interest for all frames analyzed. However, for several of the frames analysed, one or more of these points of the lower arm segment were not visible from one of the cameras. This was due to the rotations occurring in this segment during the skill, which were unavoidable. In future analyses of this type it would be more accurate if numerous point markers were placed on the arm segment, so that any two of these markers which were visible to both cameras could be used. A further source of error in this analysis is the problem of inability to exactly synchronize the frames from each of the cameras.

The magnitudes of the computed angular velocities for



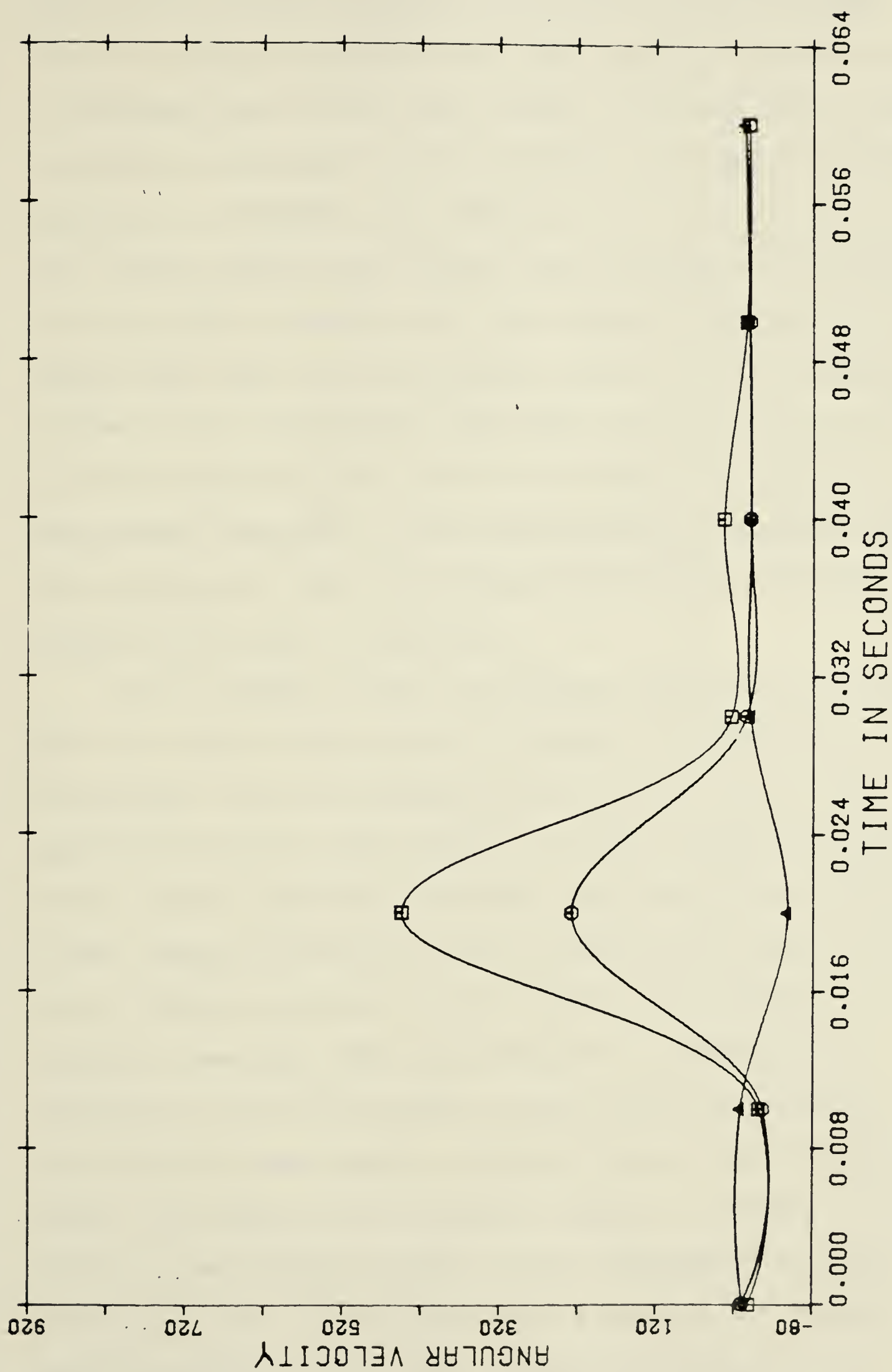


### ANGULAR VELOCITIES OF THE LOWER ARM SEGMENT

Figure 60.  $W1$ (□),  $W2$ (○), and  $W3$ (Δ) Angular Velocities for Subject 1.







# ANGULAR VELOCITIES OF THE LOWER ARM SEGMENT

Figure 61. W1( ), W2( ), and W3( ) Angular Velocities for Subject 2.



each of the pitches analyzed are illustrated in Figures 60,61. It should be noted that these magnitudes may be open to question, due to the small number of points which were available to digitize in this analysis. Because the points necessary to digitize were obscured from the view of the rear camera, only eight frames were available to digitize for this skill. However, the cubic spline routine used to smooth this data has questionable values at the endpoints, so that it is recommended that three extra points are read in at the beginning and end of the frames of interest. In the present analysis, it was not possible to provide these extra points, so that the values reported for the first frames may be open to question.

Of the graphs of the two pitches analyzed, it is likely that the graph of the pitch of Subject 1, Figure 60, is open to question. This is likely due to a larger lag in the synchronization of the frames, or a less accurate estimate of the points digitized. However, this graph does illustrate a peak angular velocity in the w1 direction, which is that of the flexion movement at the elbow joint, which is likely accurate. However, this graph failed to illustrate the magnitude of the w2 rotation, which was the supination-pronation of this segment, probably due to these sources of error. The graph of the pitch of Subject 2, Figure 61, is likely a reasonable estimate of the magnitudes of these rotations. This graph illustrates a peak in the flexion angular velocity at the same instant as a peak in the



pronation angular velocity, so that both of these joint movements are occurring at the same time to produce the resultant velocity of the ball. The magnitude of the abduction-adduction angular velocity is seen to be minimal, as is likely the case during this skill.

Although the reported angular velocities may provide fairly accurate estimates of the segment rotations, no attempt was made in the present study to verify these results. However, the development of this technique to estimate the amount of rotation occurring around all three axes of a given body segment should prove very useful to other researchers which are concerned with analysis of these movements in other, similar ballistic skills.





## CHAPTER V

### SUMMARY AND CONCLUSIONS

#### SUMMARY

This study was undertaken in an attempt to gain greater understanding of the factors which comprise a skilled performance in executing a ballistic movement. Although the specific movement chosen for the present analysis was the softball pitch, the general pattern of the segmental motions in this skill should be applicable to many similar skills. Four highly skilled subjects were filmed while performing the windmill pitch in softball. The filming was done using two cameras, a side view and a rear view. The film from the side view camera was analyzed in a single plane, and the relative motions of each of the segments of the pitching arm were calculated. The pitches were also performed while the subject pitched from a force plate, so that the recorded ground reaction forces could be compared to those calculated from film data. The film records of two of the pitches were synchronized and the digitized endpoints were read into a computer program which determined the spatial coordinates of each of the points of interest. The X, Y, and Z linear velocities of each of the segmental endpoints of the arm were calculated from these spatial coordinates. A method was also devised to calculate the angular velocities of each of the segments of the arm around their own principal axes.



These values were determined for the release frames of two of the pitches.

### CONCLUSIONS

On the basis of the present study, the following conclusions seem justified:

1. Highly skilled softball pitchers are often larger than the average person, and this greater size may afford some advantage in performance of this skill.
2. The velocity of the pitched ball at release is considerably greater than the velocity of the pitching hand, and the magnitude of this difference may be related to the skill of the pitcher.
3. The force platform provides an accurate record of the ground reaction forces being exerted by the pitcher during delivery of the ball.
4. The peak vertical ground reaction forces occur just prior to release of the ball, while the horizontal force peak occurs much earlier in the skill.
5. There is a definite sequence of segment motions which characterize the highly skilled performer in this activity.
6. The larger, more proximal segment reaches maximum velocity at the earliest point in the skill, followed by the next segment, and finally the most distal segment. This sequence is seen in many other ballistic sports' skills, and is likely a necessary characteristic pattern of skilled performance.
7. The proximal segment also attains peak acceleration



earliest in the skill, followed by the peak accelerations of the distal two segments which occur at almost the same instant. This pattern is also likely characteristic of skilled performances.

8. The vector representing resultant of the X and Y component accelerations for each of the segments has a direction approximately 90 degrees to that of the resultant velocity vectors.

9. The magnitude of the joint forces at each of the joints is greatest just prior to release of the ball, at the point of maximum acceleration of the segments.

10. The vector representing the resultant direction of the joint forces also has a direction approximately 90 degrees to that of the resultant velocity vectors.

11. The joint moment of greatest magnitude in this skill was that occurring when the upper arm segment was slowing down prior to release of the ball.

12. It is likely that the most forceful muscle contraction in this skill is that occurring during the deceleration of the arm segment.

13. The computer program used in this study to produce three-dimensional coordinates from two-camera film data is a valid instrument to produce these points.

14. The Z-component of the velocity for each of the segmental endpoints of the arm is not especially important in this skill, as it maintains a rather constant, low value throughout the skill.







15. For ballistic skills of this type in which the vast majority of the motion is occurring in the X-Y plane, it is not necessary to use three-dimensional analysis.

16. When the coordinates of three non-collinear points are available for a given body segment, it is possible to estimate the magnitudes of the angular velocities occurring around the principal axes of these segments.

17. The peak value for the angular velocity of the supination movement of the lower arm segment occurs at the same instant as the peak value for the elbow flexion velocity.

18. The movement of the lower arm segment occurring around the longitudinal axis is of considerable importance in contributing to the final velocity of this segment.

The following findings are included as practical conclusions for the teacher or coach of softball pitching:

1. An extremely long step from the rubber is characteristic of all highly skilled pitchers, both to ensure a maximal push-off from the board, and to improve accuracy by flattening the arc of the hand.

2. An important coordination pattern to develop in the windmill pitch is the simultaneous motion of the stepping leg and the pitching arm at the beginning of this pitch.

3. This motion must be accompanied by a rotation of the whole body sideways toward the pitching arm, which places the body in a more advantageous position for the subsequent rotation towards the pitch.



4. The non-pivot foot must be placed in a position with the toe pointing directly towards the pitching plate, as any position with this toe pointing to the right causes a loss of medial rotation of the body around the left hip.
5. The pitching arm must be kept extended throughout the circular backswing motion, as the linear velocity is maximized at the end of a longer lever.
6. From the top of the backswing motion, the upper arm segment must be accelerated as forcefully and rapidly as possible. For this reason, the pitcher must have very strong shoulder flexors (pectoralis major, teres major, latissimus dorsi) and adductors.
7. The next important movement which occurs in the pitch is the rapid deceleration, or slowing down of the arm segment prior to release of the ball. This is an extremely critical movement, and the pitcher must have very strong shoulder extensors (posterior deltoid, rotator cuff muscles) to execute this effectively.
8. Another important force-producing movement in the pitch is the rotation of the arm segments medially. These movements include medial rotation of the arm segment at the shoulder joint, and pronation of the forearm segment just prior to release of the ball.
9. It is recommended that pitchers work on specific strengthening exercises for these rotation movements, rather than on the movements of wrist and elbow flexion which are of relatively minor importance in this skill.



10. The ability of the pitcher to impart maximum velocity to the ball at release (the effectiveness of the release of the ball), is likely dependent upon the strength of the athlete, and on the angular velocity of the pronation movement at release.

#### Recommendations

1. That a further study be attempted in which the films from each camera are exactly synchronized, so that the accuracy of the spatial coordinates may be improved.
2. That a further study be conducted to examine more closely the rotations occurring in each arm segment during the pitch.





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APPENDIX A  
Filming Data





## Filming Data

Date: February 25, 1978.

Location: Dance Gymnasium, University of Alberta

## Camera Placement:

Camera 1: 50 feet 9 inches from center of force platform

Camera 2: 40 feet 0 inches to the rear of the force platform

## Camera Settings:

Frame Rate: 100 fps

Shutter Angle: 30 degrees

Exposure Time: .0008333 sec

f/stop: 4.0

Light Reading: 12 din

Artificial Lights: 6-1200 watt television lights and overhead dance lights

Background: Black curtain

Film: Kodak Ektachrome 7240 ASA 125



## APPENDIX B

### Three Dimensional Program Description



### 3-D PROGRAM DESCRIPTION

#### INTRODUCTION

Continuous improvement of instrumentation and technical procedures is a general and basic characteristic in all experimental sciences. A review of the last decade proves this to be true for cinematographical movement analysis in biomechanical research: from planar or two-dimensional filming to the first threedimensional recording systems with cameras aligned along the axes of an orthogonal Cartesian reference frame (Noble & Kelly, 1969; Duquet, Borms and Hebbelinck, 1973; Miller, 1973) and further to more sophisticated techniques with camera set-ups free from positional restrictions except for optical axes intersection (Bergeman, 1974; Van Gheluwe, 1974).

In a recent study (Penrose, Wood and Blanksby, 1976) it is even no longer necessary for the optical axes to intersect one another, although a theodolite is required in order to get precise spatial information of cameras and reference points.

This paper presents a further refinement in the area of threedimensional cinematography. The camera set-up is completely free of any geometrical or spatial restriction (optical axes intersection is not required). The use of a theodolite or other alignment or measuring tool is absolutely unnecessary as the external parameters (defining the spatial position and orientation of the cameras) are automatically calculated by the computer. Knowledge of intrinsic parameters, such as focal length,





film format etc... is not required either.

All these features make threedimensional filming so flexible that it can be used in game- or competitive-like situations with relative ease of operation and without tedious and time consuming preparations.

## METHOD

The basic principle of this system relies on the implicit mathematical reconstruction of the position of the cameras in space using the known life size coordinates and the image coordinates of certain reference points. These are located on a steel three-axial reference frame (fig. 1) which coincides with the mathematical coordinate system defining the objects space (= space where the real movement is described analytically by its X, Y and Z coordinates).

With the foregoing information about position and orientation of the cameras it is possible to calculate the X, Y and Z coordinates of any arbitrary point in space, provided its image coordinates are known.

### Theoretical basis of the method.

The mathematical theory underlying the method is basically the same as described by the author in a preceding publication (Van Gheluwe, 1974).

Defining an orthogonal coordinate system (O, X, Y, Z) in space, the motion of any arbitrary point can be described analytically by its spatial coordinates X, Y and Z (fig. 2) <sup>(a)</sup>.

Using matrix calculus and analytical geometry, it is possible to derive



a set of four linear equations expressing a relationship between the life size X, Y and Z coordinates of an arbitrary point in space and its known image coordinates  $(x_1, y_1)$  and  $(x_2, y_2)$  :

$$\begin{aligned}
 (n_{11} - x_1 n_{31}) X + (n_{12} - x_1 n_{32}) Y + (n_{13} - x_1 n_{33}) Z + x_1 &= 0 \\
 (n_{21} - y_1 n_{31}) X + (n_{22} - y_1 n_{32}) Y + (n_{23} - y_1 n_{33}) Z + y_1 &= 0 \\
 (m_{11} - y_2 m_{31}) X + (m_{12} - x_2 m_{32}) Y + (m_{13} - x_2 m_{33}) Z + x_2 &= 0 \\
 (m_{21} - y_2 m_{31}) X + (m_{22} - y_2 m_{32}) Y + (m_{23} - y_2 m_{33}) Z + y_2 &= 0
 \end{aligned} \tag{1}$$

where  $n_{ij}$  and  $m_{ij}$  ( $i = 1, 2, 3; j = 1, 2, 3$ ) are matrix coefficients relating to the position and orientation of the cameras.

These coefficients are calculated at an earlier stage of the computing process using the same equations as above, with the help of the known spatial X, Y and Z coordinates of certain reference points.

Taking 21 of these points (7 on each axis of the steel reference frame), one can derive 6 sets of 14 linear equations. Solving them yields respectively  $n_{11}, n_{21}, n_{31}$  for the first set,  $n_{12}, n_{22}, n_{32}$  for the second, etc... till  $m_{13}, m_{23}, m_{33}$  for the last one.

Substituting them in the set of equations 1 above, makes it possible to solve these equations for the life size X, Y and Z coordinates of any arbitrary point in space.

All the mentioned sets of equations are overdefined (having more equations than unknown variables), especially the sets defining the matrix coefficients  $n_{ij}$  and  $m_{ij}$ , in order to assure the accuracy and the stability



of the results.

The solving technique for all these sets of equations relies on the application of iterative "least square fitting" methods.

#### Reliability of the method.

Several experiments proved the accuracy of the final X, Y and Z coordinates to depend strongly on the measuring precision of the operator collecting the image coordinates and on the resolution of the used x-y-reader. On the contrary, calculation errors, inherent in solving the set of equations using the "least square fitting", and the rounding errors during computation, were negligible.

The results of one particular test reconstructing 17 linear distances between knots of a grid located on a transparent cylinder, are shown in table 1<sup>(b)</sup>.

The largest deviation found in this test did not exceed .2 cm and the mean deviation fluctuated around .1 cm.

#### APPLICATIONS

The method described above can be used in all circumstances and for any purpose where threedimensional reconstruction is required.

It requires but three simple preparative actions before real filming can start:

1. set the cameras so as to obtain the correct pictures
2. put the steel reference frame somewhere in the field of vision of the





cameras

3. film this reference frame with both cameras and remove it afterwards if necessary.

Therefore this method is especially appropriate to field-work in game- or competition-like situations, where minimal interference from "outside people" is allowed and where speed and ease of operation are decisive factors whether threedimensional filming will be possible or not.

The method as described above was applied successfully in a study analysing different styles of long jumping and was also used in an indoor swimming pool for a comparative study of four different starts in swimming.

In another, medically oriented study, the spatial position of 120 electrodes all around a human torso had to be reconstructed. Not fewer than six cameras were positioned around the body in order to have each electrode recorded by at least two cameras.

## CONCLUSION

The threedimensional filming technique as presented above combines an unprecedented ease of operation with high reliability and accuracy of results. Therefore it is especially recommended for field-work in threedimensional movement recording.



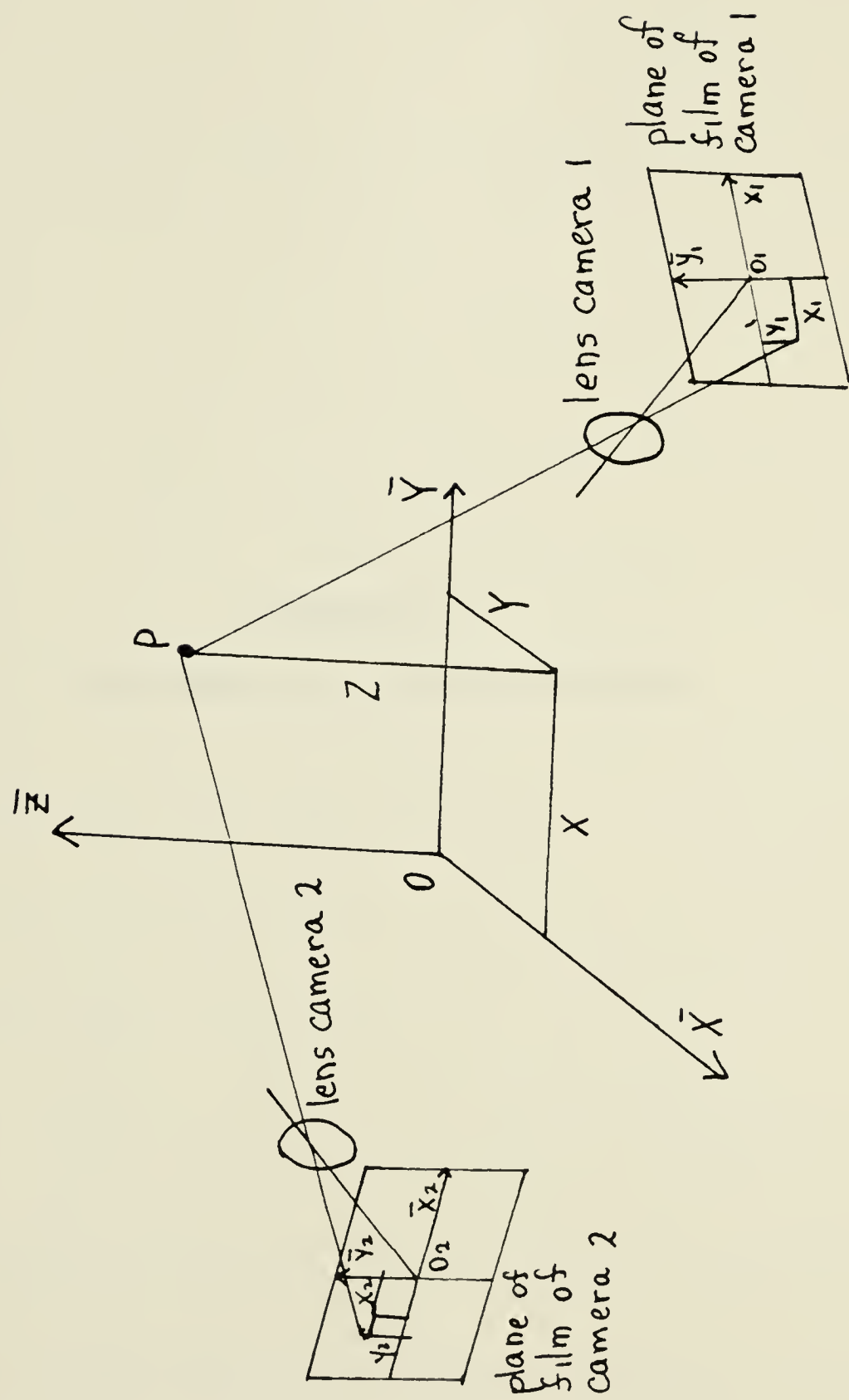


Figure 62. Position of Cameras in Space.



## APPENDIX C

## Equations for Planar Analysis





## KEY TO SYMBOLS

A - shoulder joint

B - elbow joint

C - wrist joint

D - fingertips

$G_1$  - center of gravity of the upper arm segment

$G_2$  - center of gravity of the lower arm segment

$G_3$  - center of gravity of the hand segment

$\overline{r}_1$  - position vector of the upper arm segment

$\overline{r}_2$  - position vector of the lower arm segment

$\overline{r}_3$  - position vector of the hand segment

1, 2, 3 - subscripts representing the upper, lower and hand segments of the upper extremity, respectively

$\theta_1$  - the angle of segment 1 with the right horizontal

$\theta_2$  - the angle of segment 2 with the right horizontal

$\theta_3$  - the angle of segment 3 with the right horizontal

x, y - subscripts representing vectors in the x and y directions

$S_{Ax}, S_{Ay}, S_{Bx}, S_{By}, S_{Cx}, S_{Cy}, S_{Dx}, S_{Dy}$  - the displacement vectors of the four segmental endpoints

$V_{Ax}, V_{Ay}, V_{Bx}, V_{By}, V_{Cx}, V_{Cy}, V_{Dx}, V_{Dy}$  - the velocity vectors of the four segmental endpoints

$A_{Ax}, A_{Ay}, A_{Bx}, A_{By}, A_{Cx}, A_{Cy}, A_{Dx}, A_{Dy}$  - the acceleration vectors of the four segmental endpoints

$\overline{W}_1, \overline{W}_2, \overline{W}_3$  - angular velocities of the three segments

$\overline{\alpha}_1, \overline{\alpha}_2, \overline{\alpha}_3$  - angular accelerations of the three segments

$M_1, M_2, M_3$  - masses of the three segments

$I_1, I_2, I_3$  - moments of inertia of each of the three segments around an axis through the center of gravity

$W_1, W_2, W_3$  - weights of each of the three segments



## CALCULATION OF GROUND REACTION FORCES

In the calculation of the ground reaction forces, the system is defined as the body of the subject. Rotation of the body may be neglected in the measurement of forces in this skill (Miller and Nelson, 1973: 54). The system may be represented as a particle (the mass center) with mass equal to that of the subject.

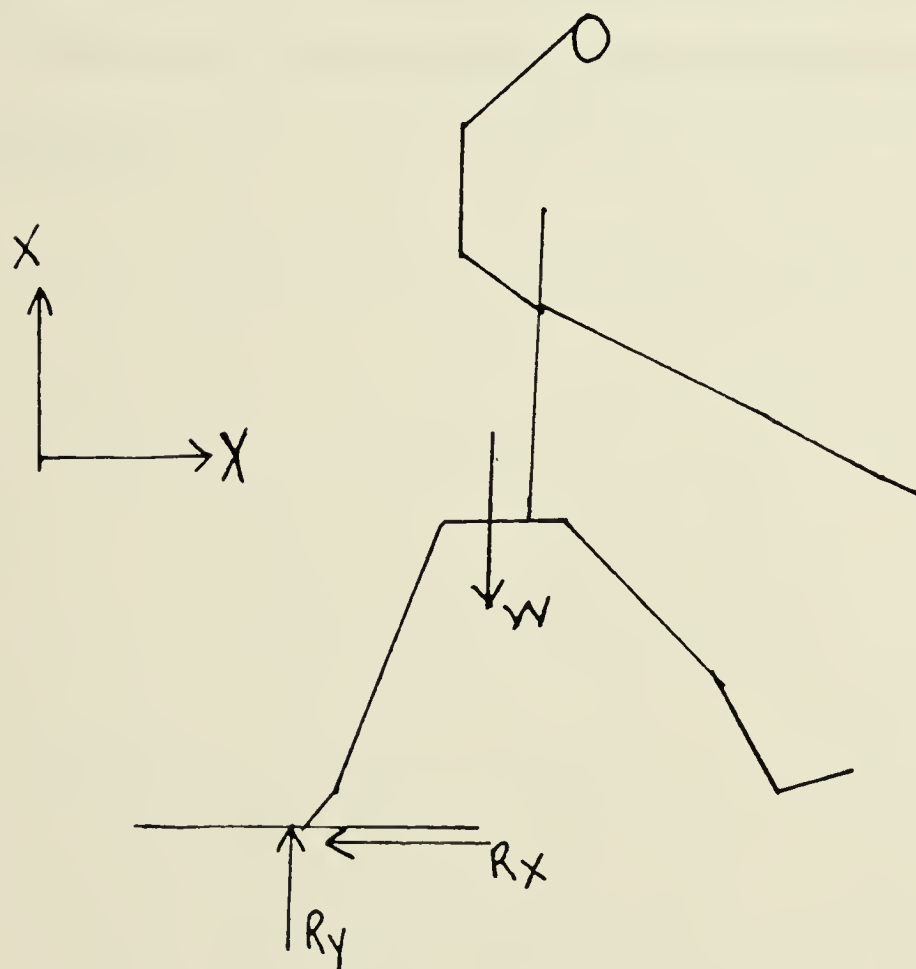


Figure 63. Free Body Diagram of the Softball Pitch

The free body diagram indicates that the body weight acts vertically downward from the mass center. The magnitudes of the forces at successive points during the takeoff were determined by application of Newton's second law of motion. The equations of motion may be ex-



pressed as: (Miller & Nelson, 1973: 55)

$$\sum F_x = M_{ax}$$

$$\sum F_y = M_{ay}$$

$$R_x = M_{ax}$$

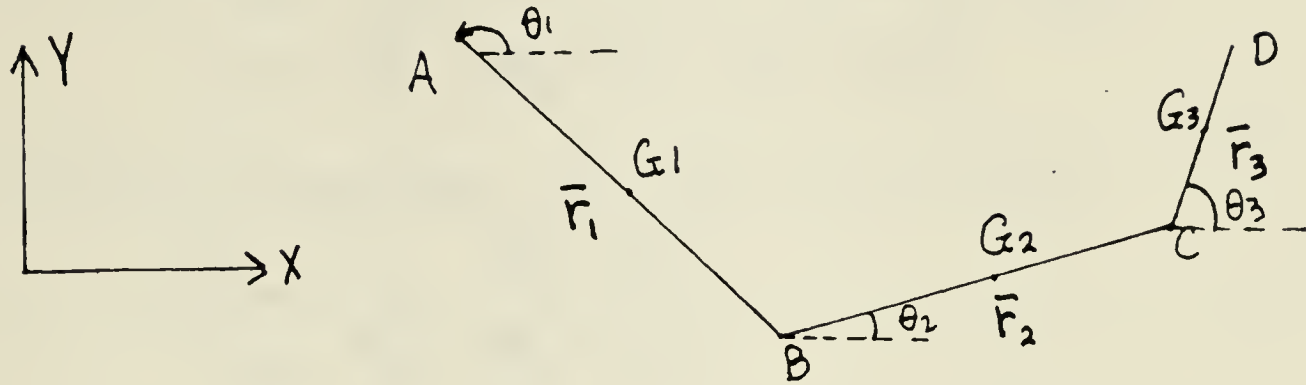
$$R_y = M_{ay} + W$$

The application of these equations to the forces exerted by the pitcher at successive points during the pitch was accomplished by a computer program written by the author. The  $R_x$  and  $R_y$  reaction forces were then displayed against time to illustrate the magnitudes and directions of such forces. These calculated body reaction forces were then compared to the tracings from a force plate from which the subject pitched the ball.





## KINEMATICS OF THE UPPER EXTREMITY MODEL



1. Let  $S_A$  be the absolute linear displacement of point A, which represents the shoulder joint. Then  $S_A$  may be divided into two components, in the X and Y directions; and each of these positions may be plotted against time to produce a displacement-time curve. This curve may then be differentiated once to produce velocity in the X (or Y) direction; and twice to produce acceleration in the X (or Y) direction.
2. To find  $\bar{V}_B$  (elbow joint):  $\bar{V}_B = \bar{V}_A + \bar{W}_1 \times \bar{r}_1$   
or  $\bar{V}_{Bx} = \bar{V}_{Ax} + (\bar{W}_1 \times \bar{r}_1)_x$   
 $\bar{V}_{By} = \bar{V}_{Ay} + (\bar{W}_1 \times \bar{r}_1)_y$
3. To find  $\bar{A}_B$  (elbow joint):  $\bar{A}_B = \bar{A}_A + \bar{\alpha}_1 \times \bar{r}_1 + \bar{W}_1 \times (\bar{W}_1 \times \bar{r}_1)$   
or  $\bar{A}_{Bx} = \bar{A}_{Ax} + (\bar{\alpha}_1 \times \bar{r}_1)_x + \bar{W}_1 \times (\bar{W}_1 \times \bar{r}_1)_x$   
 $\bar{A}_{By} = \bar{A}_{Ay} + (\bar{\alpha}_1 \times \bar{r}_1)_y + \bar{W}_1 \times (\bar{W}_1 \times \bar{r}_1)_y$
4. To find  $\bar{V}_C$  (wrist joint):  $\bar{V}_C = \bar{V}_B + \bar{W}_2 \times \bar{r}_2$   
or  $\bar{V}_{Cx} = \bar{V}_{Bx} + (\bar{W}_2 \times \bar{r}_2)_x$   
 $\bar{V}_{Cy} = \bar{V}_{By} + (\bar{W}_2 \times \bar{r}_2)_y$
5. To find  $\bar{A}_C$  (wrist joint):  $\bar{A}_C = \bar{A}_B + \bar{\alpha}_2 \times \bar{r}_2 + \bar{W}_2 \times (\bar{W}_2 \times \bar{r}_2)$



$$\begin{aligned}\underline{\text{or}} \quad \overline{A}_{Cx} &= \overline{A}_{Bx} + (\overline{\omega}_2 \times \overline{r}_2)_x + \overline{W}_2 \times (\overline{W}_2 \times \overline{r}_2)_x \\ \overline{A}_{Cy} &= \overline{A}_{By} + (\overline{\omega}_2 \times \overline{r}_2)_y + \overline{W}_2 \times (\overline{W}_2 \times \overline{r}_2)_y\end{aligned}$$

6. To find  $\overline{V}_D$  (fingertips):  $\overline{V}_D = \overline{V}_C + \overline{W}_3 \times \overline{r}_3$

$$\begin{aligned}\underline{\text{or}} \quad \overline{V}_{Dx} &= \overline{V}_{Cx} + (\overline{W}_3 \times \overline{r}_3)_x \\ \overline{V}_{Dy} &= \overline{V}_{Cy} + (\overline{W}_3 \times \overline{r}_3)_y\end{aligned}$$

7. To find  $\overline{A}_D$  (fingertips):  $\overline{A}_D = \overline{A}_C + \overline{\omega}_3 \times \overline{r}_3 + \overline{W}_3 \times (\overline{W}_3 \times \overline{r}_3)$

$$\begin{aligned}\underline{\text{or}} \quad \overline{A}_{Dx} &= \overline{A}_{Cx} + \overline{W}_3 \times \overline{r}_{3x} + \overline{W}_3 \times (\overline{W}_3 \times \overline{r}_3)_x \\ \overline{A}_{Dy} &= \overline{A}_{Cy} + \overline{W}_3 \times \overline{r}_{3y} + \overline{W}_3 \times (\overline{W}_3 \times \overline{r}_3)_y\end{aligned}$$

8. Using the above method, the Kinematics of the centers of gravity for each of the three segments were determined. The equations used were exactly the same as those listed above, except the magnitudes of the vectors  $r_1$ ,  $r_2$ ,  $r_3$  were altered to represent the distance to the C of G rather than the length of the segment.



## KINETICS OF UPPER EXTREMITY MODEL

The upper extremity model was represented by free body diagrams of each of the three segments. The segments were assumed to be connected by hinge joints and friction at the joints was assumed to be negligible. The net forces and moments of force at each joint we calculated from the equations of Newtonian rigid-body mechanics. The general equations of motion are as follows: (Meriam, 1974: 240)

$$\sum F_x = M \bar{a}_x$$

$$\sum F_y = M \bar{a}_y$$

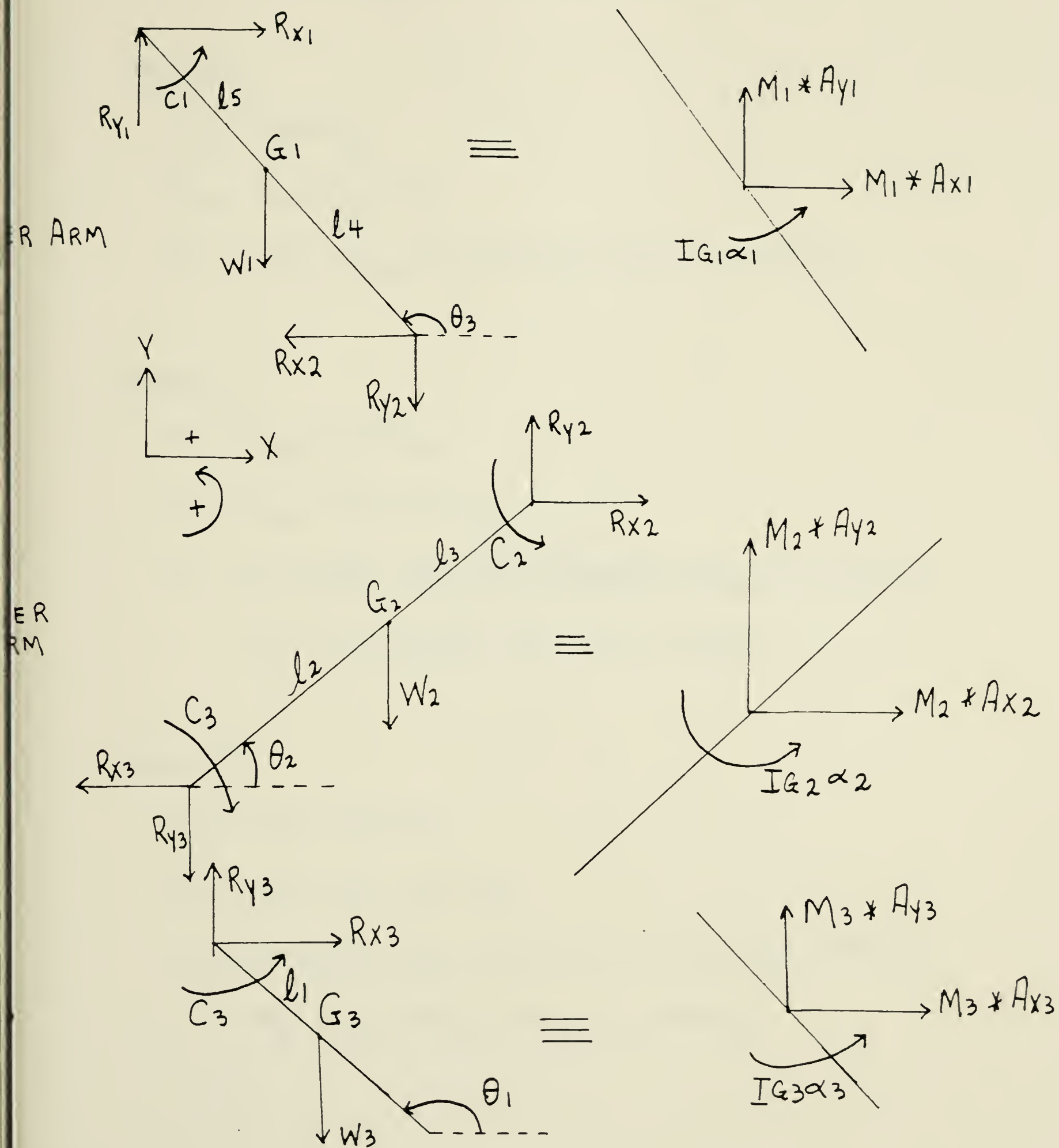
$$\sum M = I \bar{\alpha}$$

For each rigid body, the sum of the forces, either horizontal ( $F_x$ ) or vertical ( $F_y$ ) was equivalent to the product of the mass of the segment ( $M$ ) and the corresponding vertical or horizontal acceleration of the segment's center of mass. Similarly, the sum of the moments of force was equal to the product of the segment's angular acceleration and the appropriate mass moment of inertia ( $I$ ) at the segment's center of mass.





Kinetic Equations of Upper Extremity





Equations of Motion of These Segments

Segment 3:

$$R_{x3} = M_3 \times A_{x3}$$

$$R_{y3} = M_3 \times A_{y3} + W_3$$

$$C_3 = I_{G3} \alpha_3 + (R_{x3} \times l_3 \times \sin \theta_1) + (R_{y3} \times l_3 \times \cos \theta_1)$$

Segment 2:

$$R_{x2} = R_{x3} + M_2 \times A_{x2}$$

$$R_{y2} = R_{y3} + W_2 + M_2 \times A_{y2}$$

$$C_2 = C_3 + I_{G2} \alpha_2 - (R_{y2} \times l_3 \times \cos \theta_2) + (R_{x2} \times l_3 \times \sin \theta_2) - \\ (R_{y3} \times l_2 \times \cos \theta_2) + (R_{x3} \times l_2 \times \cos \theta_2)$$

Segment 1:

$$R_{x1} = R_{x2} + M_1 \times A_{x1}$$

$$R_{y1} = R_{y2} + W_1 + M_1 \times A_{y1}$$

$$C_1 = C_2 + I_{G1} \alpha_1 + (R_{x1} \times l_5 \times \sin \theta_3) + (R_{y1} \times l_5 \times \cos \theta_3) + \\ (R_{y2} \times l_4 \times \cos \theta_3) + (R_{x2} \times l_4 \times \sin \theta_3)$$



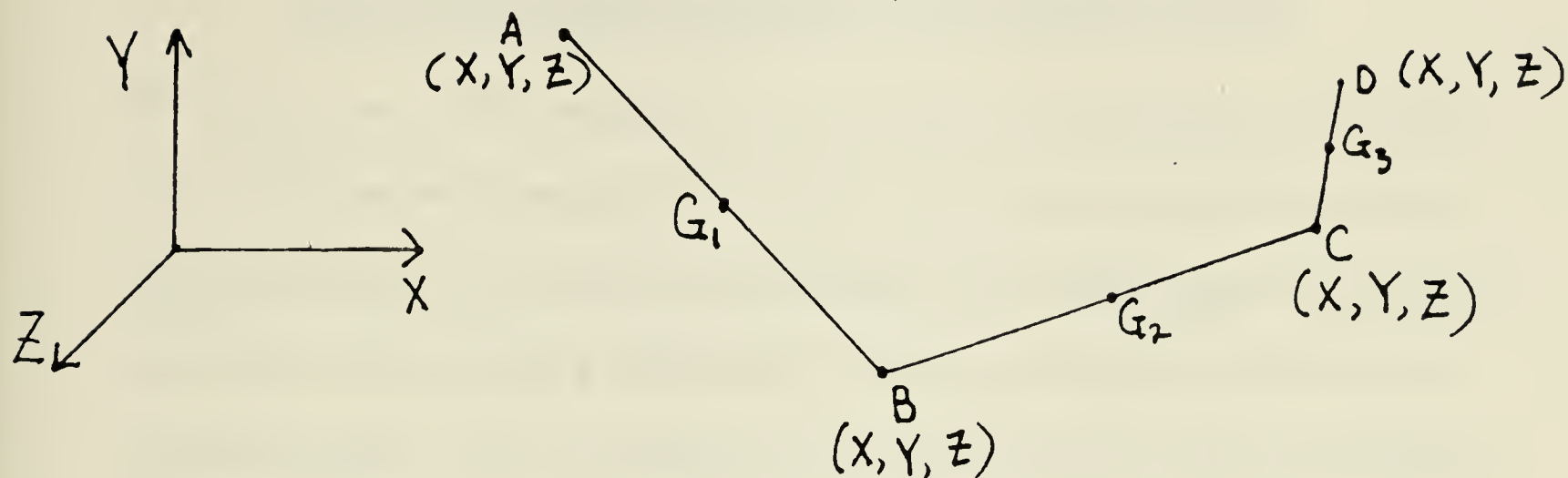
## APPENDIX D

## Equations for Three Dimensional Analyses





## SAMPLE SEGMENT CALCULATION-TWO PLANE



1. Let  $\bar{S}_A$  be the absolute linear displacement of point A over some time interval  $t$ . Then  $\bar{S}_A$  may be divided into three components, in the X, Y, and Z directions. Each of these positions over several time periods may be plotted against time to form a displacement-time curve. This curve may then be differentiated once to produce velocity in the X, Y, or Z direction; and twice to produce acceleration in the X, Y, or Z direction.
2. Let  $\bar{S}_B$  be the absolute linear displacement of point B (elbow joint) over some time interval  $t$ . From these displacements, the velocity and acceleration values may be determined in each of the 3 directions of interest.
3. This procedure may be continued for each of the segmental endpoints of interest.



# ANALYSIS OF FOREARM ROTATIONS IN THE SOFTBALL PITCH

The objective of this analysis is to describe the magnitude of the forearm rotations with respect to the three principal axes of the forearm. This analysis will be described in terms of the steps taken in calculating these values using a FORTRAN computer program written by the present author. This technique of analysis is based on the assumption that there are accurate X, Y, and Z coordinates available for three distinct, non-colinear points on the forearm segment. These points must be clearly visible in the film record from both cameras used in filming the subject.

Step 1: To determine the total angular velocity of the forearm segment with respect to reference frame R in the various time intervals of interest, the X, Y, and Z coordinates of three points must be known. When the X, Y, and Z coordinates of a point have been determined over a time interval, the velocity over that interval may be determined.  $v_1$  and  $v_2$  are the relative linear velocities of points C and E with respect to B.

$$\text{Since } \overline{v}_1 = \overline{W} \times \overline{r}_1$$

$$\text{and } \overline{v}_2 = \overline{W} \times \overline{r}_2$$

Where  $\overline{W}$  is the total angular velocity of the system, then the magnitude of  $\overline{W}$  may be calculated from:



$$\overline{W} = \frac{\overline{v}_1 \times \overline{v}_2}{\overline{v}_1 \cdot \overline{r}_2} = \frac{\overline{v}_2 \times \overline{v}_1}{\overline{v}_2 \cdot \overline{r}_1}$$

Step 2: To determine the vectors  $\overline{b}_1$  and  $\overline{b}_3$  defining the reference frame in the forearm segment, the cross product of  $\overline{c} \times \overline{d}$  must be formed.

Since  $\overline{b}_1$  is parallel to  $\overline{c} \times \overline{d}$ , then  $\overline{c} \times \overline{d}$  can be divided by its length to form the unit vector  $\overline{b}_1$ .

The vector  $\overline{b}_3$  may then be determined from  $\overline{b}_3 = \overline{b}_1 \times \overline{b}_2$ , since  $\overline{b}_2$  is defined by the forearm segmental endpoints. The three unit vectors defining the reference frame in the forearm segment are as follows:

$$\overline{b}_1 = b_{11} \overline{n}_1 + b_{12} \overline{n}_2 + b_{13} \overline{n}_3$$

$$\overline{b}_2 = b_{21} \overline{n}_1 + b_{22} \overline{n}_2 + b_{23} \overline{n}_3$$

$$\overline{b}_3 = b_{31} \overline{n}_1 + b_{32} \overline{n}_2 + b_{33} \overline{n}_3$$

Step 3: To determine the three components of the total rotation of the forearm (W) calculated in Step 1. The total rotation is

$$\overline{W} = W_1 \overline{n}_1 + W_2 \overline{n}_2 + W_3 \overline{n}_3$$

A system of three equations in three unknowns may be formed from the above known quantities. For the case of a general vector k, where

$$\overline{K} = k_1 \overline{n}_1 + k_2 \overline{n}_2 + k_3 \overline{n}_3, \text{ then}$$

$$\overline{W} \cdot \overline{K} = W_1 \overline{k}_1 + W_2 \overline{k}_2 + W_3 \overline{k}_3$$

To apply this general case to the unit vectors forming the reference frame in the arm (Q), we have:





$$\overline{W} \cdot \overline{b}_1 = W_1 b_{11} + W_2 b_{12} + W_3 b_{13}$$

$$\overline{W} \cdot \overline{b}_2 = W_1 b_{21} + W_2 b_{22} + W_3 b_{23}$$

$$\overline{W} \cdot \overline{b}_3 = W_1 b_{31} + W_2 b_{32} + W_3 b_{33}$$

Where the three unknown quantities are  $W_1$ ,  $W_2$ , and  $W_3$ . These symbols represent the following rotations:

$\overline{W}_1$  = flexion-extension at elbow joint

$\overline{W}_2$  = pronation-supination of the lower arm segment

$\overline{W}_3$  = abduction and adduction of the lower arm segment at the elbow joint.

The total rotation  $W$  in reference frame  $Q$  may be represented as:

$$\overline{W} = (\overline{W} \cdot \overline{b}_1) \overline{b}_1 + (\overline{W} \cdot \overline{b}_2) \overline{b}_2 + (\overline{W} \cdot \overline{b}_3) \overline{b}_3$$



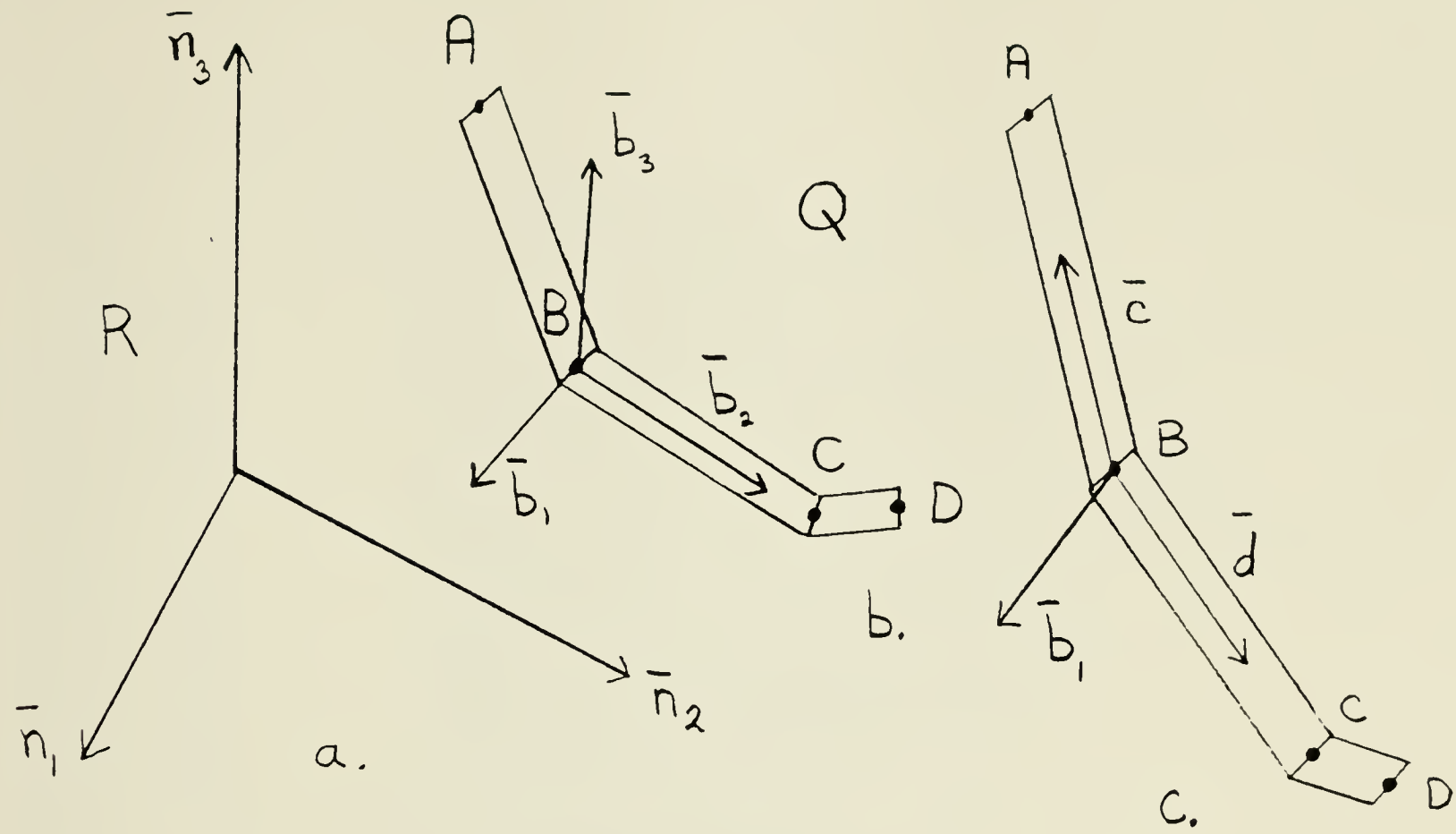


Figure 64. Reference frames of Arm Segments

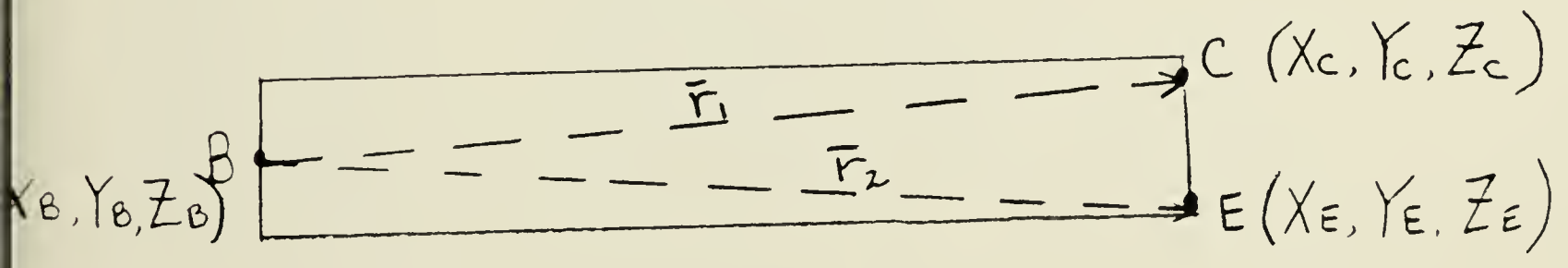


Figure 65. Points on Lower Arm Segment



## APPENDIX E

Computer Program for Segmental Analysis





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1.000      C THREE SEGMENT ANALYSIS PROGRAM
2.000      C WRITTEN BY MARION ALEXANDER, U OF ALBERTA, SPRING 1978
3.000      C PROGRAM WRITTEN TO ANALYZE THE KINETIC AND KINEMATIC
4.000      C MOTION PARAMETERS OF THE THREE SEGMENTS OF THE ARM
5.000      C DURING THE SKILL OF SOFTBALL PITCHING
6.000      0001      REAL X,P,DP,SP,Y,C,WK,LAL
7.000      0002      REAL M1,M3,M2,AG,IG1,IG2,IG3
8.000      0003      DIMENSION SHX(25),SHY(25),DS(25),YSI(25),YSY(25),CX(24,3),
9.000      $ CY(24,3),DUS(25),DISX(25),DISY(25),DDDS(25)
10.000     0004      DIMENSION VELX(25),VELY(25),ACCI(25),ACCY(25)
11.000     0005      DIMENSION ALPHA(20),ALPH(20),ALP(20),AL(20),ALPH2(20)
12.000     0006      DIMENSION ALPH8(20),ALPH9(20)
13.000     0007      DIMENSION ALPH3(20),ALPH4(20),ALPH5(20),ALPH6(20),ALPH7(20)
14.000     0008      DIMENSION RX1(25),RY1(25),RX2(25),RY2(25),RX3(25),RY3(25),
15.000     $ C1(25),C2(25),C3(25)
16.000     0009      DIMENSION X11G(25),YJ1G(25),XIAG(25),YJAG(25),X12G(25),YJ2G(25)
17.000     $ ,X1A2G(25),YJA2G(25),X13G(25),YJ3G(25),X1A3G(25),YJA3G(25)
18.000     0010      DIMENSION DISP(25),VEL(25),ACC(25),WK(2000)
19.000     0011      DIMENSION DISP2(25),VEL2(25),ACC2(25),DISP3(25)
20.000     0012      DIMENSION VEL3(25),ACC3(25)
21.000     0013      DIMENSION G(25),H(25),YY(25),YTY(25),XI(25),YJ(25)
22.000     0014      DIMENSION X1A(25),YJA(25),X12(25),YJ2(25),X1A2(25),YJA2(25)
23.000     0015      DIMENSION X13(25),YJ3(25),X1A3(25),YJA3(25)
24.000     0016      DIMENSION XII(25),YJJ(25),THETA(25)
25.000     0017      DIMENSION I(25),P(25),DP(25),Y(24),C(24,3)
26.000     0018      DIMENSION CC(24,3),CCC(24,3)
27.000     0019      IOU=6
28.000      C READ IN MASSES OF 3 SEGMENTS AND THEIR MOMENTS OF INERTIA
29.000     0020      READ(5,502)M1,M2,M3,IG1,IG2,IG3
30.000     0021      502      FORMAT(6F10.5)
31.000      C READ IN LENGTHS OF EACH OF THE SEGMENTS
32.000     0022      READ(5,502)UAL,LAL,HL
33.000     0023      503      FORMAT(3F10.5)
34.000     0024      AG=9.814
35.000     0025      SL1=UAL*.436
36.000     0026      SL2=LAL*.43
37.000     0027      SL3=HL*.28
38.000     0028      W1=M1*AG
39.000     0029      W2=M2*AG
40.000     0030      W3=M3*AG
41.000     0031      IZ=25
42.000     0032      IC=24
43.000     0033      SM=25.0
44.000     0034      READ(5,501)(ALPHA(I),I=1,20)
45.000     0035      501      FORMAT(20A4)
46.000     0036      READ(5,501)(ALP(I),I=1,20)
47.000     0037      READ(5,501)(AL(I),I=1,20)
48.000     0038      READ(5,501)(ALPH(I),I=1,20)
49.000     0039      READ(5,501)(ALPH2(I),I=1,20)
50.000     0040      READ(5,501)(ALPH3(I),I=1,20)
51.000     0041      READ(5,501)(ALPH4(I),I=1,20)
52.000     0042      READ(5,501)(ALPH5(I),I=1,20)
53.000     0043      READ(5,501)(ALPH6(I),I=1,20)
54.000     0044      READ(5,501)(ALPH7(I),I=1,20)
55.000     0045      NX=25

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56.000 0046      READ(5,501) (ALPHA(I),I=1,20)
57.000 0047      READ(5,501) (ALPHA(I),I=1,20)
58.000
59.000      C READ IN THE DEGREE OF SMOOTHING TO OCCUR IN THE SPLINE ROUTINE
60.000      C WHERE PP IS THE DEGREE OF SMOOTHING FOR THE UPPER ARM SEGMENT
61.000      C AND DSZ IS THE DEGREE OF SMOOTHING FOR THE LOWER ARM SEGMENT
62.000      C AND DSS IS THE DEGREE OF SMOOTHING FOR THE SEG ENDPOINTS
63.000      C AND DSY IS THE DEGREE OF SMOOTHING FOR THE HAND SEGMENT
64.000 0048      READ(5,51) PP,DSS,DSY,DSZ
65.000 0049      51      FORMAT(4P10.5)
66.000      C READ IN THE MINIMUM VALUES OF PARAMETERS TO BE GRAPHED
67.000      C WHERE DY3 IS THE MINIMUM ANG DISPL OF HAND
68.000      C AND DY2 IS THE MIN ANG DISPL OF THE LOWER ARM
69.000      C AND DY1 IS THE MIN ANG DISPL OF THE UPPER ARM
70.000      C WHERE A3 IS THE MINIMUM ANG ACCEL OF THE HAND
71.000      C AND A2 IS THE MIN ANG ACCEL OF THE LOWER ARM
72.000      C AND A1 IS THE MIN ANG ACCEL OF THE UPPER ARM
73.000 0050      READ(5,561) DY3,DY2,DY1,A3,A2,A1
74.000 0051      561      FORMAT(6P10.5)
75.000      C READ IN THE LINEAR KINEMATIC PARAMETERS TO BE GRAPHED
76.000      C WHERE VPX IS THE MINIMUM X-VEL OF THE FINGERS
77.000      C AND VPY IS THE MIN Y-VEL OF THE FINGERS
78.000      C AND APX IS THE MIN X-ACCEL OF THE FINGERS
79.000      C AND APY IS THE MIN Y-ACCEL OF THE FINGERS
80.000 0052      READ(5,562) VPX,VPY,APX,APY
81.000 0053      562      FORMAT(4P10.4)
82.000 0054      READ(5,562) RPX,RPY,CM1,CM2
83.000      C AND THEN READ IN THE KINETIC PARAMETERS TO BE GRAPHED
84.000      C WHERE RPX IS THE MINIMUM X-FORCE AT SHOULDER
85.000      C AND RPY IS THE MINIMUM Y-FORCE AT SHOULDER
86.000      C AND CM1 IS THE MINIMUM TIME FOR THE MOMENT CURVES
87.000      C AND CM2 IS THE MIN VALUE FOR THE SHOULDER MOMENT
88.000 0055      RAD=57.29577
89.000 0056      DO 2 I=1,NX
90.000 0057      READ(5,3) X(I),P(I),G(I),H(I),SHX(I),SBY(I)
91.000 0058      3      FORMAT(6P10.5)
92.000 0059      DP(I)=PP
93.000 0060      DS(I)=DSS
94.000 0061      DDS(I)=DSY
95.000 0062      DDDS(I)=DSZ
96.000      C CHANGE DISPLACEMENTS IN DEGREES TO RADIANS
97.000 0063      P(I)=P(I)/RAD
98.000 0064      G(I)=G(I)/RAD
99.000 0065      H(I)=H(I)/RAD
100.000 0066      2      CONTINUE
101.000 0067      M=NX-1
102.000 0068      CALL ICSSCU(X,SHX,DS,NX,SP,YSX,CX,IC,WK,IER)
103.000 0069      CALL ICSSCU(X,SHY,DS,NX,SM,YSY,CY,IC,WK,IER)
104.000 0070      CALL ICSSCU(X,P,DP,NX,SP,Y,C,IC,WK,IER)
105.000 0071      CALL ICSSCU(X,G,DDS,NX,SP,Y,CC,IC,WK,IER)
106.000 0072      CALL ICSSCU(X,H,DDS,NX,SP,YYY,CCC,IC,WK,IER)
107.000 0073      DO 4 I=1,M
108.000 0074      DISX(I)=YSX(I)
109.000 0075      DISY(I)=YSY(I)
110.000 0076      VELX(I)=CX(I,1)
111.000 0077      VPLY(I)=CY(I,1)

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97.000 0078      ACCX(I)=2.*CX(I,2)
98.000 0079      ACCY(I)=2.*CY(I,2)
99.000 0080      DISP(I)=Y(I)
100.000 0081     DISP2(I)=YY(I)
101.000 0082     VEL2(I)=CC(I,1)
102.000 0083     ACC2(I)=2.*CC(I,2)
103.000 0084     DISP3(I)=YYY(I)
104.000 0085     VEL3(I)=CCC(I,1)
105.000 0086     ACC3(I)=2.*CCC(I,2)
106.000 0087     VEL(I)=C(I,1)
107.000 0088     ACC(I)=2.*C(I,2)
108.000 0089      4      CONTINUE
109.000 0090      WRITE(6,15)
110.000 0091      15      FORMAT('1',30X,'SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS')
111.000 0092      WRITE(6,555)
112.000 0093      555     FORMAT('1',30X,'ANGULAR KINEMATICS OF THE UPPER ARM')
113.000 0094      WRITE(6,6)
114.000 0095      6      FORMAT('0',10X,'INPUT',50X,'OUTPUT')
115.000 0096      WRITE(6,7)
116.000 0097      7      FORMAT('0',5X,'X',10X,'P',10X,'TIMP',8X,'DISPLACEMENT',
117.000          *8X,'VELOCITY',8X,'ACCELERATION')
118.000 0098      DO 8 I=1,N
119.000 0099      8      WRITE(6,9) X(I),P(I),X(I),DISP(I),VEL(I),ACC(I)
120.000 0100      WRITE(6,500) (ALPH7(I),I=1,20)
121.000 0101      500     FORMAT(/,20A4)
122.000 0102      WRITE(6,15)
123.000 0103      WRITE(6,556)
124.000 0104      556     FORMAT('1',30X,'ANGULAR KINEMATICS OF THE LOWER ARM')
125.000 0105      WRITE(6,6)
126.000 0106      WRITE(6,7)
127.000 0107      DO 13 I=1,N
128.000 0108      13      WRITE(6,9) X(I),G(I),X(I),DISP2(I),VEL2(I),ACC2(I)
129.000 0109      WRITE(6,500) (ALPH7(I),I=1,20)
130.000 0110      WRITE(6,15)
131.000 0111      WRITE(6,557)
132.000 0112      557     FORMAT('1',30X,'ANGULAR KINEMATICS OF THE HAND SEGMENT')
133.000 0113      WRITE(6,6)
134.000 0114      WRITE(6,7)
135.000 0115      DO 14 I=1,N
136.000 0116      14      WRITE(6,9) X(I),H(I),X(I),DISP3(I),VEL3(I),ACC3(I)
137.000 0117      WRITE(6,500) (ALPH7(I),I=1,20)
138.000 0118      WRITE(6,666)
139.000 0119      666     FORMAT('1',30X,'LINEAR KINEMATICS OF SHOULDER')
140.000 0120      WRITE(6,6)
141.000 0121      WRITE(6,7)
142.000 0122      9      FORMAT(3X,F5.3,5X,F7.3,6X,F5.3,3(6X,F12.4))
143.000 0123      WRITE(6,558)
144.000 0124      558     FORMAT('0',30X,'X-COORDINATES OF SHOULDER')
145.000 0125      DO 18 I=1,N
146.000 0126      18      WRITE(6,9) X(I),SHX(I),X(I),DISX(I),VELX(I),ACCX(I)
147.000 0127      WRITE(6,500) (ALPH7(I),I=1,20)
147.200 0128      WRITE(6,666)
147.400 0129      WRITE(6,6)
147.600 0130      WRITE(6,7)
148.000 0131      WRITE(6,559)

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149.000 0132 559 FORMAT('0',30X,'Y-COORDINATES OF SHOULDER')
150.000 0133 DO 19 I=1,M
151.000 0134 19 WRITE(6,9)X(I),SHY(I),X(I),DISY(I),VELY(I),ACCY(I)
152.000 0135 WRITE(6,500)(ALPH7(I),I=1,20)
153.000 C CALCULATE LINEAR VELOCITIES
154.000 C INSERT TRUE LENGTHS OF LIMB SEGMENTS
155.000 C VA IS LINEAR VEL OF SHOULDER JOINT
156.000 C VB IS LINEAR VEL OF ELBOW JOINT
157.000 C VC IS LINEAR VEL OF WRIST
158.000 C VD IS LINEAR VEL OF FINGERTIPS
159.000 C VECTOR NOTATION FOR THE THREE VECTORS IS XI,YJ,ZK
160.000 0136 WRITE(6,24)
161.000 0137 24 FORMAT('1',15X,'LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL
161.200 3 ENDOPOINTS')
162.000 0138 WRITE(6,25)
163.000 0139 25 FORMAT('/',40X,'ELBOW KINEMATICS',//)
164.000 0140 WRITE(6,23)
165.000 0141 23 FORMAT(' FRAME',4X,'X-VELOCITY',10X,'Y-VELOCITY',10X,
166.000 6*X-ACCELERATION',6X,'Y-ACCELERATION')
167.000 C CALCULATE VELOCITY AND ACCELERATION COMPONENTS OF THE ELBOW
168.000 0142 CALL VECTOR(DISP,UAL,XI,YJ)
169.000 0143 DO 5 I=1,M
170.000 0144 XII(I)=VEL(I)*(-YJ(I))+VELX(I)
171.000 0145 YJJ(I)=VEL(I)*(XI(I))+VELY(I)
172.000 0146 XIA(I)=(ACC(I)*(-YJ(I)))+(VEL(I)*(-YJJ(I)))+ACCY(I)
173.000 0147 YJA(I)=(ACC(I)*XI(I))+(VEL(I)*XII(I))+ACCY(I)
174.000 0148 WRITE(6,27)I,XII(I),YJJ(I),XIA(I),YJA(I)
175.000 0149 5 CONTINUE
176.000 0150 WRITE(6,500)(ALPH7(I),I=1,20)
177.000 C CALCULATE VELOCITY AND ACCELERATION COMPONENTS OF THE ARM COFG
178.000 0151 WRITE(6,24)
179.000 0152 WRITE(6,56)
180.000 0153 56 FORMAT('-',30X,'KINEMATICS OF THE ARM CENTER OF GRAVITY',//)
181.000 0154 WRITE(6,23)
182.000 0155 CALL VECTOR(DISP,SL1,XI,YJ)
183.000 0156 DO 55 I=1,M
184.000 0157 XIIG(I)=VEL(I)*(-YJ(I))+VELX(I)
185.000 0158 YJIG(I)=VEL(I)*(XI(I))+VELY(I)
186.000 0159 XIAG(I)=(ACC(I)*(-YJ(I)))+(VEL(I)*(-YJIG(I)))+ACCY(I)
187.000 0160 YJAG(I)=(ACC(I)*XI(I))+(VEL(I)*XIIG(I))+ACCY(I)
188.000 0161 WRITE(6,27)I,XIIG(I),YJIG(I),XIAG(I),YJAG(I)
189.000 0162 55 CONTINUE
190.000 0163 WRITE(6,500)(ALPH7(I),I=1,20)
191.000 0164 27 FORMAT(15,5X,3(F10.4,10X),F10.4)
192.000 C CALCULATE VELOCITY AND ACCELERATION COMPONENTS OF THE WRIST
193.000 0165 WRITE(6,24)
194.000 0166 WRITE(6,28)
195.000 0167 28 FORMAT('-',40X,'WRIST KINEMATICS',//)
196.000 0168 WRITE(6,23)
197.000 0169 CALL VECTOR(DISP2,LAL,XI,YJ)
198.000 0170 DO 43 I=1,M
199.000 0171 X12(I)=VEL2(I)*(-YJ(I))+X11(I)
200.000 0172 YJ2(I)=VEL2(I)*(XI(I))+YJ1(I)
201.000 0173 X1A2(I)=(ACC2(I)*(-YJ(I)))+(VEL2(I)*(-YJ2(I)))+X1A(I)
202.000 0174 YJ2(I)=(ACC2(I)*XI(I))+(VEL2(I)*X12(I))+YJ1(I)

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203.000 0175      WRITE(6,27) I,XI2(I),YJ2(I),XIA2(I),YJA2(I)
205.000 0176      43      CONTINUE
205.500 0177      WRITE(6,500) (ALPH7(I),I=1,20)
206.000      C CALCULATE VELOCITY AND ACCELERATION COMPONENTS OF THE L ARM COPG
207.000 0178      WRITE(6,24)
208.000 0179      WRITE(6,92)
209.000 0180      92      FORMAT('=',30X,'KINEMATICS OF THE LOWER ARM CENTER OF GRAVITY',//)
210.000 0181      WRITE(6,23)
211.000 0182      CALL VECTOR(DISP2,SL2,XI,YJ)
212.000 0183      DO 96 I=1,M
213.000 0184      XI2G(I)=VEL2(I)*(-YJ(I))+XII(I)
214.000 0185      YJ2G(I)=VEL2(I)*(XI(I))+YJJ(I)
215.000 0186      XIA2G(I)=(ACC2(I)*(-YJ(I)))+(VEL2(I)*(-YJ2(I)))+XIA(I)
216.000 0187      YJA2G(I)=(ACC2(I)*XI(I))+(VEL2(I)*XI2(I))+YJA(I)
217.000 0188      WRITE(6,27) I,XI2G(I),YJ2G(I),XIA2G(I),YJA2G(I)
219.000 0189      96      CONTINUE
219.500 0190      WRITE(6,500) (ALPH7(I),I=1,20)
220.000      C CALCULATE VELOCITY AND ACCEL OF FINGERTIPS--VD
221.000 0191      WRITE(6,24)
222.000 0192      CALL VECTOR(DISP3,HL,XI,YJ)
223.000 0193      WRITE(6,29)
224.000 0194      29      FORMAT('=',40X,'FINGERTIP KINEMATICS',//)
225.000 0195      WRITE(6,23)
226.000 0196      DO 44 I=1,M
227.000 0197      XI3(I)=(VEL3(I)*(-YJ(I)))+XII(I)
228.000 0198      YJ3(I)=(VEL3(I)*(XI(I)))+YJJ(I)
229.000 0199      XIA3(I)=(ACC3(I)*(-YJ(I)))+(VEL3(I)*(-YJ3(I)))+XIA2(I)
230.000 0200      YJA3(I)=(ACC3(I)*XI(I))+(VEL3(I)*XI3(I))+YJA2(I)
231.000 0201      WRITE(6,27) I,XI3(I),YJ3(I),XIA3(I),YJA3(I)
233.000 0202      44      CONTINUE
233.500 0203      WRITE(6,500) (ALPH7(I),I=1,20)
234.000      C CALCULATION OF THE HAND COPG KINEMATICS
235.000 0204      WRITE(6,24)
236.000 0205      WRITE(6,99)
237.000 0206      99      FORMAT('=',30X,'KINEMATICS OF THE HAND CENTER OF GRAVITY',//)
238.000 0207      WRITE(6,23)
239.000 0208      CALL VECTOR(DISP3,SL3,XI,YJ)
240.000 0209      DO 98 I=1,M
241.000 0210      XI3G(I)=(VEL3(I)*(-YJ(I)))+XII(I)
242.000 0211      YJ3G(I)=(VEL3(I)*(XI(I)))+YJJ(I)
243.000 0212      XIA3G(I)=(ACC3(I)*(-YJ(I)))+(VEL3(I)*(-YJ3(I)))+XIA2(I)
244.000 0213      YJA3G(I)=(ACC3(I)*XI(I))+(VEL3(I)*XI3(I))+YJA2(I)
245.000 0214      WRITE(6,27) I,XI3G(I),YJ3G(I),XIA3G(I),YJA3G(I)
247.000 0215      98      CONTINUE
247.500 0216      WRITE(6,500) (ALPH7(I),I=1,20)
248.000      C CALCULATION OF THE JOINT FORCES AND MOMENTS FOR EACH PRAGE
249.000 0217      DO 90 I=1,M
250.000      C CALCULATIONS FOR SEGMENT 3--THE HAND
251.000 0218      RX3(I)=F3*XIA3G(I)
252.000 0219      RY3(I)=F3*YJA3G(I)
253.000 0220      CJ(I)=IG3*ACC3(I)+RX3(I)*SL3*SIN(DISP3(I))+RY3(I)*SL3*
254.000      3 COS(DISP3(I))
255.000      C CALCULATIONS FOR SEGMENT 2=THE LOWER ARM SEGMENT
256.000 0221      RX2(I)=RX3(I)+F2*XIA2G(I)
257.000 0222      RY2(I)=RY3(I)+F2*YJA2G(I)

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258.000 0223      C2(I)=IG2*ACC2(I)+(RX2(I)*S2*SIN(DISP2(I)))-(RY2(I)*S2*
259.000          $ COS(DISP2(I)))
260.000          $ *C3(I)+(RX3(I)*(LAL-S2)*SIN(DISP2(I)))-(RY3(I)*(LAL-S2)*
261.000          $ COS(DISP2(I)))
262.000      C CALCULATIONS FOR SEGMENT 1--THE UPPER ARM SEGMENT
263.000 0224      RX1(I)=RX2(I)+L1*YIAG(I)
264.000 0225      RY1(I)=RY2(I)+L1*YJAG(I)
265.000 0226      C1(I)=C2(I)+IG1*ACC(I)+(RX2(I)*(UAL-SL1)*SIN(DISP(I)))+(
266.000          $ (RY2(I)*(UAL-SL1)*
267.000          $ COS(DISP(I)))+(RX1(I)*SL1*SIN(DISP(I)))+(RY1(I)*SL1*COS(DISP(I)))
268.000 0227      90      CONTINUE
269.000 0228      WRITE(6,61)
270.000 0229      81      FORMAT('1',20X,'KINETICS OF THE UPPER EXTREMITY'//)
271.000 0230      WRITE(6,85)
272.000 0231      85      FORMAT(20X,'FORCES AND MOMENTS AT THE WRIST JOINT'//)
273.000 0232      WRITE(6,84)
274.000 0233      84      FORMAT(2X,'PRAMP',3X,'X-JOINT FORCES',3X,'Y-JOINT FORCES',
275.000          $ 5X,'MOMENT AT THE JOINT')
276.000 0234      DO 82 I=1,M
277.000 0235      82      WRITE(6,83) I, RX3(I), RY3(I), C3(I)
278.000 0236      WRITE(6,500) (ALPH7(I), I=1,20)
279.000 0237      83      FORMAT(15,3(5X,P15.5))
280.000 0238      WRITE(6,81)
281.000 0239      WRITE(6,88)
282.000 0240      88      FORMAT('-',20X,'FORCES AND MOMENTS AT THE ELBOW JOINT'//)
283.000 0241      WRITE(6,64)
284.000 0242      DO 86 I=1,M
285.000 0243      86      WRITE(6,83) I, RX2(I), RY2(I), C2(I)
286.000 0244      WRITE(6,500) (ALPH7(I), I=1,20)
287.000 0245      WRITE(6,61)
288.000 0246      WRITE(6,89)
289.000 0247      89      FORMAT('-',20X,'FORCES AND MOMENTS AT THE SHOULDER JOINT'//)
290.000 0248      WRITE(6,84)
291.000 0249      DO 87 I=1,M
292.000 0250      87      WRITE(6,83) I, RX1(I), RY1(I), C1(I)
293.000 0251      WRITE(6,500) (ALPH7(I), I=1,20)
294.000 0252      WRITE(6,560)
295.000 0253      560      FORMAT('1')
296.000      C      CALL CGPEP1 (1.0,1.0)
297.000      C GRAPHS OF X AND Y LINEAR VELOCITIES VS. TIME
298.000      C FOR THE FOUR SEGMENTAL ENDPOINTS OF THE ARM
299.000 0254      CALL CGPL(X,XI3,X,M,1,1,1,3,2,0.,-9.9,4.0,VFX,
300.000          $ -9.9,4.0,ALPH9,IOU)
301.000 0255      CALL CGPL(X,YJ3,X,M,2,1,1,3,2,0.,-9.9,4.0,VFY,
302.000          $ -9.9,4.0,ALPH9,IOU)
303.000 0256      CALL CGPL(X,XI2,X,M,1,1,1,3,2,0.,-9.9,4.0,VFX,
304.000          $ -9.9,4.0,ALPH8,IOU)
305.000 0257      CALL CGPL(X,YJ2,X,M,2,1,1,3,2,0.,-9.9,4.0,VFY,
306.000          $ -9.9,4.0,ALPH8,IOU)
307.000 0258      CALL CGPL(X,XI1,X,M,1,1,1,3,2,0.,-9.9,4.0,VFX,
308.000          $ -9.9,4.0,ALPH5,IOU)
309.000 0259      CALL CGPL(X,YJ1,X,M,2,1,1,3,2,0.,-9.9,4.0,VFY,
310.000          $ -9.9,4.0,ALPH5,IOU)
311.000 0260      CALL CGPL(X,VELX,X,M,1,1,1,3,2,0.,-9.9,4.0,VFX,
312.000          $ -9.9,4.0,ALPH4,IOU)

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313.000 0261      CALL CGPL(X,VELY,X,P,2,1,1,3,2,0.,-9.9,4.0,VPY,
314.000          $ -9.9,4.0,ALPH4,IOU)
314.200      C GRAPH OF ANGULAR DISPLACEMENT VS. TIME--3 SEGS
315.000 0262      CALL CGPL(X,DISP3,H,M,1,1,1,3,2,0.,-9.9,6.0,DY3,
316.000          $ -9.9,6.0,ALPH4,IOU)
319.000 0263      CALL CGPL(X,DISP2,G,M,2,1,1,3,2,0.,-9.9,6.0,DY2,
320.000          $ -9.9,6.0,ALPH4,IOU)
321.000 0264      CALL CGPL(X,DISP,P,M,3,1,1,3,2,0.,-9.9,6.0,DY1,-9.9,8.0,ALPHA,
322.000          $ IOU)
322.200      C GRAPHS OF ANGULAR VELOCITY VS TIME 3 SEGS
323.000 0265      CALL CGPL(X,VEL3,H,M,1,1,1,3,2,0.,-9.9,6.0,0.0,
324.000          $ -9.9,6.0,ALP,IOU)
325.000 0266      CALL CGPL(X,VEL2,G,M,2,1,1,3,2,0.,-9.9,6.0,0.0,
326.000          $ -9.9,6.0,ALP,IOU)
327.000 0267      CALL CGPL(X,VEL,P,M,3,1,1,3,2,0.,-9.9,6.0,0.0,-9.9,8.0,ALP,
328.000          $ IOU)
328.200      C GRAPHS OF ANGULAR ACCELERATION VS. TIME 3 SEGS
329.000 0268      CALL CGPL(X,ACC3,H,M,1,1,1,3,2,0.,-9.9,6.0,A3,
330.000          $ -9.9,8.0,AL,IOU)
331.000 0269      CALL CGPL(X,ACC2,G,M,2,1,1,3,2,0.,-9.9,6.0,A2,
332.000          $ -9.9,8.0,AL,IOU)
333.000 0270      CALL CGPL(X,ACC,P,M,3,1,1,3,2,0.,-9.9,6.0,A1,
334.000          $ -9.9,8.0,AL,IOU)
334.200      C GRAPHS OF LINEAR VELOCITIES X VS. Y FOR EACH SEG
335.000 0271      CALL CGPL(XI3,YJ3,X,M,1,1,1,3,2,VPX,-9.9,6.0,VPY,-9.9,8.0,ALPH,
336.000          $ IOU)
337.000 0272      CALL CGPL(XI2,YJ2,X,M,2,1,1,3,2,VPX,-9.9,6.0,VPY,-9.9,8.0,ALPH,
338.000          $ IOU)
339.000 0273      CALL CGPL(XI1,YJ1,X,M,3,1,1,3,2,VPX,-9.9,6.0,VPY,-9.9,8.0,ALPH,
340.000          $ IOU)
341.000 0274      CALL CGPL(VELX,VELY,X,M,4,1,1,3,2,VPX,-9.9,6.0,VPY,
342.000          $ -9.9,8.0,ALPH,IOU)
342.200      C GRAPHS OF LINEAR ACCELERATIONS X VS. Y FOR SEGS
343.000 0275      CALL CGPL(XIA3,YJA3,X,M,1,1,1,3,2,APX,-9.9,6.0,APY,
344.000          $ -9.9,8.0,ALPH2,IOU)
345.000 0276      CALL CGPL(XIA2,YJA2,X,M,2,1,1,3,2,APX,-9.9,6.0,APY,
346.000          $ -9.9,8.0,ALPH2,IOU)
347.000 0277      CALL CGPL(XIA,YJA,X,M,3,1,1,3,2,APX,-9.9,6.0,APY,
348.000          $ -9.9,8.0,ALPH2,IOU)
349.000 0278      CALL CGPL(ACCX,ACCY,X,M,4,1,1,3,2,APX,-9.9,6.0,APY,
350.000          $ -9.9,8.0,ALPH2,IOU)
351.000 0279      CALL CGPL(RX1,RY1,X,M,1,1,1,3,2,RPX,-9.9,6.0,RPY,
351.200      C GRAPHS OF RESULTANT FORCES AT THE JOINTS
352.000          $ -9.9,8.0,ALPH3,IOU)
353.000 0280      CALL CGPL(RX2,RY2,X,M,2,1,1,3,2,RPX,-9.9,6.0,RPY,
354.000          $ -9.9,8.0,ALPH4,IOU)
355.000 0281      CALL CGPL(RX3,RY3,X,M,3,1,1,3,2,RPX,-9.9,6.0,RPY,
356.000          $ -9.9,8.0,ALPH3,IOU)
356.200      C GRAPHS OF RESULTANT COUPLES AT THE JOINTS
357.000 0282      CALL CGPL(X,C1,H,M,1,1,1,3,2,CM1,-9.9,6.0,CM2,
358.000          $ -9.9,8.0,ALPH6,IOU)
359.000 0283      CALL CGPL(X,C2,H,M,2,1,1,3,2,CM1,-9.9,6.0,CM2,
360.000          $ -9.9,8.0,ALPH6,IOU)
361.000 0284      CALL CGPL(X,C3,G,M,3,1,1,3,2,CM1,-9.9,8.0,CM2,
362.000          $ -9.9,8.0,ALPH7,IOU)

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VECTOR

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367.000 0001      SUBROUTINE VECTOR(P,XL,X,Y)
368.000 0002      DIMENSION P(25),X(25),Y(25),Z(25),THETA(25)
369.000 0003      DO 11 I=1,25
370.000 0004          Y(I)=0.0
371.000 0005      11  X(I)=0.0
372.000 0006      DO 3 I=1,25
373.000 0007          THETA(I)=P(I)
374.000 0008          X(I)=XL*COS(THETA(I))
375.000 0009          Y(I)=XL*SIN(THETA(I))
376.000 0010      3  CONTINUE
377.000 0011      RETURN
378.000 0012      END

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363.000 0285      CALL CGPL(X,DISP,P,M,0,1,1,3,2,0.,-9.9,6.0,-1.25,-9.9,6.0,ALPHA,
364.000 0286      $ IOU)
365.000 0286      STOP
366.000 0287      END

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## APPENDIX F

Computer Program for Angular Velocities





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1.000      C COMPUTER PROGRAM TO DETERMINE MAGNITUDES OF FOREARM ROTATIONS
2.000      DIMENSION IA(20),IB(20),IC(20),ID(20),IE(20)
3.000      DIMENSION YA(20),YB(20),YC(20),YD(20),YE(20),
4.000      $ ZA(20),ZB(20),ZC(20),ZD(20),ZE(20),XC1(20,3),
5.000      $ YC1(20,3),ZC1(20,3),XC2(20,3),YC2(20,3),ZC2(20,3),
6.000      $ XC3(20,3),YC3(20,3),ZC3(20,3),VELXB(20),VELYB(20),
7.000      $ VELXB(20),VELXC(20),VELYC(20),VELZC(20),VELXE(20),
8.000      $ VELYE(20),VELZE(20),B2(20),B2X(20),B2Y(20),B2Z(20),
9.000      $ B1X(20),B1Y(20),B1Z(20),CX(20),CY(20),CZ(20),B1X(20),
10.000     $ R1Y(20),R1Z(20),R2X(20),R2Y(20),R2Z(20),B3X(20),B3Y(20),
11.000     $ B3Z(20),TIME(20),WK(3000),WB1(20),WB2(20),WB3(20),
12.000     $ Y1(20),Y2(20),Y3(20),Y4(20),Y5(20),Y6(20),Y7(20),
13.000     $ Y8(20),DS(20),Y9(20),
14.000     $ DEN1(20),DEN2(20),DEN3(20),DEN4(20),DEN5(20),
15.000     $ WN1(20),WN2(20),WN3(20),W(20)
16.000     COMMON N,A(10,11),NP1
17.000     N=3
18.000     NP1=N+1
19.000     READ(5,1)NFRAME,TIME,DSS
20.000     FORMAT(I2,2F5.3)
21.000     1  N=NFRAME-1
22.000     IOU=6
23.000     DO 12 I=1,NFRAME
24.000     12 DS(I)=DSS
25.000     IC=NFRAME-1
26.000     NI=NFRAME
27.000     SH=NFRAME
28.000     TIME(1)=0.0
29.000     DO 11 I=2,NFRAME
30.000     11 TIME(I)=TIME(I-1)+.01
31.000     WRITE(6,66)(TIME(I),I=1,NFRAME)
32.000     66 FORMAT(10F5.4)
33.000     DO 10 I=1,NFRAME
34.000     C READ IN COORDINATES OF SEGMENTAL ENDPOINTS
35.000     READ(5,2)IA(I),YA(I),ZA(I)
36.000     READ(5,2)IB(I),YB(I),ZB(I)
37.000     READ(5,2)IC(I),YC(I),ZC(I)
38.000     READ(5,2>ID(I),YD(I),ZD(I)
39.000     READ(5,2)IE(I),YE(I),ZE(I)
40.000     10 CONTINUE
40.200     Z=.0254
41.000     DO 44 I=1,NFRAME
42.000     IA(I)=IA(I)+.0254
43.000     YA(I)=YA(I)+.0254
44.000     ZA(I)=ZA(I)+Z
45.000     IB(I)=IB(I)+Z
46.000     YB(I)=YB(I)+Z
47.000     ZB(I)=ZB(I)+Z
48.000     IC(I)=IC(I)+Z
49.000     YC(I)=YC(I)+Z
50.000     ZC(I)=ZC(I)+Z
51.000     ID(I)=ID(I)+Z
52.000     YD(I)=YD(I)+Z
53.000     ZD(I)=ZD(I)+Z
54.000     IE(I)=IE(I)+Z

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55.000 0042      YE(I)=YE(I)*Z
56.000 0043      ZE(I)=ZE(I)*Z
56.200 0044      44 CONTINUE
57.000 0045      2  FORMAT(10X,3(E12.5,2X))
60.000 0046      CALL ICSSCU (TIME,YB,DS,NX,SH,Y1,IC1,IC,WK,IER)
61.000 0047      CALL ICSSCU (TIME,YB,DS,NX,SH,Y2,IC1,IC,WK,IER)
62.000 0048      CALL ICSSCU (TIME,ZB,DS,NX,SH,Y3,ZC1,IC,WK,IER)
63.000 0049      CALL ICSSCU (TIME,IC,DS,NX,SH,Y4,IC2,IC,WK,IER)
64.000 0050      CALL ICSSCU (TIME,YC,DS,NX,SH,Y5,IC2,IC,WK,IER)
65.000 0051      CALL ICSSCU (TIME,ZC,DS,NX,SH,Y6,ZC2,IC,WK,IER)
66.000 0052      CALL ICSSCU (TIME,YE,DS,NX,SH,Y7,IC3,IC,WK,IER)
67.000 0053      CALL ICSSCU (TIME,YE,DS,NX,SH,Y8,IC3,IC,WK,IER)
68.000 0054      CALL ICSSCU (TIME,ZE,DS,NX,SH,Y9,ZC3,IC,WK,IER)
69.000          C  CALCULATE THE RELATIVE LINEAR VELOCITIES OF POINTS C AND
70.000          C  E WITH RESPECT TO B
71.000          N=NX-1
72.000          DO 13 I=1,N
73.000          VELXB(I)=XC1(I,1)
74.000          VELYB(I)=YC1(I,1)
75.000          VELZB(I)=ZC1(I,1)
76.000          VELXC(I)=XC2(I,1)-VELXB(I)
77.000          VELYC(I)=YC2(I,1)-VELYB(I)
78.000          VELZC(I)=ZC2(I,1)-VELZB(I)
79.000          VELXE(I)=XC3(I,1)-VELXB(I)
80.000          VELYE(I)=YC3(I,1)-VELYB(I)
81.000          VELZE(I)=ZC3(I,1)-VELZB(I)
82.000          13 CONTINUE
83.000          DO 8 I=1,N
84.000          8  WRITE(6,27) TIME(I),YB(I),TIME(I),Y1(I),VELXB(I)
85.000          DO 9 I=1,N
86.000          9  WRITE(6,27) TIME(I),YB(I),TIME(I),Y2(I),VELYB(I)
87.000          DO 100 I=1,N
88.000          100 WRITE(6,27) TIME(I),ZB(I),TIME(I),Y3(I),VELZB(I)
89.000          27  FORMAT(P5.3,P10.5,P5.3,2P15.5)
90.000          C  CALCULATE THE TOTAL ANGULAR VELOCITY W
91.000          C  MUST FIRST DEFINE THE VECTORS LYING IN THE ARM SEGMENT
92.000          DEN1(I)=SQRT((XC(I)-XB(I))**2+(YC(I)-YB(I))**2+(ZC(I)-ZB(I))**2)
93.000          DO 50 I=1,N
94.000          DEN2(I)=SQRT((XE(I)-XB(I))**2+(YE(I)-YB(I))**2+(ZE(I)-ZB(I))**2)
95.000          R1X(I)=(XC(I)-XB(I))/DEN1(I)
96.000          R1Y(I)=(YC(I)-YB(I))/DEN1(I)
97.000          R1Z(I)=(ZC(I)-ZB(I))/DEN1(I)
98.000          R2X(I)=(XE(I)-XB(I))/DEN2(I)
99.000          R2Y(I)=(YE(I)-YB(I))/DEN2(I)
100.000          R2Z(I)=(ZE(I)-ZB(I))/DEN2(I)
101.000          DENOM(I)=(VELXC(I)*R2Y(I)-(VELYC(I)*R2X(I))
102.000          $ +(VELZC(I)*R2Z(I))
103.000          WM1(I)=(VELYC(I)*VELZE(I)-VELZC(I)*VELYE(I))/DENOM(I)
104.000          WM2(I)=(VELZC(I)*VELXE(I)-VELXC(I)*VELZE(I))/DENOM(I)
105.000          WM3(I)=(VELXC(I)*VELYE(I)-VELYC(I)*VELXE(I))/DENOM(I)
106.000          C  FIND THE VECTORS WHICH DEFINE THE ARM SEGMENTS: B1,B2,B3
107.000          C  B2=B2X+B2Y+B2Z
108.000          DEN3(I)=SQRT((XC(I)-XB(I))**2+(YC(I)-YB(I))**2+(ZC(I)-ZB(I))**2)
109.000          B2X(I)=(XC(I)-XB(I))/DEN3(I)
110.000          B2Y(I)=(YC(I)-YB(I))/DEN3(I)

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111.000 0090      B2Z(I) = (ZC(I) - ZB(I)) / DEN3(I)
112.000 0091      DEN4(I) = SQRT((XB(I) - XA(I)) ** 2 + (YB(I) - YA(I)) ** 2 + (ZB(I)
113.000          $ - ZA(I)) ** 2)
114.000 0092      CX(I) = (XB(I) - XA(I)) / DEN4(I)
115.000 0093      CY(I) = (YB(I) - YA(I)) / DEN4(I)
116.000 0094      CZ(I) = (ZB(I) - ZA(I)) / DEN4(I)
117.000          C FORM C X B TO FIND B1 VECTOR
118.000 0095      B1X(I) = (CY(I) * B2Z(I)) - (CZ(I) * B2Y(I))
119.000 0096      B1Y(I) = (CZ(I) * B2X(I)) - (CX(I) * B2Z(I))
120.000 0097      B1Z(I) = (CX(I) * B2Y(I)) - (CY(I) * B2X(I))
121.000 0098      DEN5(I) = SQRT(B1X(I) ** 2 + B1Y(I) ** 2 + B1Z(I) ** 2)
122.000 0099      B1X(I) = B1X(I) / DEN5(I)
123.000 0100      B1Y(I) = B1Y(I) / DEN5(I)
124.000 0101      B1Z(I) = B1Z(I) / DEN5(I)
125.000          C FORM B1 X B2 TO FORM B3 VECTOR
126.000 0102      B3X(I) = (B1Y(I) * B2Z(I)) - (B1Z(I) * B2Y(I))
127.000 0103      B3Y(I) = (B1Z(I) * B2X(I)) - (B1X(I) * B2Z(I))
128.000 0104      B3Z(I) = (B1X(I) * B2Y(I)) - (B1Y(I) * B2X(I))
129.000          C MUST FORM THE DOT PRODUCT OF OMEGA WITH EACH OF THE
130.000          C UNIT VECTORS TO FROM 3 EQUATIONS IN THREE UNKNOWNNS
131.000          C WHICH MAY BE SOLVED FOR THE COMPONENTS OF OMEGA
132.000 0105      WB1(I) = (WN1(I) * B1X(I) + WN2(I) * B1Y(I) + WN3(I) * B1Z(I))
133.000 0106      WB2(I) = (WN1(I) * B2X(I) + WN2(I) * B2Y(I) + WN3(I) * B2Z(I))
134.000 0107      WB3(I) = (WN1(I) * B3X(I) + WN2(I) * B3Y(I) + WN3(I) * B3Z(I))
135.000          C MUST SOLVE THIS SYSTEM OF EQUATIONS FOR THE UNKNOWN QUANTITIES
136.000          C USE SUBROUTINE SOLVE TO SOLVE THESE
137.000 0108      A(1,1) = B1X(I)
138.000 0109      A(1,2) = B1Y(I)
139.000 0110      A(1,3) = B1Z(I)
140.000 0111      A(1,4) = WB1(I)
141.000 0112      A(2,1) = B2X(I)
142.000 0113      A(2,2) = B2Y(I)
143.000 0114      A(2,3) = B2Z(I)
144.000 0115      A(2,4) = WB2(I)
145.000 0116      A(3,1) = B3X(I)
146.000 0117      A(3,2) = B3Y(I)
147.000 0118      A(3,3) = B3Z(I)
148.000 0119      A(3,4) = WB3(I)
149.000 0120      CALL SOLVE
150.000 0121      WRITE(6,60)
151.000 0122      60  FORMAT('---', 'SOLUTION OF THE SYSTEM OF EQUATIONS')
152.000 0123      WRITE(6,62) I, (K, A(K, NP1), K=1, N)
153.000 0124      62  FORMAT('PRIME NUMBER', I5, 'W', I3, F10.5, 'W',
154.000          $ I3, F10.5, 'W', I3, F10.5)
155.000 0125      50  CONTINUE
156.000 0126      STOP
157.000 0127      END

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SOLVE

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159.000 0001      SUBROUTINE SOLVE
160.000 0002      COMMON N,A(10,11),NP1
161.000 0003      K=1
162.000 0004      DO 70 IROW=1,N
163.000 0005      K=K+1
164.000 0006      ISWAP=IROW
165.000 0007      DO 50 IN=K,N
166.000 0008      IF (ABS(A (ISWAP,IROW)) -ABS(A (IN,IROW)) .GE.0.) GO TO 50
167.000 0009      ISWAP=IN
168.000 0010      50  CONTINUE
169.000 0011      IF (ISWAP.EQ.IROW) GO TO 99
170.000 0012      DO 92 J=1,NP1
171.000 0013      TEMP=A (IROW,J)
172.000 0014      A (IROW,J)=A (ISWAP,J)
173.000 0015      92  A (ISWAP,J)=TEMP
174.000 0016      99  PIVOT=A (IROW,IROW)
175.000 0017      IF (ABS (PIVOT) -1.E-06) 27,27,28
176.000 0018      27  WRITE (6,65) PIVOT
177.000 0019      65  FORMAT ('-', 'PIVOT IS TOO SMALL. VALUE OF PIVOT
178.000      $ =', F10.5)
179.000 0020      STOP
180.000 0021      28  DO 10 J=1,NP1
181.000 0022      10  A (IROW,J)=A (IROW,J)/PIVOT
182.000 0023      DO 20 I=1,N
183.000 0024      IF (I.EQ.IROW) GO TO 20
184.000 0025      RATIO=A (I,IROW)
185.000 0026      DO 18 J=1,NP1
186.000 0027      18  A (I,J)=A (I,J) -A (IROW,J)*RATIO
187.000 0028      20  CONTINUE
188.000 0029      70  CONTINUE
189.000 0030      RETURN
190.000 0031      END

```



## APPENDIX G

Raw Data for Planar Analysis



SEGMENTAL ANALYSIS PROGRAM-5 SEGMENTS  
ANGULAR KINEMATICS OF THE UPPER ARM

INPUT

OUTPUT

X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-1.143	0.0	-1.1731	7.6048	0.0
0.020	-1.005	0.020	-1.0191	7.7690	10.4172
0.040	-0.859	0.040	-0.8606	8.1290	25.5791
0.060	-0.694	0.060	-0.6919	8.7964	41.1555
0.080	-0.520	0.080	-0.5067	9.7661	56.0170
0.100	-0.296	0.100	-0.2995	10.9922	66.3844
0.120	-0.080	0.120	-0.0656	12.4355	77.9421
0.140	0.164	0.140	0.1992	14.0586	84.3684
0.160	0.461	0.160	0.4968	15.6900	76.7658
0.180	0.772	0.180	0.8252	17.0950	60.7350
0.200	1.221	0.200	1.1766	17.9351	24.2721
0.220	1.665	0.220	1.5387	18.2084	3.0583
0.240	1.921	0.240	1.9036	16.2658	4.6334
0.260	2.254	0.260	2.2708	18.4565	12.3860
0.280	2.611	0.280	2.6425	18.7237	14.3338
0.300	2.947	0.300	3.0193	18.9212	5.4201
0.320	3.344	0.320	3.3965	18.6919	-28.3466
0.340	3.778	0.340	3.7612	17.6065	-60.2009
0.360	4.199	0.360	4.0943	15.5402	-126.4216
0.380	4.525	0.380	4.3791	12.9097	-136.6317
0.400	4.627	0.400	4.6126	10.5763	-96.6961
0.420	4.706	0.420	4.8078	9.0897	-51.9702
0.440	4.960	0.440	4.9812	8.3523	-21.6569
0.460	5.075	0.460	5.1455	8.1493	1.3043

N.B. DATA FOR SUBJECT 1, FITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





SCALAR RINGEOLICS OF 333 LOWER AMP

INPUT

OUTPUT

X	F	WAVE	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-1.000	0.0	-1.00075	8.4598	0.0
0.020	-0.976	0.020	-0.9162	8.4836	2.3702
0.040	-0.709	0.040	-0.7474	8.6275	11.9955
0.060	-0.545	0.060	-0.5746	8.5456	-10.7648
0.080	-0.407	0.080	-0.4063	8.3246	-1.7248
0.100	-0.227	0.100	-0.2380	8.0730	15.0579
0.120	-0.070	0.120	-0.0562	8.7190	16.5264
0.140	0.120	0.140	0.1125	9.0025	1.4011
0.160	0.277	0.160	0.2957	9.3704	25.5912
0.180	0.513	0.180	0.4684	9.9050	26.1132
0.200	0.694	0.200	0.6442	10.7760	31.7449
0.220	0.912	0.220	0.9225	12.2435	87.8381
0.240	1.100	0.240	1.1564	14.0709	94.3725
0.260	1.477	0.260	1.4164	15.9150	89.6204
0.280	1.000	0.280	1.0205	17.4004	94.3787
0.300	2.207	0.300	2.1800	19.2420	116.0350
0.320	2.000	0.320	2.5991	22.3403	194.7977
0.340	3.031	0.340	3.0011	27.1002	207.1015
0.360	3.055	0.360	3.5992	32.6053	200.2905
0.380	4.300	0.380	4.3709	39.2705	-5.5047
0.400	5.103	0.400	5.0514	31.0750	-334.3064
0.420	5.700	0.420	5.0720	23.0110	-470.3551
0.440	6.050	0.440	6.0133	16.5150	-353.0417
0.460	6.200	0.460	6.2075	10.4712	-159.4019

N.B. DATA FOR SPECT-1, PAPER 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 369, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 571, 572, 573, 574, 575, 576, 577, 578, 579, 580, 581, 582, 583, 584, 585, 586, 587, 588, 589, 590, 591, 592, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 607, 608, 609, 610, 611, 612, 613, 614, 615, 616, 617, 618, 619, 620, 621, 622, 623, 624, 625, 626, 627, 628, 629, 630, 631, 632, 633, 634, 635, 636, 637, 638, 639, 640, 641, 642, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 699, 700, 701, 702, 703, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 732, 733, 734, 735, 736, 737, 738, 739, 740, 741, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 784, 785, 786, 787, 788, 789, 790, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 835, 836, 837, 838, 839, 840, 841, 842, 843, 844, 845, 846, 847, 848, 849, 850, 851, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 897, 898, 899, 900, 901, 902, 903, 904, 905, 906, 907, 908, 909, 910, 911, 912, 913, 914, 915, 916, 917, 918, 919, 920, 921, 922, 923, 924, 925, 926, 927, 928, 929, 930, 931, 932, 933, 934, 935, 936, 937, 938, 939, 940, 941, 942, 943, 944, 945, 946, 947, 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 959, 960, 961, 962, 963, 964, 965, 966, 967, 968, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 991, 992, 993, 994, 995, 996, 997, 998, 999, 1000



# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE HAND SEGMENT

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-2.154	0.0	-2.1914	7.4653	0.0
0.020	-2.058	0.020	-2.0388	7.9546	48.9229
0.040	-1.938	0.040	-1.8683	9.1714	72.7579
0.060	-1.860	0.060	-1.6749	9.9420	4.3022
0.080	-1.419	0.080	-1.4784	9.5437	-44.1364
0.100	-1.244	0.100	-1.2944	8.9600	-14.2321
0.120	-1.122	0.120	-1.1116	9.6481	83.0406
0.140	-0.945	0.140	-0.8964	12.1425	166.4044
0.160	-0.689	0.160	-0.6190	15.6675	196.6903
0.180	-0.359	0.180	-0.2733	18.6548	112.6382
0.200	0.284	0.200	0.1099	19.0413	-73.4818
0.220	0.451	0.220	0.4788	17.9994	-30.2065
0.240	0.832	0.240	0.8332	17.4707	-22.6609
0.260	1.211	0.260	1.1786	17.0619	-16.2174
0.280	1.536	0.280	1.5203	17.2529	33.3022
0.300	1.951	0.300	1.8767	18.6268	104.1042
0.320	2.243	0.320	2.2814	22.4049	273.6929
0.340	2.715	0.340	2.7521	29.0631	392.1384
0.360	3.265	0.360	3.4529	37.0697	406.5190
0.380	3.962	0.380	4.2605	42.9143	175.9435
0.400	5.398	0.400	5.1121	40.1531	-452.0520
0.420	6.127	0.420	5.8081	28.6211	-791.1567
0.440	6.348	0.440	6.2518	16.3257	-528.3523
0.460	6.438	0.460	6.4927	8.7634	-227.8471

N.B. DATA FOR SUBJECT 1, FLITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



MECHANICS OF SHOULDER

INPUT

X	I	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	0.232	0.0	0.2355	1.0316	0.0
0.020	0.202	0.120	0.2060	1.0204	-1.0530
0.040	0.224	0.040	0.3261	0.9772	-0.1402
0.060	0.250	0.000	0.2440	0.8001	-5.7769
0.080	0.227	0.000	0.2614	0.7606	-7.0291
0.100	0.277	0.100	0.3752	0.6227	-0.7721
0.120	0.404	0.120	0.2065	0.4972	-5.0160
0.140	0.312	0.120	0.3955	0.4050	-0.2271
0.160	0.407	0.160	0.4344	0.4043	3.1003
0.180	0.410	0.180	0.4146	0.5074	7.1097
0.200	0.277	0.200	0.4276	0.7051	11.5901
0.220	0.212	0.220	0.4452	1.0301	15.5064
0.240	0.450	0.240	0.4092	1.2052	17.4012
0.260	0.650	0.260	0.4962	1.0391	15.1112
0.280	0.534	0.280	0.5055	1.2445	10.4093
0.300	0.302	0.300	0.5700	2.0027	4.9002
0.320	0.005	0.320	0.6155	2.1040	3.6409
0.340	0.012	0.340	0.0040	2.0152	-0.0162
0.360	0.717	0.360	0.7002	2.1090	0.0782
0.380	0.740	0.380	0.7520	2.2420	3.1334
0.400	0.790	0.400	0.7901	2.3152	4.1354
0.420	0.140	0.420	0.0452	2.0050	2.6087
0.440	0.000	0.440	0.0953	2.4214	0.0003
0.460	0.007	0.460	0.0417	2.3067	-3.1230

N.B. DATA FOR SUBJECT 1, TIME INTERVAL .02 SECONDS PER 100 PULSES





LINEAR KINEMATICS OF SHOULDER

INPUT		OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY
Y-COORDINATES OF SHOULDER				
0.0	0.630	0.0	0.6106	-1.4273
0.020	0.562	0.020	0.5853	-0.9492
0.040	0.574	0.040	0.5751	-0.1067
0.060	0.570	0.060	0.5793	0.4811
0.080	0.601	0.080	0.5919	0.7005
0.100	0.603	0.100	0.6059	0.7026
0.120	0.617	0.120	0.6196	0.6847
0.140	0.630	0.140	0.6304	0.3866
0.160	0.639	0.160	0.6333	-0.1430
0.180	0.625	0.180	0.6238	-0.6039
0.200	0.614	0.200	0.6020	-1.3354
0.220	0.548	0.220	0.5739	-1.3265
0.240	0.560	0.240	0.5501	-1.1411
0.260	0.524	0.260	0.5267	-1.1410
0.280	0.510	0.280	0.5020	-1.3006
0.300	0.473	0.300	0.4750	-1.3585
0.320	0.446	0.320	0.4489	-1.2275
0.340	0.435	0.340	0.4264	-1.0241
0.360	0.402	0.360	0.4095	-0.6060
0.380	0.405	0.380	0.4041	0.0729
0.400	0.407	0.400	0.4129	0.8397
0.420	0.430	0.420	0.4370	1.5400
0.440	0.484	0.440	0.4721	1.8760
0.460	0.506	0.460	0.5105	1.9860
				ACCELERATION
				0.0
				47.8026
				36.4503
				22.3511
				-0.3616
				0.5586
				-6.3217
				-19.4719
				-33.4913
				-32.5965
				-20.5528
				21.4375
				-2.9563
				-2.0894
				-5.9774
				3.0480
				10.0925
				10.2876
				32.1620
				35.1305
				40.6504
				30.2790
				3.3819
				6.9567

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	2.2018	-0.9354	2.2927	28.4849
2	2.1165	-0.2746	-4.2455	76.1669
3	1.9990	0.7714	-15.4812	66.2014
4	1.8179	1.6034	-28.3008	54.1523
5	1.5455	2.1158	-41.0719	32.7738
6	1.1600	2.4427	-55.0526	31.4379
7	0.6322	2.7005	-71.6579	16.5871
8	-0.0250	2.6696	-82.1083	-14.5020
9	-0.7747	2.1422	-83.0765	-59.3221
10	-1.5122	1.1165	-61.7398	-97.5659
11	-1.9885	-0.1941	-15.1112	-118.3251
12	-1.9851	-1.2298	35.5156	-65.7114
13	-1.5001	-2.1309	79.0473	-93.3103
14	-0.6497	-3.1609	118.9822	-71.2406
15	0.4602	-4.0244	150.5871	-38.3061
16	1.7162	-4.4704	165.6122	25.2681
17	2.9659	-4.2243	153.8768	88.9601
18	3.9093	-3.3988	105.5929	128.4765
19	4.3081	-2.0921	45.5145	153.4295
20	4.2631	-0.6268	1.5221	131.3251
21	4.0587	0.6562	-16.3078	109.0270
22	3.8856	1.6835	-22.6714	62.3995
23	3.7557	2.2442	-25.5193	48.2187
24	3.6223	2.5407	-29.6559	49.4890

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



WRIST KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	5.8887	0.8409	-4.8208	78.3022
2	5.4892	2.0922	-19.5459	124.3236
3	5.0206	3.7423	-41.2462	115.6415
4	4.5681	5.1364	-69.7028	93.4787
5	3.5168	6.1665	-86.8400	72.1184
6	2.4263	7.0814	-109.7870	70.0088
7	0.9754	7.9034	-139.7255	46.4380
8	-0.9140	8.2263	-160.2663	-2.6181
9	-3.1695	7.6979	-165.4043	-67.1394
10	-5.5504	6.1376	-135.9407	-130.5026
11	-7.5371	3.6841	-70.5350	-184.4372
12	-8.7179	1.0365	1.8497	-177.0702
13	-8.9868	-1.8811	79.0626	-214.7741
14	-8.2726	-5.3202	175.8719	-202.3913
15	-6.3624	-8.7994	284.4849	-150.6344
16	-3.3357	-11.7156	363.6572	-59.3230
17	0.6316	-13.6495	428.1150	60.5683
18	5.7028	-14.3371	480.8013	214.1611
19	11.9658	-12.1097	459.3623	494.5918
20	16.5448	-4.8608	144.4657	725.1421
21	15.0907	3.5915	-242.5308	556.0769
22	10.0623	7.3272	-291.9929	213.3939
23	6.6875	7.0787	-167.6882	52.6055
24	5.2553	6.3160	-96.2625	58.4159

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## ELBOW KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	3.7163	-0.2991	2.2927	28.4849
2	3.5345	0.5482	-2.3441	77.3371
3	3.3200	1.9073	-11.3244	69.7756
4	3.0206	3.0551	-22.6736	60.9445
5	2.5615	3.9463	-35.2454	43.2708
6	1.8550	4.6937	-50.8554	45.0323
7	0.8068	5.3600	-70.5633	33.2557
8	-0.6211	5.6233	-85.6857	3.2224
9	-2.3775	5.0983	-91.1227	-44.4820
10	-4.2023	3.6006	-71.3028	-88.7350
11	-5.5376	1.2822	-19.9142	-116.3272
12	-5.8655	-1.1043	34.8605	-85.6904
13	-5.2041	-3.4114	73.0986	-98.6382
14	-3.6751	-5.7091	116.9519	-72.9567
15	-1.4604	-7.5478	145.1168	-41.0034
16	1.2215	-8.4953	165.4705	24.1151
17	3.9762	-8.1069	152.3447	94.8390
18	6.1667	-6.4767	95.6105	142.4694
19	7.0224	-4.0222	23.4333	169.1313
20	6.8777	-1.5320	-26.1494	140.9053
21	6.3142	0.4304	-36.9286	111.0911
22	5.8243	1.8690	-33.7590	81.3385
23	5.4816	2.7197	-29.9943	46.9860
24	5.2077	3.2797	-29.4022	49.6069

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPPOINTS

## KINEMATICS OF THE LOWER ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	4.6504	0.1911	-4.8208	78.3022
2	4.3750	1.2406	-19.6579	124.0851
3	4.0513	2.6964	-42.5940	114.1671
4	3.6000	3.9501	-67.9272	96.2212
5	2.9722	4.9010	-86.7264	72.3824
6	2.1049	5.7204	-110.3993	67.5740
7	0.6793	6.4536	-139.8996	43.6111
8	-0.7473	6.7426	-160.1107	-3.9980
9	-2.7181	6.2161	-164.1810	-71.1543
10	-4.7820	4.6915	-133.7547	-140.6166
11	-6.3974	2.3150	-64.3135	-191.9141
12	-7.1034	-0.1840	13.4321	-185.8262
13	-6.8307	-2.7534	93.6000	-220.0551
14	-5.6520	-5.5419	190.5346	-203.6313
15	-3.5683	-8.0860	294.8276	-153.9938
16	-0.7381	-9.8800	379.1665	-43.3493
17	2.5380	-10.4868	444.7380	83.1458
18	5.9296	-9.8532	483.1992	261.5923
19	9.1481	-7.4998	436.4917	532.0083
20	11.6345	-2.9720	145.5358	724.8190
21	10.0494	1.7697	-190.5900	574.9735
22	7.6460	4.2160	-244.3199	274.7917
23	6.0002	4.5941	-152.1298	103.6509
24	5.2282	4.5853	-95.8500	34.7618

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



KINEMATICS OF THE HAND CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	6.1501	0.6540	-6.1170	46.1091
2	5.7947	1.9378	-29.9221	31.8483
3	5.3980	3.6266	-68.7849	16.2426
4	4.7536	5.0919	-119.0057	-11.1844
5	3.9257	6.2044	-148.8735	-39.5127
6	2.8073	7.1866	-177.1921	-76.2542
7	1.3476	8.0874	-219.1161	-115.9055
8	-0.5064	8.5526	-266.7104	-149.1991
9	-2.7783	8.2471	-312.0923	-186.6493
10	-5.3337	6.9107	-300.6299	-220.3754
11	-7.6270	4.4987	-195.7307	-223.3288
12	-9.0748	1.7240	-60.4039	-179.1632
13	-9.5433	-1.3755	81.1010	-113.3212
14	-8.9519	-5.0392	250.2525	-7.1496
15	-7.1040	-8.7619	432.5569	129.0952
16	-4.1001	-11.9570	593.6689	249.3221
17	-0.0992	-14.2784	775.3259	376.1016
18	5.2745	-15.5122	1013.6772	586.2314
19	12.4545	-13.6284	1114.7078	950.8848
20	18.2062	-5.6873	484.2544	1105.7490
21	16.5925	4.2639	-501.0889	580.4973
22	10.6257	8.4225	-627.4700	26.7563
23	6.7095	7.7810	-324.9111	-79.9542
24	5.1769	6.6849	-161.1188	-62.2545

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## FINGERTIP KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	6.8222	0.1736	-6.1170	46.1091
2	0.5803	1.5407	-25.0903	29.4060
3	6.3683	3.3291	-61.0870	13.9820
4	5.8679	4.9776	-118.5322	-11.2339
5	4.9774	6.3018	-153.7370	-39.9631
6	3.7612	7.4572	-178.7073	-76.5840
7	2.3047	8.5607	-210.8786	-111.8322
8	0.5432	9.3916	-254.3264	-137.7010
9	-1.7723	9.6592	-300.1456	-169.8768
10	-4.7764	8.8984	-297.2651	-208.3732
11	-7.8580	6.5931	-194.8332	-231.4666
12	-9.9925	3.4919	-58.8658	-182.1301
13	-10.9742	-0.0754	82.9570	-115.0076
14	-10.6987	-4.3166	251.9169	-7.8356
15	-9.0108	-8.6654	428.8762	129.2313
16	-6.0658	-12.5776	582.6331	245.8527
17	-1.9786	-15.8956	752.3678	356.3459
18	4.1732	-18.5540	998.8174	545.4595
19	13.7109	-17.5335	1128.5542	597.8491
20	22.4785	-7.7612	501.8005	1097.2461
21	20.6856	5.9930	-547.1719	561.0308
22	12.0744	11.2391	-662.9604	-42.2441
23	6.7662	9.5867	-326.7441	-138.3984
24	4.9752	7.6335	-155.6744	-86.9175

N.B. DATA FOR SUBJECT 1, PLTCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE WRIST JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-5.37070	49.10043	-1.04072
2	-26.27101	34.43518	0.50295
3	-66.39313	20.80513	2.46393
4	-104.48700	-1.24669	4.49221
5	-130.71094	-26.47092	5.34372
6	-155.57466	-58.71182	5.70446
7	-192.58394	-89.57193	5.98869
8	-235.92776	-112.28474	5.46616
9	-274.01685	-140.53510	2.53423
10	-263.95288	-174.33496	-3.78382
11	-171.65159	-194.61098	-9.38121
12	-53.03459	-151.29349	-6.93070
13	71.20667	-92.36000	-0.48013
14	219.72173	1.73705	8.71256
15	379.78491	122.12570	16.69958
16	521.24121	224.47533	18.82706
17	680.73608	321.48804	14.09057
18	896.06854	487.52979	-5.29510
19	978.71338	805.70776	-44.55217
20	425.20166	971.99854	-34.14516
21	-439.95581	501.20192	24.33417
22	-550.91346	-28.47360	7.42699
23	-285.27197	-112.89708	-6.22559
24	-141.46227	-67.69690	-4.87237

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE ELBOW JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-15.10867	227.09518	-6.27797
2	-66.38461	304.91138	0.52797
3	-146.43295	271.28735	10.12582
4	-241.70006	212.94446	20.96321
5	-305.89819	139.56537	27.35689
6	-378.58130	97.61191	33.15852
7	-474.98096	18.75078	35.84050
8	-559.35132	-100.53647	30.28587
9	-605.66260	-264.44238	18.74574
10	-534.13721	-438.55591	5.37189
11	-301.76489	-562.45313	3.00203
12	-25.90181	-506.82789	8.59447
13	260.27979	-518.25903	30.14914
14	604.60156	-389.77466	73.51569
15	975.33667	-169.11740	153.15681
16	1287.15806	146.63409	181.59186
17	1579.10693	519.36670	198.81229
18	1366.07102	1055.77148	153.31067
19	1860.42576	1960.18896	10.31633
20	118.77979	2455.95898	-58.48485
21	-824.94751	1682.48242	89.44273
22	-1044.44458	546.42993	104.78453
23	-592.57202	126.60608	42.02040
24	-335.07910	123.34613	12.97731

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





## KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE SHOULDER JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-7.03840	327.36182	37.64148
2	-81.32861	573.01855	108.63632
3	-200.92673	504.31616	152.78003
4	-341.31885	403.56030	178.70354
5	-450.47695	254.92967	161.17703
6	-572.36646	208.27347	141.22972
7	-727.21655	77.13725	70.92479
8	-848.37256	-151.53351	-62.91206
9	-898.09160	-473.25635	-229.00272
10	-751.46118	-781.93779	-318.93335
11	-354.95630	-978.95752	-216.43259
12	99.11320	-808.54199	11.83637
13	538.52612	-864.31104	250.49854
14	1023.41876	-640.54126	425.04936
15	1505.40332	-303.95483	429.30469
16	1670.15368	235.57780	183.36722
17	2120.75317	832.50625	-217.69756
18	2237.75761	1468.00854	-679.54590
19	2020.63745	2440.26074	-1063.36182
20	724.13745	2916.22339	-654.39771
21	-882.35059	2066.25732	336.15233
22	-1124.24605	836.47607	534.86208
23	-682.39990	296.53589	292.66140
24	-439.46777	257.54932	176.09616

N.B. DATA FOR SUBJECT 1, LITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



SUGMENTAL ANALYSIS PROGRAM-3 SEGMENTS  
ANGULAR KINEMATICS OF THE UPPER ARM

INPUT

OUTPUT

X	P	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	1.127	0.0	1.1393	19.3107	0.0
0.010	1.343	0.010	1.3321	19.2281	-16.5239
0.020	1.513	0.020	1.5236	19.0527	-18.5707
0.030	1.725	0.030	1.7129	18.7806	-35.8254
0.040	1.893	0.040	1.8989	18.4177	-36.7570
0.050	2.108	0.050	2.0811	18.0019	-46.4031
0.060	2.252	0.060	2.2592	17.6791	-18.1510
0.070	2.442	0.070	2.4354	17.5854	0.0109
0.080	2.610	0.080	2.6118	17.7282	27.9586
0.090	2.788	0.090	2.7909	18.1375	53.8982
0.100	2.970	0.100	2.9753	18.7672	76.0353
0.110	3.131	0.110	3.1672	19.6214	90.7999
0.120	3.377	0.120	3.3674	20.3455	54.6356
0.130	3.544	0.130	3.5732	20.7815	21.9592
0.140	3.751	0.140	3.7816	20.7853	-31.1996
0.150	4.002	0.150	3.9861	19.9456	-136.7472
0.160	4.153	0.160	4.1773	18.1602	-220.2538
0.170	4.424	0.170	4.3460	15.3696	-337.8276
0.180	4.554	0.180	4.4826	11.9563	-346.0344
0.190	4.622	0.190	4.5864	8.9486	-254.4365
0.200	4.642	0.200	4.6655	7.1078	-113.5761
0.210	4.677	0.210	4.7327	6.5128	-5.4313
0.220	4.771	0.220	4.7980	6.6124	25.3736
0.230	4.857	0.230	4.8653	6.8529	18.6921

N.P. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



## SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE LOWER ARM

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	0.667	0.0	0.6505	13.1992	0.0
0.010	0.778	0.010	0.7829	13.3140	22.9685
0.020	0.912	0.020	0.9174	13.6217	38.5824
0.030	1.055	0.030	1.0557	14.0491	46.8665
0.040	1.197	0.040	1.1987	14.5569	54.6966
0.050	1.341	0.050	1.3471	15.1334	60.6049
0.060	1.521	0.060	1.5014	15.7278	58.2894
0.070	1.630	0.070	1.6620	16.4340	92.9473
0.080	1.843	0.080	1.8302	17.1665	63.5527
0.090	2.027	0.090	2.0050	17.7912	61.3722
0.100	2.120	0.100	2.1864	18.5428	88.9782
0.110	2.399	0.110	2.3766	19.5271	107.8640
0.120	2.595	0.120	2.5781	20.8535	157.4227
0.130	2.611	0.130	2.7957	22.7924	230.3524
0.140	3.018	0.140	3.0367	25.5620	323.5630
0.150	3.242	0.150	3.3097	29.1552	391.0608
0.160	3.554	0.160	3.6201	32.9171	365.2861
0.170	3.882	0.170	3.9656	35.9879	248.9042
0.180	4.340	0.180	4.3341	37.3180	17.0615
0.190	4.737	0.190	4.7044	36.3674	-207.1953
0.200	5.174	0.200	5.0547	33.4003	-386.1921
0.210	5.417	0.210	5.3692	29.4595	-401.9875
0.220	5.731	0.220	5.6445	25.6915	-351.5923
0.230	5.895	0.230	5.8867	23.0251	-181.0606

R.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN PAGES





## SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE HAND SEGMENT

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	0.274	0.0	0.2938	16.3988	0.0
0.010	0.489	0.010	0.4560	15.8467	-110.4183
0.020	0.605	0.020	0.6102	15.1219	-34.5396
0.030	0.773	0.030	0.7605	15.0242	14.9835
0.040	0.888	0.040	0.9135	15.7751	135.1971
0.050	1.070	0.050	1.0777	17.0307	115.9492
0.060	1.241	0.060	1.2528	17.8816	54.2020
0.070	1.469	0.070	1.4322	17.7899	-72.5318
0.080	1.614	0.080	1.6077	17.4486	4.3249
0.090	1.748	0.090	1.7843	18.0535	116.5997
0.100	1.988	0.100	1.9692	18.7675	26.2058
0.110	2.152	0.110	2.1584	19.1104	42.3841
0.120	2.373	0.120	2.3513	19.4312	21.7660
0.130	2.549	0.130	2.5483	20.1444	120.8804
0.140	2.796	0.140	2.7576	21.8694	223.9246
0.150	3.021	0.150	2.9927	25.6901	540.4126
0.160	3.225	0.160	3.2845	33.4056	1014.5566
0.170	3.617	0.170	3.6723	44.3320	1158.8643
0.180	3.961	0.180	4.1709	55.1100	590.8496
0.190	4.866	0.190	4.7496	58.4051	-337.9009
0.200	5.405	0.200	5.2998	49.9368	-1355.6934
0.210	5.855	0.210	5.7241	34.2177	-1788.1479
0.220	6.035	0.220	5.9818	17.8082	-1493.7485
0.230	6.151	0.230	6.0951	5.8297	-901.9375

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



# LINEAR KINEMATICS OF SHOULDER

INPUT			OUTPUT		
X	P	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
X-COORDINATES OF SHOULDER					
0.0	0.323	0.0	0.3118	1.4521	0.0
0.010	0.332	0.010	0.3263	1.4610	1.7777
0.020	0.340	0.020	0.3411	1.4920	4.4141
0.030	0.355	0.030	0.3563	1.5485	6.8834
0.040	0.366	0.040	0.3721	1.6284	9.0960
0.050	0.387	0.050	0.3889	1.7257	10.3621
0.060	0.402	0.060	0.4067	1.8343	11.3675
0.070	0.413	0.070	0.4256	1.9493	11.6193
0.080	0.441	0.080	0.4456	2.0572	9.9570
0.090	0.469	0.090	0.4667	2.1448	7.5624
0.100	0.478	0.100	0.4885	2.2099	5.4502
0.110	0.521	0.110	0.5108	2.2460	1.7686
0.120	0.529	0.120	0.5333	2.2529	-0.3954
0.130	0.564	0.130	0.5557	2.2345	-3.2675
0.140	0.586	0.140	0.5779	2.1942	-4.7679
0.150	0.607	0.150	0.5996	2.1447	-5.1195
0.160	0.638	0.160	0.6208	2.0974	-4.3394
0.170	0.641	0.170	0.6416	2.0709	-0.9502
0.180	0.659	0.180	0.6623	2.0779	2.3437
0.190	0.670	0.190	0.6833	2.1151	5.0918
0.200	0.696	0.200	0.7047	2.1697	5.8207
0.210	0.724	0.210	0.7267	2.2249	5.2226
0.220	0.740	0.220	0.7492	2.2720	4.1964
0.230	0.776	0.230	0.7721	2.3020	1.8013

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



# LINEAR KINEMATICS OF SHOULDER

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
Y-COORDINATES OF SHOULDER					
0.0	-0.062	0.0	-0.0598	-1.1525	0.0
0.010	-0.073	0.010	-0.0714	-1.1557	-0.6212
0.020	-0.081	0.020	-0.0830	-1.1674	-1.7640
0.030	-0.096	0.030	-0.0947	-1.1877	-2.3697
0.040	-0.106	0.040	-0.1057	-1.2164	-3.3527
0.050	-0.124	0.050	-0.1191	-1.2535	-4.0734
0.060	-0.130	0.060	-0.1319	-1.3035	-5.9245
0.070	-0.132	0.070	-0.1452	-1.3698	-7.3347
0.080	-0.153	0.080	-0.1592	-1.4334	-5.3834
0.090	-0.176	0.090	-0.1738	-1.4695	-1.8419
0.100	-0.187	0.100	-0.1885	-1.4726	1.2202
0.110	-0.202	0.110	-0.2031	-1.4433	4.6411
0.120	-0.205	0.120	-0.2173	-1.3780	3.4207
0.130	-0.231	0.130	-0.2305	-1.2594	15.2757
0.140	-0.246	0.140	-0.2422	-1.0729	22.0095
0.150	-0.252	0.150	-0.2518	-0.8234	27.9001
0.160	-0.272	0.160	-0.2585	-0.5153	33.6819
0.170	-0.272	0.170	-0.2619	-0.1660	36.1578
0.180	-0.275	0.180	-0.2618	0.1954	36.1116
0.190	-0.263	0.190	-0.2581	0.5400	32.7798
0.200	-0.267	0.200	-0.2511	0.8443	28.0910
0.210	-0.239	0.210	-0.2414	1.0820	19.4239
0.220	-0.225	0.220	-0.2298	1.2358	11.3335
0.230	-0.208	0.230	-0.2170	1.3154	4.5725

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## ELBOW KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	-5.2134	1.9163	-37.0053	-100.6744
2	-5.6366	0.5715	-3.1106	-110.5247
3	-5.7400	-0.8255	27.1915	-111.3992
4	-5.5162	-2.1983	61.6449	-104.0400
5	-4.9971	-3.4715	66.2557	-90.8865
6	-4.2437	-4.5945	108.4592	-71.3561
7	-3.3537	-5.5716	115.1953	-60.8326
8	-2.3679	-6.4550	125.1492	-49.3380
9	-1.2475	-7.2465	133.0545	-38.4394
10	-0.2232	-7.9422	144.5785	-25.1210
11	1.0283	-8.5133	160.6080	-7.9561
12	2.4371	-8.8970	177.2245	17.9684
13	3.9840	-8.9141	185.6422	69.2538
14	5.5382	-8.4322	177.0463	119.3361
15	6.9111	-7.4033	142.1149	175.1674
16	7.8114	-5.8567	72.8447	218.2116
17	8.0338	-4.0339	-3.0945	222.2611
18	7.5237	-2.2565	-86.0903	197.7874
19	6.4997	-0.8388	-115.6703	143.7308
20	5.4884	0.1126	-91.8348	94.0416
21	4.8677	0.7177	-42.3918	64.7135
22	4.6993	1.1322	-4.2146	49.9877
23	4.7755	1.4508	4.2097	43.7412
24	4.8682	1.7109	-2.8652	38.9182

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	-1.4541	0.1854	-37.0053	-100.6744
2	-1.6344	-0.4026	-6.5516	-109.6875
3	-1.6612	-1.0183	23.2159	-111.2113
4	-1.5317	-1.6283	54.0442	-105.1272
5	-1.2603	-2.1996	78.7981	-93.4249
6	-0.8770	-2.7102	99.7809	-76.7133
7	-0.4277	-3.1644	112.1911	-63.3041
8	0.0532	-3.5869	125.1507	-49.3363
9	0.5728	-3.9679	136.0829	-33.2688
10	1.1124	-4.2916	148.5465	-14.2747
11	1.6947	-4.5423	163.3053	8.1150
12	2.3293	-4.6931	176.7256	37.4222
13	3.0076	-4.6637	183.0207	80.6660
14	3.6749	-4.3867	174.1808	125.5594
15	4.2508	-3.8351	146.1082	169.3046
16	4.6154	-3.0179	94.7567	198.7427
17	4.6857	-2.0494	37.5206	198.1879
18	4.0483	-1.0783	-18.4934	171.8473
19	4.0053	-0.2555	-43.4569	126.8416
20	3.5858	0.3536	-37.7364	87.1877
21	3.3460	0.7891	-18.0769	63.5719
22	3.3037	1.1039	-3.0508	50.0113
23	3.3635	1.3295	-1.2084	43.2760
24	3.4269	1.4879	-6.8286	38.3080

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



KINEMATICS OF THE LOWER AND UPPER PARTS OF GRAVITY

FLAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	-6.2102	5.2261	-102.5626	-200.0838
2	-6.8096	1.7424	-49.1607	-219.8253
3	-7.0988	0.2670	1.9978	-229.3956
4	-7.0409	-1.3353	59.2472	-228.4715
5	-6.6661	-2.6115	100.0557	-216.3949
6	-6.0535	-4.1755	155.8870	-195.1618
7	-5.3702	-5.4557	190.0008	-184.6373
8	-4.4207	-6.0417	223.6651	-167.5265
9	-3.4165	-7.7555	271.7112	-146.2647
10	-2.2359	-8.6755	317.5518	-115.5859
11	-0.6595	-9.6480	366.9922	-76.7027
12	0.7508	-10.6536	421.4153	-20.7223
13	2.5950	-11.1126	467.6636	68.3779
14	4.5747	-11.1061	501.2315	167.4729
15	6.5774	-10.5765	515.7124	291.6687
16	8.4191	-9.4357	494.3234	436.8964
17	9.9240	-7.6776	429.5935	590.9731
18	10.6172	-5.2066	273.6401	723.1091
19	10.6242	-2.5575	66.7725	760.8079
20	10.0252	0.0765	-116.6981	677.3816
21	8.7910	2.1158	-226.3257	515.8750
22	7.6687	3.3751	-256.9025	357.1440
23	6.6854	4.0250	-212.8629	245.3434
24	5.5771	4.3594	-192.8267	100.4921

N.B. DATA FOR SUBJECT 1, FIGURE 1, TIME INTERVAL .01 SECONDS REPRODUCED





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## WRIST KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	-7.5315	4.9523	-102.5036	-200.0838
2	-8.3619	3.3085	-51.8586	-217.1340
3	-8.8767	1.5757	-3.1565	-225.5138
4	-9.0619	-0.1914	52.5052	-224.6557
5	-8.9297	-1.9367	99.6711	-215.1077
6	-8.5230	-3.6209	146.1187	-196.9395
7	-7.9038	-5.2554	180.9887	-183.9699
8	-7.1340	-6.8891	214.4109	-168.7697
9	-6.1592	-8.5234	261.5574	-148.8942
10	-4.9039	-10.1127	308.3484	-119.8537
11	-3.3619	-11.6186	354.9844	-85.1964
12	-1.4845	-12.9822	409.0679	-33.5850
13	0.7538	-14.0267	453.7646	46.3788
14	3.2975	-14.6506	488.3230	131.6503
15	6.1352	-14.7805	510.1145	233.6776
16	9.2248	-14.1869	505.1516	375.1670
17	12.4296	-12.5076	457.3987	537.3740
18	15.1830	-9.3476	303.2854	695.1616
19	16.5567	-4.8358	69.3964	759.7651
20	16.0345	0.0282	-152.9464	677.6558
21	13.9917	3.9691	-280.4590	494.4458
22	11.4653	6.3483	-283.5576	316.5737
23	9.2172	7.4326	-247.5301	198.6819
24	7.4471	7.8701	-264.4267	161.7927

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE LOWER ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	-6.2102	3.2261	-102.5036	-200.0838
2	-6.6096	1.7484	-49.1807	-219.8253
3	-7.0888	0.2070	1.9078	-229.3906
4	-7.0409	-1.3353	59.2472	-228.4719
5	-6.6881	-2.8115	108.0937	-218.3949
6	-6.0438	-4.1759	155.8870	-199.1618
7	-5.3102	-5.4357	190.6008	-184.6378
8	-4.4287	-6.6417	228.0651	-167.5205
9	-3.4165	-7.7955	271.7112	-146.2047
10	-2.2359	-8.6755	317.5518	-115.5859
11	-0.6595	-9.8486	366.9922	-76.7027
12	0.7508	-10.6536	421.4153	-20.7223
13	2.5950	-11.1126	467.6636	68.3779
14	4.5747	-11.1061	501.2310	167.4729
15	6.5774	-10.5783	515.7124	291.8687
16	8.4191	-9.4387	494.3384	438.8984
17	9.9240	-7.6776	429.5935	590.9731
18	10.6172	-5.3068	273.0901	723.1091
19	10.8242	-2.5575	56.7725	760.8079
20	10.0232	0.0763	-118.6961	677.3818
21	8.7910	2.1158	-220.3257	515.8750
22	7.6087	3.3751	-230.9323	357.1440
23	6.6854	4.0230	-212.8829	245.3434
24	5.9771	4.3594	-192.8287	189.4921

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## FINGER TIP KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	-8.2615	7.3748	-223.4413	-237.9818
2	-9.4344	5.4953	-131.4686	-216.6007
3	-10.2035	3.4805	-52.7461	-161.8802
4	-10.6536	1.4817	28.6573	-105.8871
5	-10.8491	-0.4553	90.4028	-59.7781
6	-10.8288	-2.3818	170.9847	-29.8673
7	-10.5143	-4.3960	251.6834	-4.4193
8	-9.8421	-6.5113	341.2876	37.7810
9	-8.8393	-8.6224	411.3433	107.2978
10	-7.6157	-10.7006	484.0176	167.0017
11	-6.0206	-12.7376	590.3245	240.4207
12	-3.9290	-14.6106	682.8604	330.3706
13	-1.3683	-16.1282	764.7771	424.8225
14	1.5066	-17.2177	824.7771	504.4763
15	4.8759	-17.8969	888.5957	584.3318
16	9.6391	-18.0917	957.6096	644.9475
17	13.1624	-17.5987	1068.5527	743.5308
18	18.6319	-15.2241	1068.3582	975.6587
19	23.8154	-9.2018	707.8059	1302.9038
20	25.0052	0.3620	-225.9999	1305.5513
21	26.3506	8.2227	-864.5176	621.8057
22	14.2547	10.8069	-799.1111	-28.7947
23	10.0296	10.0464	-494.5250	-288.1031
24	7.0146	8.7503	-231.3611	-246.2178

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES





# LOCAL VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE HAND CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	-7.7355	5.0378	-223.4413	-237.9818
2	-8.0622	3.9208	-136.8491	-205.6298
3	-9.2496	2.7090	-54.9363	-158.7477
4	-9.5675	0.2771	29.8002	-107.0884
5	-9.4671	-1.5219	102.2469	-67.9193
6	-9.1686	-3.2740	132.2574	-35.9413
7	-8.6347	-5.0148	257.3806	-5.2949
8	-7.8923	-6.7834	332.3381	38.8501
9	-6.9596	-8.5511	411.8214	107.3155
10	-5.6632	-10.2773	496.6274	169.7958
11	-4.1063	-11.9319	592.9976	241.5556
12	-2.1685	-13.4262	686.7639	332.9709
13	0.1566	-14.6152	766.4485	426.5173
14	2.7129	-15.3698	832.2556	515.5676
15	5.7010	-15.9551	897.8801	607.8071
16	8.0698	-15.2802	966.4307	704.0901
17	12.6245	-12.9331	1052.5586	854.6604
18	16.1407	-10.9930	1003.4458	1096.2620
19	18.5152	-6.0513	613.2732	1359.7634
20	18.5093	0.1217	-188.6250	1306.9419
21	15.7806	5.1691	-739.6365	764.9480
22	12.2902	7.5967	-694.1597	138.9641
23	9.6046	8.1645	-445.5195	-130.3086
24	7.4900	8.1166	-262.6968	-198.1666

N.B. DATA FOR SUBJECT 1, PLUCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



# KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE ELBOW JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-403.23877	-584.67627	1.07954
2	-219.49855	-605.78149	3.43687
3	-44.38028	-577.05884	7.00162
4	145.84396	-526.04102	17.56139
5	308.12207	-464.32373	31.99353
6	474.94019	-400.68936	53.40491
7	610.99341	-348.40747	75.64864
8	753.36200	-276.77856	99.36859
9	910.43604	-172.68480	125.36574
10	1077.49390	-58.36252	151.90668
11	1261.97607	84.59961	178.48724
12	1454.23755	276.64673	199.83279
13	1617.65723	539.55811	209.28883
14	1743.20679	809.66602	200.40227
15	1830.67788	1131.49756	172.04547
16	1847.13379	1481.27954	111.89008
17	1791.92529	1875.02637	21.93678
18	1432.66748	2345.74951	-60.74275
19	673.33423	2709.22217	-63.51706
20	-405.38330	2543.02612	55.40456
21	-1094.45850	1616.45361	149.53146
22	-1075.95557	724.59009	144.18599
23	-821.18945	271.02734	109.17807
24	-620.16162	151.13603	78.56841

N.B. DATA FOR SUBJECT 1, PITCH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES



# KINEMATICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE SHOULDER JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-533.49731	-939.05029	-275.18384
2	-242.56030	-991.88159	-151.65672
3	37.33957	-968.52246	-10.63072
4	336.07935	-896.00887	138.88422
5	585.49121	-793.17944	258.97681
6	826.16895	-670.12012	355.53906
7	1005.90625	-571.23779	412.16797
8	1193.89258	-450.44214	434.42212
9	1389.44775	-289.79102	415.03467
10	1600.37769	-108.60956	353.59009
11	1816.81055	113.16451	240.91724
12	2076.31177	408.37280	60.49261
13	2261.88989	823.50244	-195.26955
14	2356.32324	1251.63501	-463.64111
15	2344.37842	1729.20752	-719.95508
16	2180.67725	2180.87500	-911.58325
17	1923.99756	2572.64771	-1015.50049
18	1367.57056	2950.65186	-930.49512
19	520.36572	3155.70459	-555.96045
20	-538.21533	2949.92676	89.94836
21	-1158.08911	1840.22681	539.47754
22	-1086.69464	900.62964	560.65820
23	-825.44287	423.35689	432.98071
24	-644.19800	285.97996	328.46851

N.B. DATA FOR SUBJECT 1, PLICH 1, TIME INTERVAL .01 SECONDS BETWEEN FRAMES





SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS  
ANGULAR KINEMATICS OF THE UPPER ARM

## INPUT

## OUTPUT

X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-1.901	0.0	-1.9149	7.0076	0.0
0.020	-1.754	0.020	-1.7737	7.1565	14.8919
0.040	-1.630	0.040	-1.6252	7.8110	50.5462
0.060	-1.450	0.060	-1.4569	9.1252	80.8744
0.080	-1.268	0.080	-1.2557	11.1146	118.0747
0.100	-1.022	0.100	-1.0082	13.7207	142.5341
0.120	-0.732	0.120	-0.7046	16.6674	152.1332
0.140	-0.368	0.140	-0.3422	19.5081	131.9437
0.160	-0.014	0.160	0.0712	21.6715	84.3933
0.180	0.582	0.180	0.5122	21.9630	-55.2460
0.200	1.006	0.200	0.9367	20.2068	-120.3643
0.220	1.363	0.220	1.3165	17.9042	-109.8866
0.240	1.655	0.240	1.6570	16.3114	-49.4066
0.260	1.962	0.260	1.9772	15.9099	9.2643
0.280	2.286	0.280	2.3001	16.5232	52.0677
0.300	2.610	0.300	2.6429	17.8432	79.9217
0.320	2.957	0.320	3.0152	19.3666	72.4272
0.340	3.370	0.340	3.4123	20.1121	2.1223
0.360	3.802	0.360	3.8073	18.9953	-113.6077
0.380	4.253	0.380	4.1563	15.5035	-235.3732
0.400	4.493	0.400	4.4210	11.0495	-210.0231
0.420	4.592	0.420	4.6068	7.8783	-107.0966
0.440	4.723	0.440	4.7488	6.6019	-20.5303
0.460	4.791	0.460	4.8805	0.7769	38.0166

N.B. DATA FOR SUBJECT 2, FITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE LOWER ARM

### INPUT

X	P
0.0	-1.337
0.020	-1.195
0.040	-1.028
0.060	-0.930
0.080	-0.703
0.100	-0.461
0.120	-0.332
0.140	-0.204
0.160	-0.072
0.180	0.013
0.200	0.187
0.220	0.384
0.240	0.714
0.260	1.121
0.280	1.577
0.300	2.012
0.320	2.472
0.340	2.956
0.360	3.428
0.380	4.149
0.400	5.002
0.420	5.494
0.440	5.860
0.460	5.998

### OUTPUT

TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-1.3432	7.3503	0.0
0.020	-1.1953	7.4763	12.5952
0.040	-1.0424	7.8582	25.5936
0.060	-0.8773	8.7966	68.2461
0.080	-0.6919	9.5353	5.6235
0.100	-0.5057	8.7988	-79.2715
0.120	-0.3452	7.2700	-73.6124
0.140	-0.2124	6.1243	-40.9531
0.160	-0.0947	5.8087	9.3878
0.180	0.0297	6.9545	105.1958
0.200	0.1939	9.6726	166.6198
0.220	0.4239	13.4885	214.9616
0.240	0.7345	17.4637	182.5631
0.260	1.1154	20.3791	108.9757
0.280	1.5407	21.9424	47.3549
0.300	1.9898	23.0040	58.8014
0.320	2.4653	24.7341	114.2130
0.340	2.9875	27.7157	183.9480
0.360	3.5790	31.4580	190.2807
0.380	4.2345	33.5045	14.3650
0.400	4.8843	30.3199	-332.8220
0.420	5.4168	22.5566	-443.5076
0.440	5.7821	14.1221	-399.9407
0.460	5.9979	8.1217	-200.0961

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE HAND SEGMENT

INPUT			OUTPUT		
X	P	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-0.901	0.0	-0.9328	5.2447	0.0
0.020	-0.827	0.020	-0.8241	5.8064	56.1674
0.040	-0.761	0.040	-0.6934	7.4346	106.6547
0.060	-0.569	0.060	-0.5281	8.8520	35.0883
0.080	-0.304	0.080	-0.3537	8.1084	-109.4494
0.100	-0.172	0.100	-0.2171	5.3742	-163.9747
0.120	-0.099	0.120	-0.1407	2.3552	-137.9184
0.140	-0.104	0.140	-0.1144	0.6119	-36.4123
0.160	-0.091	0.160	-0.1014	1.0887	84.0947
0.180	-0.134	0.180	-0.0535	4.1694	223.9700
0.200	0.074	0.200	0.0744	8.5963	218.7207
0.220	0.275	0.220	0.2896	12.9050	212.1434
0.240	0.558	0.240	0.5879	16.8142	178.7752
0.260	0.944	0.260	0.9541	19.5126	91.0670
0.280	1.430	0.280	1.3555	20.2723	-15.0915
0.300	1.848	0.300	1.7598	20.2470	12.5654
0.320	2.154	0.320	2.1796	22.3577	198.4966
0.340	2.649	0.340	2.6758	27.7320	338.9265
0.360	3.166	0.360	3.3044	35.4376	431.6318
0.380	3.848	0.380	4.0891	42.5071	275.3147
0.400	5.059	0.400	4.9550	42.1158	-314.4382
0.420	5.961	0.420	5.7075	31.7965	-717.4834
0.440	6.384	0.440	6.2035	17.9714	-605.0220
0.460	6.406	0.460	6.4550	8.4405	-288.0718

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR KINEMATICS OF SHOULDER

INPUT		OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY
			X-COORDINATES OF SHOULDER	ACCELERATION
0.0	0.409	0.0	0.4052	0.0
0.020	0.418	0.020	0.4195	0.1681
0.040	0.436	0.040	0.4339	0.2471
0.060	0.448	0.060	0.4484	0.4355
0.080	0.465	0.080	0.4630	0.5966
0.100	0.479	0.100	0.4779	0.8519
0.120	0.493	0.120	0.4932	1.1787
0.140	0.524	0.140	0.5089	1.4742
0.160	0.539	0.160	0.5252	2.4664
0.180	0.537	0.180	0.5426	4.0662
0.200	0.557	0.200	0.5616	5.4133
0.220	0.576	0.220	0.5827	6.5637
0.240	0.600	0.240	0.6065	7.4056
0.260	0.619	0.260	0.6332	7.9739
0.280	0.637	0.280	0.6630	7.9074
0.300	0.691	0.300	0.6959	6.6274
0.320	0.739	0.320	0.7314	5.1322
0.340	0.773	0.340	0.7691	3.9692
0.360	0.821	0.360	0.8083	2.9999
0.380	0.853	0.380	0.8488	2.6035
0.400	0.880	0.400	0.8903	2.3735
0.420	0.927	0.420	0.9327	1.6738
0.440	0.976	0.440	0.9758	0.7213
0.460	1.044	0.460	1.0192	-0.2081

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR KINEMATICS OF SHOULDER

INPUT		OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY
			Y-COORDINATES OF SHOULDER	ACCELERATION
0.0	0.360	0.0	0.3435	0.0
0.020	0.323	0.020	0.3396	22.6382
0.040	0.333	0.040	0.3432	21.8954
0.060	0.357	0.060	0.3546	6.5820
0.080	0.376	0.080	0.3688	-5.2672
0.100	0.383	0.100	0.3816	-7.5223
0.120	0.385	0.120	0.3915	-7.8386
0.140	0.399	0.140	0.3976	-17.7467
0.160	0.413	0.160	0.3967	-25.8652
0.180	0.380	0.180	0.3870	-11.2225
0.200	0.374	0.200	0.3722	-6.1210
0.220	0.347	0.220	0.3552	1.9657
0.240	0.334	0.240	0.3381	-1.1624
0.260	0.325	0.260	0.3203	-9.8343
0.280	0.315	0.280	0.2989	-11.4617
0.300	0.269	0.300	0.2745	9.5175
0.320	0.249	0.320	0.2535	23.2910
0.340	0.238	0.340	0.2413	31.0634
0.360	0.233	0.360	0.2412	33.7419
0.380	0.256	0.380	0.2539	25.5204
0.400	0.284	0.400	0.2770	20.5579
0.420	0.289	0.420	0.3090	24.7341
0.440	0.356	0.440	0.3491	1.9754
0.460	0.409	0.460	0.3905	-11.6509

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINKAGE VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## ELBOW KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	2.7600	-1.0037	7.0334	19.3414
2	2.8897	-0.4916	8.2081	42.3879
3	3.1386	0.2691	13.7915	45.5585
4	3.5381	1.0071	16.1536	41.7178
5	4.0139	1.7665	15.7643	50.6884
6	4.3503	2.8396	-0.7345	75.7350
7	4.1196	4.3537	-40.8368	96.7545
8	2.8286	5.8583	-99.0846	75.9645
9	0.3609	6.4264	-138.6644	8.0512
10	-2.4327	5.2892	-103.7080	-79.5806
11	-4.0452	2.8954	-23.0471	-109.9883
12	-4.2537	0.5340	29.9749	-82.7524
13	-3.7795	-1.2877	43.6683	-61.4937
14	-3.1183	-2.9122	51.6695	-60.5815
15	-2.2485	-4.5887	71.6926	-59.3693
16	-0.9296	-6.0525	102.7722	-28.8273
17	1.0769	-6.8226	134.4324	21.8744
18	3.5922	-6.3309	131.4733	102.6754
19	5.6511	-4.3066	63.0156	168.4551
20	6.1324	-1.6196	-34.2556	159.1101
21	5.3812	0.3941	-64.3400	98.7226
22	4.5695	1.5738	-43.7401	64.2314
23	4.2100	2.1726	-19.9823	29.5381
24	4.2411	2.3531	-4.5362	19.0634

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	1.6066	-0.5904	7.0334	19.3414
2	1.6641	-0.2394	5.6578	42.9126
3	1.7750	0.3434	4.9670	46.0394
4	1.9530	0.8258	2.1052	40.1106
5	2.1663	1.1643	-3.8637	44.2911
6	2.3211	1.5000	-21.8141	62.4425
7	2.2320	2.1335	-58.0662	76.4900
8	1.6841	2.6452	-106.8256	54.2330
9	0.6304	2.6470	-137.6149	-6.6667
10	-0.5508	1.9420	-108.4418	-71.1609
11	-1.2004	0.8005	-39.9933	-97.5090
12	-1.2237	-0.2525	11.3787	-77.9251
13	-0.9382	-1.0423	35.0621	-62.2370
14	-0.5632	-1.8126	53.1573	-59.9411
15	-0.0944	-2.6636	78.4805	-53.3031
16	0.5626	-3.3128	109.4560	-16.5500
17	1.5038	-3.4035	136.0286	34.4366
18	2.6517	-2.9426	131.3740	103.0330
19	3.5800	-1.6945	75.3045	152.8052
20	3.8302	-0.1887	0.6926	137.3872
21	3.5308	0.9491	-29.1667	88.1730
22	3.1997	1.7189	-25.1195	62.2587
23	3.0565	2.1306	-16.3951	29.6087
24	3.0729	2.1548	-11.0392	17.9506

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## WRIST KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	4.6934	-0.5559	11.1192	53.8398
2	4.7677	0.2486	9.5135	79.2793
3	4.9710	1.3387	9.2399	88.1052
4	5.3646	2.5253	8.1096	100.6867
5	5.6565	3.7489	-19.0141	105.7935
6	5.5012	4.9179	-54.3750	105.4149
7	4.7839	6.2007	-92.6420	112.8307
8	3.1771	7.4747	-147.1927	84.6133
9	0.5092	7.9877	-184.8226	13.5325
10	-2.4885	7.1661	-154.3883	-68.4964
11	-4.5485	5.4581	-84.5109	-109.8405
12	-5.7518	3.8535	-45.8773	-107.4331
13	-6.9398	2.2117	-27.9935	-146.1072
14	-8.0599	-0.4923	35.2766	-211.8950
15	-8.1702	-4.4103	155.6856	-238.2586
16	-6.6035	-8.5793	285.6262	-187.1924
17	-3.1030	-12.0309	412.7046	-78.9257
18	2.4434	-13.7255	504.2603	121.3192
19	9.2290	-12.0006	462.2515	412.2417
20	14.1651	-5.7801	162.8420	631.9207
21	13.4469	1.7945	-207.2876	491.0581
22	9.2104	5.5176	-259.4475	194.4438
23	6.0417	5.5168	-149.7647	20.1511
24	4.8583	4.4573	-55.9435	6.6792

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE LOWER ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	5.5914	-0.8111	11.1192	53.8398
2	3.6972	-0.1733	7.7101	78.5685
3	3.9266	0.7290	5.8382	86.1196
4	4.3235	1.6600	0.0325	93.9730
5	4.7202	2.6189	-19.5663	105.1271
6	4.8452	3.7333	-48.4647	116.0870
7	4.4053	5.1479	-88.8081	123.4911
8	2.9785	6.5533	-145.8641	90.7744
9	0.4247	7.0978	-184.9592	12.0942
10	-2.4567	6.0963	-153.9074	-84.6769
11	-4.2610	3.9973	-79.5691	-135.0026
12	-4.8979	1.9614	-32.2689	-137.5871
13	-5.1385	0.2171	-9.1621	-166.9588
14	-5.2432	-1.8717	50.3389	-219.2711
15	-4.7948	-4.5120	162.9704	-238.4781
16	-3.3694	-7.1390	293.8931	-183.5109
17	-0.7204	-9.0622	423.7063	-65.2171
18	3.0982	-9.5106	508.6060	149.2932
19	7.1782	-7.0150	449.8470	438.7690
20	9.5865	-3.4080	160.8789	632.9375
21	8.8495	0.9963	-156.8213	499.8206
22	6.5651	3.2696	-207.4353	238.6432
23	4.9976	3.6106	-120.1968	74.1349
24	4.5065	3.2579	-47.2761	36.2290

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## FINGERTIP KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	5.2534	-0.1116	11.7015	38.8812
2	5.3745	0.8702	10.6797	46.1523
3	5.6477	2.1529	2.9413	62.9067
4	5.9998	3.6141	-21.3647	65.5361
5	6.0564	4.8321	-63.5934	15.4731
6	5.6660	5.6652	-89.8497	-46.7270
7	4.8309	6.5328	-110.7814	-100.7099
8	3.1871	7.5613	-152.4111	-150.3937
9	0.5249	8.1420	-192.4751	-172.3375
10	-2.4568	7.7590	-185.0345	-132.7838
11	-4.6395	6.6788	-144.2383	-93.3336
12	-6.2766	5.6146	-126.9611	-97.9249
13	-8.2676	4.2040	-112.8000	-145.8263
14	-10.3267	1.1147	2.9468	-158.7236
15	-10.9903	-3.7936	234.6898	-67.5732
16	-9.4353	-9.1209	468.5391	94.2525
17	-5.7147	-13.8517	699.2097	268.7715
18	0.6699	-17.2538	961.0679	479.7151
19	10.0471	-16.9801	1073.9905	757.6855
20	19.0799	-9.3133	590.5554	950.9883
21	19.2686	3.2352	-387.0054	593.4683
22	11.6752	9.3157	-611.2722	26.0789
23	6.2455	8.0678	-302.2957	-131.9233
24	4.6528	5.6416	-96.5465	-57.0894

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE HAND CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	4.8614	-0.4313	11.7015	38.8812
2	4.9376	0.4058	6.4530	42.2409
3	5.1605	1.5666	-4.0479	54.4987
4	5.5425	2.8302	-23.1776	62.4287
5	5.7665	4.0522	-59.7063	26.0000
6	5.5473	5.1271	-86.2288	-30.3095
7	4.7971	6.2937	-108.7990	-86.7090
8	3.1799	7.4989	-151.9851	-146.6848
9	0.5136	8.0309	-193.3477	-180.9153
10	-2.4796	7.3321	-186.2615	-155.7141
11	-4.5740	5.7999	-142.5719	-115.6966
12	-5.8987	4.3466	-120.7496	-118.7698
13	-7.3117	2.7695	-102.6340	-161.0783
14	-8.6946	-0.0423	10.5638	-164.1236
15	-8.9599	-4.2376	233.1782	-67.2427
16	-7.3964	-8.7309	469.8044	94.4945
17	-3.6343	-12.5407	715.9045	280.4104
18	1.9468	-14.7134	976.6741	510.7629
19	9.4581	-13.3948	1066.8159	801.3545
20	15.5413	-6.7694	567.6360	967.4651
21	15.0770	2.1979	-355.7107	601.2126
22	9.9005	6.5611	-571.2268	87.7856
23	6.0987	6.2311	-296.8662	-63.9564
24	4.8007	4.7889	-101.5969	-27.9890

N.B. DATA FOR SUBJECT 2, PLTCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE WRIST JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	6.42415	26.73364	0.42913
2	3.54272	30.72546	0.82501
3	-2.22227	39.92473	1.46436
4	-12.72451	41.36717	1.74067
5	-32.77875	13.88259	0.78372
6	-47.33963	-20.26521	-0.66456
7	-59.73067	-49.90181	-1.87338
8	-83.43982	-77.17825	-2.74013
9	-106.14787	-89.22537	-2.96637
10	-102.25754	-67.51038	-2.08485
11	-78.27199	-45.85223	-1.67887
12	-66.29155	-48.37288	-2.23835
13	-56.34608	-74.67076	-3.41593
14	5.79955	-81.75139	-1.53988
15	128.01485	-31.70981	4.69028
16	257.92261	57.13251	9.69453
17	393.03149	152.94342	9.70918
18	536.19385	268.75122	0.61025
19	585.68188	421.35693	-19.62160
20	311.63208	527.48022	-21.89188
21	-195.28517	331.20166	10.18982
22	-313.60352	19.70517	6.23188
23	-162.97955	-67.03799	-3.29081
24	-55.77667	-25.95418	-1.89536

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE ELBOW JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	19.32242	100.57198	-2.88934
2	12.48642	133.24916	-3.01117
3	4.55005	151.20763	-3.25714
4	-12.68681	161.76001	-2.23812
5	-55.47565	147.21425	3.58668
6	-103.55869	125.78056	9.71175
7	-162.74605	104.73212	15.70343
8	-252.64218	39.56423	22.06735
9	-320.70044	-63.81187	23.79872
10	-280.79004	-154.35364	16.11430
11	-170.57210	-191.07097	7.66270
12	-103.72345	-196.58969	3.93733
13	-66.97412	-256.95850	2.73734
14	64.19261	-324.72144	10.40244
15	317.06030	-296.95972	39.85628
16	598.83838	-144.35587	80.03282
17	884.53052	88.67580	109.20313
18	1126.17651	453.31519	95.93506
19	1107.55054	941.71289	17.89566
20	498.25146	1273.07153	-30.99539
21	-377.19775	922.57744	44.31221
22	-554.22827	307.91528	63.93832
23	-302.40771	30.34268	30.68355
24	-110.61696	27.45573	7.54690

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE SHOULDER JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	34.65518	142.73619	-22.91824
2	24.82045	226.79869	-19.02849
3	15.37820	251.57349	-8.46527
4	-8.09750	249.20114	9.61666
5	-63.89845	243.76894	41.42580
6	-151.11336	261.90503	75.59497
7	-289.33228	271.48022	104.23155
8	-485.52197	157.73215	87.98000
9	-620.70093	-78.34538	-6.26047
10	-517.19312	-309.48438	-103.22878
11	-257.75732	-403.64038	-98.82651
12	-78.91788	-366.46631	-47.08772
13	9.46130	-392.63501	-0.15131
14	180.07561	-455.39307	90.01830
15	488.14771	-413.16040	203.17328
16	837.45239	-180.44798	229.34012
17	1181.07275	163.74748	112.84683
18	1412.57178	677.92700	-172.40680
19	1271.71411	1274.82813	-475.00586
20	499.76123	1572.57568	-396.46948
21	-440.78101	1114.59448	70.98665
22	-608.98877	443.63916	228.15062
23	-338.14893	95.02036	129.46938
24	-134.79138	60.58809	47.60049

N.B. DATA FOR SUBJECT 2, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS ANGULAR KINEMATICS OF THE UPPER ARM

INPUT

OUTPUT

X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-1.192	0.0	-1.2268	7.3075	0.0
0.020	-1.091	0.020	-1.0790	7.5634	25.5915
0.040	-0.914	0.040	-0.9215	8.2425	42.3129
0.060	-0.737	0.060	-0.7467	9.3119	64.6329
0.080	-0.549	0.080	-0.5456	10.8959	93.7690
0.100	-0.308	0.100	-0.3071	13.0379	120.4348
0.120	-0.082	0.120	-0.0205	15.7102	146.7868
0.140	0.260	0.140	0.3218	18.4589	128.0873
0.160	0.676	0.160	0.7123	20.3801	64.0391
0.180	1.188	0.180	1.1267	20.7513	-26.9219
0.200	1.599	0.200	1.5333	19.7513	-73.0882
0.220	1.930	0.220	1.9138	18.3098	-71.0464
0.240	2.299	0.240	2.2667	17.0260	-57.3406
0.260	2.592	0.260	2.5933	16.2563	-19.6300
0.280	2.891	0.280	2.9217	16.1946	13.4605
0.300	3.190	0.300	3.2489	16.5674	23.8129
0.320	3.516	0.320	3.5828	16.7113	-9.4114
0.340	3.930	0.340	3.9097	15.6972	-92.0048
0.360	4.316	0.360	4.2007	13.1631	-159.4074
0.380	4.511	0.380	4.4337	10.1725	-141.6544
0.400	4.553	0.400	4.6138	8.0835	-67.2494
0.420	4.726	0.420	4.7639	7.0314	-37.9453
0.440	4.884	0.440	4.8971	6.2889	-36.3197
0.460	5.087	0.460	5.0151	5.4807	-44.4944

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE LOWER ARM

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-0.823	0.0	-0.6339	7.1741	0.0
0.020	-0.702	0.020	-0.6888	7.4041	23.0024
0.040	-0.551	0.040	-0.5364	7.8267	19.2617
0.060	-0.396	0.060	-0.3782	7.8809	-13.8455
0.080	-0.204	0.080	-0.2280	6.9177	-82.4735
0.100	-0.060	0.100	-0.1074	5.0732	-101.9807
0.120	-0.020	0.120	-0.0220	3.6898	-36.3593
0.140	0.043	0.140	0.0493	3.6679	34.1767
0.160	0.119	0.160	0.1333	4.9814	92.1676
0.180	0.253	0.180	0.2524	7.0705	121.7401
0.200	0.417	0.200	0.4201	9.8048	151.6993
0.220	0.630	0.220	0.6481	13.0741	175.2312
0.240	0.907	0.240	0.9446	16.5670	174.0635
0.260	1.336	0.260	1.3056	19.2792	97.1477
0.280	1.726	0.280	1.7096	21.0771	82.6397
0.300	2.178	0.300	2.1490	22.9172	101.3729
0.320	2.624	0.320	2.6327	25.7165	178.5560
0.340	3.094	0.340	3.1668	29.8673	238.5264
0.360	3.734	0.360	3.8236	33.3698	109.7122
0.380	4.500	0.380	4.4922	32.4521	-201.4714
0.400	5.191	0.400	5.0812	25.4620	-497.5476
0.420	5.628	0.420	5.4862	14.7932	-569.3242
0.440	5.689	0.440	5.6827	5.5858	-351.4182
0.460	5.685	0.460	5.7396	0.8735	-119.8129

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE HAND SEGMENT

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-0.095	0.0	-0.6649	11.8160	0.0
0.020	-0.403	0.020	-0.4348	10.8886	-92.7390
0.040	-0.231	0.040	-0.2358	8.9996	-96.1641
0.060	-0.055	0.060	-0.0744	7.1754	-86.2522
0.080	0.012	0.080	0.0561	6.0876	-22.5262
0.100	0.165	0.100	0.1693	5.0299	-83.2495
0.120	0.305	0.120	0.2484	2.6387	-155.8679
0.140	0.530	0.140	0.2759	0.3989	-68.1116
0.160	0.788	0.160	0.2862	1.4387	172.0939
0.180	0.350	0.180	0.3469	4.4978	133.8141
0.200	0.493	0.200	0.4617	6.8922	105.6245
0.220	0.655	0.220	0.6246	9.5926	164.4144
0.240	0.741	0.240	0.8590	14.3273	309.0576
0.260	1.227	0.260	1.1948	18.6300	121.2023
0.280	1.606	0.280	1.5852	20.0878	24.5818
0.300	2.070	0.300	1.9893	20.1914	-14.2224
0.320	2.433	0.320	2.4030	21.8060	175.6788
0.340	2.867	0.340	2.8925	28.0666	450.3796
0.360	3.396	0.360	3.5575	39.1019	653.1543
0.380	4.177	0.380	4.4537	49.6996	406.6184
0.400	5.546	0.400	5.4604	47.5418	-622.3970
0.420	6.520	0.420	6.2346	27.2737	-1404.4023
0.440	6.646	0.440	6.5008	-0.5755	-1380.5200
0.460	6.061	0.460	6.2798	-18.1886	-380.7979

N.B. DATA FOR SUBJECT 3, FITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR KINEMATICS OF SHOULDER

INPUT		OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY
X-COORDINATES OF SHOULDER				
0.0	0.144	0.0	0.1293	0.8012
0.020	0.155	0.020	0.1454	0.8057
0.040	0.165	0.040	0.1616	0.8225
0.060	0.172	0.060	0.1784	0.8559
0.080	0.190	0.080	0.1960	0.9051
0.100	0.225	0.100	0.2147	0.9660
0.120	0.237	0.120	0.2347	1.0398
0.140	0.250	0.140	0.2564	1.1305
0.160	0.272	0.160	0.2800	1.2370
0.180	0.305	0.180	0.3059	1.3550
0.200	0.327	0.200	0.3343	1.4819
0.220	0.355	0.220	0.3653	1.6153
0.240	0.395	0.240	0.3989	1.7499
0.260	0.428	0.260	0.4352	1.8815
0.280	0.453	0.280	0.4741	2.0070
0.300	0.510	0.300	0.5154	2.1175
0.320	0.560	0.320	0.5587	2.2047
0.340	0.610	0.340	0.6034	2.2670
0.360	0.665	0.360	0.6492	2.3070
0.380	0.763	0.380	0.6955	2.3315
0.400	0.752	0.400	0.7424	2.3481
0.420	0.784	0.420	0.7895	2.3621
0.440	0.822	0.440	0.8369	2.3749
0.460	0.906	0.460	0.8845	2.3798
				ACCELERATION
				0.0
				0.4560
				1.2263
				2.1166
				2.8018
				3.2886
				4.0992
				4.9809
				5.6734
				6.1315
				6.5634
				6.7775
				6.6881
				6.4891
				6.0650
				4.9899
				3.7306
				2.5058
				1.4909
				0.9664
				0.6867
				0.7169
				0.5596
				-0.0610

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR KINEMATICS OF SHOULDER

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
Y-COORDINATES OF SHOULDER					
0.0	0.410	0.0	0.4149	0.6146	0.0
0.020	0.422	0.020	0.4271	0.6046	-1.0015
0.040	0.441	0.040	0.4389	0.5638	-3.0737
0.060	0.453	0.060	0.4494	0.4866	-4.6522
0.080	0.455	0.080	0.4582	0.3858	-5.4297
0.100	0.452	0.100	0.4647	0.2620	-6.9499
0.120	0.477	0.120	0.4683	0.0800	-11.2418
0.140	0.474	0.140	0.4675	-0.1694	-13.6978
0.160	0.466	0.160	0.4613	-0.4542	-14.7837
0.180	0.456	0.180	0.4492	-0.7496	-14.7551
0.200	0.441	0.200	0.4314	-1.0296	-13.2419
0.220	0.416	0.220	0.4084	-1.2580	-9.5959
0.240	0.388	0.240	0.3810	-1.4094	-5.5427
0.260	0.355	0.260	0.3526	-1.4660	-0.1222
0.280	0.332	0.280	0.3237	-1.4082	5.9063
0.300	0.290	0.300	0.2972	-1.2125	13.6594
0.320	0.264	0.320	0.2761	-0.8765	19.9354
0.340	0.259	0.340	0.2623	-0.4417	23.5417
0.360	0.246	0.360	0.2589	0.0574	26.3743
0.380	0.253	0.380	0.2653	0.5856	26.4393
0.400	0.253	0.400	0.2822	1.0894	23.9438
0.420	0.311	0.420	0.3082	1.4819	15.3027
0.440	0.355	0.440	0.3403	1.7076	7.2667
0.460	0.387	0.460	0.3756	1.8049	2.4629

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## ELBOW KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	3.0714	1.4279	-10.4340	22.4440
2	3.0058	1.7833	-5.5875	25.7206
3	2.9890	2.2085	-5.8558	30.0059
4	2.9431	2.7420	-8.9302	38.4077
5	2.7709	3.4595	-18.8359	51.2133
6	2.2666	4.3632	-41.5839	60.4863
7	1.1401	5.2633	-77.5949	55.1927
8	-0.7961	5.6053	-111.9300	11.7059
9	-3.1587	4.6358	-102.6177	-63.1651
10	-4.8286	2.1926	-31.3455	-118.7717
11	-5.0314	-0.7849	46.1689	-113.5243
12	-4.0750	-3.2901	59.0978	-76.3240
13	-2.5623	-5.0113	106.5332	-37.0373
14	-0.8519	-6.0580	108.3192	-9.0758
15	0.8411	-6.6237	112.3640	15.1931
16	2.7032	-6.6483	115.9762	50.6332
17	4.5598	-5.8631	100.3840	98.9448
18	5.8659	-4.1675	46.8298	137.4560
19	6.1007	-2.0726	-17.0529	132.5507
20	5.5589	-0.3379	-40.5388	95.8472
21	5.0026	0.8268	-28.0811	66.5674
22	4.6794	1.6015	-23.0492	47.5603
23	4.4149	2.0888	-24.3580	32.8302
24	4.1063	2.3440	-26.9236	20.5914

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	1.7910	0.9692	-10.4340	22.4440
2	1.7649	1.1185	-9.7860	23.4712
3	1.7671	1.2809	-12.1283	25.2440
4	1.7659	1.4699	-17.1005	29.5786
5	1.7186	1.7259	-27.8917	36.2944
6	1.5351	2.0501	-48.3600	39.1197
7	1.0861	2.3399	-78.1549	27.8735
8	0.2905	2.3501	-104.3898	-10.9098
9	-0.6795	1.7650	-94.8274	-72.1858
10	-1.3410	0.5332	-35.8701	-116.6189
11	-1.3579	-0.9229	32.5753	-113.0137
12	-0.8657	-2.1440	76.6449	-80.7711
13	-0.1302	-2.9798	98.3425	-43.8790
14	0.6723	-3.4681	106.4304	-12.2032
15	1.4987	-3.6821	112.9106	17.6360
16	2.3729	-3.5825	115.5013	55.0397
17	3.2315	-3.0507	101.1321	97.3609
18	3.8362	-2.0662	58.7267	125.1418
19	3.9608	-0.8713	8.8164	118.0240
20	3.7387	0.1830	-15.1914	88.5941
21	3.5055	0.9749	-15.6255	65.3350
22	3.3724	1.5341	-15.9962	47.9242
23	3.2643	1.8738	-17.7132	34.0716
24	3.1326	2.0400	-19.0187	23.0598

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## WRIST KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	4.5589	2.7778	-30.3619	55.1499
2	4.3250	3.3837	-26.5468	62.7047
3	4.1090	4.0922	-35.1281	66.8014
4	3.7579	4.7927	-48.1323	64.4208
5	3.2086	5.3463	-61.0389	50.9142
6	2.4189	5.7755	-73.9447	44.3676
7	1.1668	6.2962	-101.0498	49.3271
8	-0.6467	6.6351	-136.7384	18.1582
9	-3.3423	6.0044	-135.6580	-54.0694
10	-5.3229	4.1096	-68.9136	-123.3996
11	-6.1512	1.7217	11.9637	-135.0532
12	-6.2850	-0.3716	64.3369	-119.3794
13	-6.3208	-2.2926	105.0248	-113.1899
14	-6.1013	-4.0432	171.5854	-119.5749
15	-5.0037	-7.4405	246.2709	-93.4717
16	-2.6700	-10.1550	324.9287	-26.0801
17	1.0516	-12.1513	388.5164	82.3315
18	6.2438	-12.5274	424.2556	257.3501
19	11.9902	-9.3259	313.5154	508.8123
20	14.4262	-2.3223	-20.2248	576.3264
21	11.6525	3.3972	-244.5237	313.0352
22	7.6421	4.4962	-203.5836	49.2070
23	5.2966	3.3792	-98.8317	-18.7567
24	4.2323	2.5533	-46.5056	-4.4230

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE LOWER ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	3.7110	2.0083	-30.3619	55.1499
2	3.5724	2.4715	-28.8804	59.8707
3	3.4700	3.0185	-36.6942	64.1590
4	3.2934	3.6238	-47.3163	60.4744
5	2.9591	4.2708	-58.0642	63.7364
6	2.3321	4.9705	-72.2000	60.5500
7	1.1558	5.7074	-100.9223	55.1286
8	-0.8179	6.0504	-136.4698	12.7102
9	-3.2377	5.2243	-133.7026	-68.6485
10	-5.0411	3.0169	-64.0622	-142.2139
11	-5.5129	0.2929	121.8385	-157.1591
12	-5.0253	-2.0351	81.2201	-141.6752
13	-4.1785	-3.8423	127.5338	-129.4718
14	-3.1319	-5.4496	136.5461	-123.6388
15	-1.6721	-6.9749	259.3330	-91.6463
16	0.3926	-8.1562	338.4783	-17.2384
17	3.0514	-6.5670	402.4001	107.2186
18	6.0284	-7.7622	422.5364	295.3801
19	8.6329	-5.1915	302.4773	522.4050
20	9.3718	-1.1912	11.1538	569.3040
21	7.8621	1.9321	-170.4557	341.6648
22	5.9533	2.8462	-136.5913	112.7073
23	4.7949	2.6436	-67.1406	27.5131
24	4.1606	2.4340	-36.6151	11.9427

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPPOINTS

KINEMATICS OF THE HAND CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	4.8420	3.1389	-78.4235	35.4547
2	4.5017	3.7672	-79.8223	24.1914
3	4.1906	4.4320	-83.7516	0.8441
4	3.7786	5.0706	-89.8921	-23.9774
5	3.1953	5.5824	-98.6683	-42.6680
6	2.3860	5.9680	-105.9087	-65.5562
7	1.1436	6.3955	-117.1111	-104.0706
8	-0.8569	6.6500	-138.6859	-139.6273
9	-3.3561	6.0560	-146.4592	-134.1363
10	-5.3823	4.2739	-91.8036	-88.9217
11	-6.2704	1.9613	-7.6287	-29.6942
12	-6.5026	-0.0694	53.8147	1.7635
13	-6.7421	-1.9291	110.1857	0.7465
14	-6.7743	-4.3775	236.0337	14.8692
15	-5.7337	-7.4517	395.5867	89.7821
16	-3.3870	-10.4737	553.4573	219.5647
17	0.4816	-12.7775	697.6589	362.0027
18	5.9751	-13.5836	877.4316	555.6150
19	12.6036	-10.7151	882.4163	844.8206
20	16.2921	-2.8161	198.1048	1023.9058
21	15.0059	4.6530	-636.9829	522.8193
22	7.6935	5.5541	-431.9099	-44.6243
23	5.3034	3.3574	-65.3557	-154.2405
24	4.2304	1.8470	-45.9986	-138.1290

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

FINGERTIP KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	5.5701	4.0675	-78.4235	35.4547
2	4.9597	4.7534	-83.7235	15.7919
3	4.4006	5.3059	-85.9952	-8.4935
4	3.8319	5.7852	-90.5323	-32.5671
5	3.1612	6.1693	-98.5421	-44.9140
6	2.3013	6.4631	-104.5077	-73.7509
7	1.0788	6.6509	-113.2839	-119.1584
8	-0.6618	6.6883	-136.8331	-146.1720
9	-3.3986	6.1958	-151.3118	-117.6496
10	-5.5350	4.6963	-96.3467	-76.3545
11	-6.5770	2.5775	-12.3278	-20.2506
12	-7.0630	0.7076	44.2131	15.0824
13	-7.8255	-0.9945	86.8161	20.9060
14	-8.5043	-3.6944	224.7754	19.3134
15	-7.7895	-7.4807	393.1321	89.7467
16	-5.2294	-11.2931	554.7551	220.1419
17	-0.9845	-14.3876	685.8469	349.0310
18	5.2842	-16.3061	866.3447	512.0261
19	14.1811	-14.2671	908.7664	785.1533
20	21.0901	-4.0558	237.3599	1013.5176
21	16.4862	7.6823	-682.5452	480.5425
22	7.8257	8.2746	-438.7175	-184.7083
23	5.3159	3.5012	-55.5889	-288.8528
24	4.2243	0.0306	-46.1256	-176.1568

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



## KINEMATICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE WRIST JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-43.83875	25.30521	1.82386
2	-44.62068	14.31367	1.07460
3	-46.81712	0.73816	0.28725
4	-50.24969	-12.71896	-0.49591
5	-55.15556	-19.62090	-0.91969
6	-59.20290	-35.74072	-1.89881
7	-65.46510	-61.12349	-3.19413
8	-77.52541	-70.22411	-3.78556
9	-81.87070	-60.28009	-2.84753
10	-51.31818	-37.19614	-1.80591
11	-4.26445	-5.63407	-0.09495
12	30.06241	13.91708	1.40442
13	61.59380	17.17282	2.77844
14	131.94284	16.28218	5.20687
15	221.13295	55.65440	8.59811
16	309.38257	128.54536	8.92486
17	335.59121	200.59436	4.73942
18	450.43413	291.70825	-5.50912
19	493.27051	444.38647	-22.40260
20	119.74055	572.04199	-9.14160
21	-356.07324	274.10889	16.30707
22	-241.43764	-97.76587	-5.75280
23	-47.71384	-155.98267	-8.68944
24	-25.71321	-92.98561	-4.26281

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



KINEMATICS OF THE UPPER EXTREMITY

FORCES AND MOMENTS AT THE ELBOW JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-80.18193	103.06689	6.15221
2	-79.19049	97.72617	6.11320
3	-90.74600	89.28384	6.96880
4	-106.88731	78.59816	7.89450
5	-124.65842	68.41893	7.23761
6	-145.62633	48.48491	8.98144
7	-186.26910	16.61278	14.01700
8	-240.87967	-49.26262	16.74594
9	-241.91264	-130.70529	11.59878
10	-128.00064	-195.67868	5.70176
11	21.37625	-182.20609	2.16863
12	127.30284	-143.92073	4.83716
13	214.25174	-126.05751	15.37870
14	355.24072	-119.96603	40.47067
15	551.55420	-42.29877	72.76207
16	714.54077	119.65842	101.98312
17	671.65382	346.68213	108.47112
18	996.225977	657.02539	71.86400
19	855.33569	1081.45215	-11.96455
20	124.09167	1265.24585	-6.09233
21	-560.10864	694.82861	77.50131
22	-407.33150	48.69209	57.00638
23	-128.08113	-111.29616	31.97737
24	-69.54147	-66.94290	20.74944

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# KINEMATICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE SHOULDER JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	-103.44977	153.11690	48.11252
2	-101.01329	150.06691	51.26271
3	-117.79210	145.57799	57.55948
4	-145.02133	144.55832	62.99602
5	-186.85693	149.35532	64.53595
6	-253.46907	135.72173	58.05267
7	-360.55420	78.78180	33.42957
8	-473.66870	-73.59154	-34.92737
9	-453.37769	-291.67944	-109.23663
10	-207.99104	-455.73828	-87.24393
11	94.51912	-434.22656	14.60844
12	296.22070	-324.04028	90.69180
13	433.55542	-223.90775	128.29601
14	592.58032	-147.17915	155.54066
15	783.34448	-2.96594	127.32693
16	972.10840	242.39699	16.45152
17	1057.18823	557.79666	-158.34117
18	1127.22021	936.09131	-356.47876
19	874.99609	1344.64551	-457.31299
20	90.21495	1462.81055	-166.56305
21	-594.95337	840.52503	240.31522
22	-443.00269	155.76312	197.16542
23	-167.58144	-35.31642	73.57892
24	-111.95314	-15.51947	43.12593

N.B. DATA FOR SUBJECT 3, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS ANGULAR KINEMATICS OF THE UPPER ARM

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-2.151	0.0	-2.1732	6.6602	0.0
0.020	-2.022	0.020	-2.0380	6.9585	29.8295
0.040	-1.917	0.040	-1.8895	8.0713	81.4518
0.060	-1.739	0.060	-1.7108	9.8405	95.4690
0.080	-1.491	0.080	-1.4965	11.5102	71.4996
0.100	-1.234	0.100	-1.2531	12.7802	55.5056
0.120	-0.993	0.120	-0.9857	13.9901	65.4779
0.140	-0.682	0.140	-0.6928	15.3051	66.0284
0.160	-0.376	0.160	-0.3725	16.7753	80.9886
0.180	-0.031	0.180	-0.0200	18.5016	91.6456
0.200	0.328	0.200	0.3681	20.2952	87.7168
0.220	0.600	0.220	0.7875	21.4552	28.2820
0.240	1.233	0.240	1.2194	21.5914	-14.6685
0.260	1.678	0.260	1.6467	21.0532	-39.1471
0.280	2.109	0.280	2.0612	20.4563	-20.5428
0.300	2.425	0.300	2.4718	20.8878	63.6898
0.320	2.814	0.320	2.9036	22.3617	83.7031
0.340	3.283	0.340	3.3607	23.0047	-19.4009
0.360	3.904	0.360	3.8030	20.5172	-229.3529
0.380	4.305	0.380	4.1627	15.2151	-300.8684
0.400	4.428	0.400	4.4150	10.4363	-177.0016
0.420	4.514	0.420	4.5979	8.3181	-34.8228
0.440	4.743	0.440	4.7591	7.8932	-7.6614
0.460	4.913	0.460	4.9158	7.7953	-2.1280

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE LOWER ARM

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-2.124	0.0	-2.1502	6.5763	0.0
0.020	-2.022	0.020	-2.0122	7.5419	96.5592
0.040	-1.876	0.040	-1.8380	10.0855	157.7966
0.060	-1.588	0.060	-1.6098	12.4803	81.6858
0.080	-1.362	0.080	-1.3437	14.1337	83.6552
0.100	-1.044	0.100	-1.0486	15.1681	19.7903
0.120	-0.732	0.120	-0.7444	15.0952	-27.0866
0.140	-0.456	0.140	-0.4481	14.5208	-30.3543
0.160	-0.161	0.160	-0.1659	13.5992	-61.8093
0.180	0.125	0.180	0.0929	12.2336	-74.7440
0.200	0.317	0.200	0.3296	11.7822	29.6033
0.220	0.563	0.220	0.5750	12.9460	86.7712
0.240	0.859	0.240	0.8570	15.5435	172.9838
0.260	1.132	0.260	1.2087	19.9454	267.2007
0.280	1.644	0.280	1.6487	23.4385	82.1136
0.300	2.195	0.300	2.1206	23.0744	-118.5194
0.320	2.618	0.320	2.5630	21.4060	-48.3302
0.340	2.972	0.340	2.9995	23.1464	222.3792
0.360	3.417	0.360	3.5182	29.2890	391.8818
0.380	4.071	0.380	4.1692	35.1466	193.8770
0.400	4.961	0.400	4.8740	33.4848	-360.0627
0.420	5.549	0.420	5.4558	23.9024	-598.1655
0.440	5.864	0.440	5.8208	12.9283	-499.2612
0.460	5.992	0.460	5.9966	5.5160	-241.9638

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# SEGMENTAL ANALYSIS PROGRAM-3 SEGMENTS

## ANGULAR KINEMATICS OF THE HAND SEGMENT

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
0.0	-2.106	0.0	-2.1602	3.6506	0.0
0.020	-2.123	0.020	-2.0713	6.0373	238.6722
0.040	-1.928	0.040	-1.9037	10.6806	225.6500
0.060	-1.644	0.060	-1.6528	14.0129	107.5775
0.080	-1.369	0.080	-1.3562	15.3918	30.3084
0.100	-0.992	0.100	-1.0512	14.6678	-102.7035
0.120	-0.792	0.120	-0.7699	13.8899	24.9156
0.140	-0.526	0.140	-0.4851	14.6796	54.0559
0.160	-0.144	0.160	-0.1907	14.2647	-95.5472
0.180	0.038	0.180	0.0793	12.9320	-37.7288
0.200	0.403	0.200	0.3221	10.9314	-162.3276
0.220	0.523	0.220	0.5238	10.0078	69.9676
0.240	0.665	0.240	0.7531	13.6840	297.6594
0.260	1.151	0.260	1.0757	18.0441	138.3376
0.280	1.338	0.280	1.4757	22.5232	309.5754
0.300	2.026	0.300	1.9590	24.3667	-125.2225
0.320	2.549	0.320	2.4120	20.4563	-265.8131
0.340	2.823	0.340	2.7989	19.7911	199.2978
0.360	3.130	0.360	3.2727	29.4842	770.0103
0.380	3.674	0.380	4.0126	44.3226	713.8262
0.400	5.287	0.400	4.9386	43.1183	-834.2559
0.420	5.737	0.420	5.6332	26.2962	-347.9487
0.440	5.871	0.440	6.0192	13.7772	-403.9565
0.460	6.387	0.460	6.1999	3.5981	-613.9399

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



LINER KINEMATICS OF SHOULDER

INPUT			OUTPUT		
X	F	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
X-COORDINATES OF SHOULDER					
0.0	0.735	0.0	0.7339	2.2359	0.0
0.020	0.776	0.020	0.7802	2.4729	23.6982
0.040	0.834	0.040	0.8308	2.4076	-30.2296
0.060	0.877	0.060	0.8734	1.8782	-22.7066
0.080	0.914	0.080	0.9120	2.2515	60.0364
0.100	0.951	0.100	0.9776	4.7459	189.3961
0.120	1.110	0.120	1.0842	4.5970	-204.2789
0.140	1.141	0.140	1.1431	1.6891	-86.5124
0.160	1.165	0.160	1.1644	0.6788	-14.5112
0.180	1.172	0.180	1.1813	1.3306	79.6841
0.200	1.225	0.200	1.2173	1.9309	-19.6520
0.220	1.254	0.220	1.2558	2.1217	38.7288
0.240	1.310	0.240	1.3075	3.1134	60.4463
0.260	1.371	0.260	1.3861	4.9625	124.4603
0.280	1.514	0.280	1.4950	5.1707	-103.6367
0.300	1.575	0.300	1.5870	4.4874	35.3022
0.320	1.684	0.320	1.6774	4.2409	-59.9474
0.340	1.752	0.340	1.7531	3.4724	-16.9046
0.360	1.820	0.360	1.8210	3.3978	9.4428
0.380	1.888	0.380	1.8917	3.7181	22.5854
0.400	1.973	0.400	1.9668	3.6085	-33.5449
0.420	2.034	0.420	2.0362	3.5246	25.1620
0.440	2.106	0.440	2.1133	4.2579	48.1576
0.460	2.209	0.460	2.2006	4.1082	-63.1164

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR KINEMATICS OF SHOULDER

INPUT			OUTPUT		
X	P	TIME	DISPLACEMENT	VELOCITY	ACCELERATION
Y-COORDINATES OF SHOULDER					
0.0	0.581	0.0	0.5799	0.2505	0.0
0.020	0.587	0.020	0.5856	0.3495	9.8962
0.040	0.591	0.040	0.5963	0.8119	36.3470
0.060	0.620	0.060	0.6171	1.1354	-3.9978
0.080	0.636	0.080	0.6386	0.9871	-10.8285
0.100	0.663	0.100	0.6538	0.4149	-46.3938
0.120	0.651	0.120	0.6582	0.2885	33.7513
0.140	0.669	0.140	0.6698	0.18280	20.2010
0.160	0.692	0.160	0.6890	1.0246	-0.5415
0.180	0.698	0.180	0.7104	1.1721	15.2862
0.200	0.748	0.200	0.7276	0.0741	-125.0877
0.220	0.702	0.220	0.7114	-1.3267	-14.9869
0.240	0.682	0.240	0.6815	-1.6782	-20.1640
0.260	0.653	0.260	0.6436	-2.1202	-24.0388
0.280	0.583	0.280	0.6038	-1.5013	85.9318
0.300	0.601	0.300	0.5806	-1.3297	-68.7662
0.320	0.537	0.320	0.5473	-1.6514	36.5912
0.340	0.525	0.340	0.5203	-1.1082	17.7258
0.360	0.502	0.360	0.5044	-0.3413	58.9684
0.380	0.509	0.380	0.5104	0.9932	74.4849
0.400	0.548	0.400	0.5449	2.4434	70.5310
0.420	0.594	0.420	0.6100	4.1604	101.1703
0.440	0.712	0.440	0.7020	4.4714	-70.0742
0.460	0.767	0.460	0.7748	2.6783	-109.2367

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## ELBOW KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	4.6780	-1.4289	9.5168	31.1562
2	5.2375	-1.0453	42.8230	40.3623
3	5.8185	-0.3134	6.7208	71.9535
4	6.2144	0.5243	14.2020	51.2261
5	7.3594	1.3673	76.0277	76.2419
6	10.1464	2.1917	184.8498	91.0212
7	9.7870	3.7268	-232.1261	186.7641
8	6.6389	6.0688	-160.6306	135.2371
9	3.3954	7.9778	-135.2258	89.9860
10	1.4950	9.4036	-93.4808	83.7316
11	-1.3160	8.5006	-206.2179	-115.4295
12	-4.6439	5.4099	-86.2610	-105.7434
13	-5.9077	1.6286	31.4107	-149.9662
14	-4.3792	-2.8307	201.4257	-114.9139
15	-2.8595	-5.7885	22.8389	31.7416
16	-1.2831	-8.6166	197.6883	-117.7869
17	1.8954	-11.3220	184.4509	42.7763
18	5.6979	-11.1005	236.5826	157.2324
19	9.0055	-7.5464	101.5870	324.2778
20	9.4913	-2.5441	-52.8660	288.8442
21	8.0489	1.0828	-120.1543	177.6083
22	7.2019	3.7374	-21.3203	162.8471
23	7.7665	4.6352	8.1650	-8.9301
24	7.5057	3.3789	-90.3833	-50.9192

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	3.3006	-0.4817	9.5168	31.1562
2	3.6783	-0.2586	36.1386	43.7344
3	3.8947	0.3213	-12.6928	78.3582
4	3.7688	0.8690	-9.5243	54.5700
5	4.4786	1.1529	58.1323	74.9099
6	7.1014	1.1896	171.6163	86.6691
7	6.8598	1.7876	-245.8261	177.6880
8	3.5856	3.1130	-171.2144	122.4853
9	1.8633	4.0562	-142.6227	71.0532
10	1.4026	4.7610	-93.9417	60.7350
11	0.5141	3.7480	-198.2968	-135.9703
12	-0.8281	1.6105	-81.2310	-110.7518
13	-0.8198	-0.2364	27.9541	-148.6992
14	0.8895	-2.4300	191.6288	-115.6590
15	1.6695	-3.3705	18.2906	29.3134
16	1.9714	-4.5068	207.6119	-105.2554
17	3.2183	-5.8678	189.4028	63.1921
18	4.4428	-5.4649	237.6412	152.4796
19	5.8428	-3.4827	136.9419	278.8518
20	0.2352	-0.5491	11.5206	249.3930
21	5.5445	1.8502	-77.6798	164.5931
22	5.1279	3.9760	-12.6378	161.8483
23	5.7877	4.5428	10.0857	-8.8404
24	5.5895	2.9837	-89.8602	-50.8113

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## WRIST KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	6.3014	-2.4911	25.8989	72.5958
2	7.2491	-1.9958	83.6294	82.8649
3	8.6881	-1.0989	62.7017	147.2872
4	9.8933	0.3808	33.5290	173.7577
5	11.4219	2.3060	67.4799	243.2313
6	14.0266	4.4237	122.8111	306.6902
7	12.8040	7.0021	-343.2375	374.1658
8	7.6849	9.9295	-308.6948	241.8062
9	4.0577	11.9345	-300.5349	127.1840
10	1.1608	12.9970	-250.4356	75.9782
11	-2.4435	11.7893	-347.9480	-135.9569
12	-6.7208	8.6150	-211.7099	-171.2684
13	-9.3736	4.6307	-79.1394	-262.2544
14	-9.8816	-0.7466	142.6027	-284.0862
15	-9.7529	-6.3269	146.9811	-198.7375
16	-7.0871	-12.1731	508.3867	-263.0496
17	-1.5577	-16.6089	547.7776	21.3683
18	4.7311	-17.8599	640.6851	201.7996
19	12.1833	-15.5810	600.4585	573.6125
20	18.3671	-7.9033	273.8699	904.8223
21	17.7982	2.6718	-314.4543	756.4907
22	12.3929	8.5095	-354.6243	339.6431
23	9.4679	6.0486	-161.5916	-18.3414
24	7.9656	4.9398	-137.8049	-75.4506

N.B. DATA FOR SUBJECT 4, FITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE LOWER ARM CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	5.3760	-1.8856	25.8989	72.5958
2	6.1025	-1.4540	68.9494	89.8015
3	7.0524	-0.6511	37.1097	154.2926
4	7.7963	0.4626	19.8040	174.2932
5	9.1063	1.7710	53.7744	240.0644
6	11.8160	3.1514	119.9269	305.0303
7	11.0643	5.1352	-340.1519	377.5159
8	6.8370	7.7289	-306.4834	246.4064
9	3.6802	9.6792	-298.8191	137.4346
10	1.3517	10.9488	-251.6015	88.4922
11	-1.8023	9.9147	-346.3369	-140.6668
12	-5.5370	6.7881	-203.7755	-183.5130
13	-7.3981	2.9195	-57.1532	-281.2983
14	-6.7452	-1.9345	184.6195	-300.0005
15	-5.8237	-6.0200	160.7465	-197.6625
16	-3.7788	-10.1459	491.3943	-273.4622
17	0.4105	-13.5954	543.3337	14.5642
18	5.2822	-14.0070	645.9797	238.8160
19	10.3719	-11.0013	576.2229	634.8887
20	13.3079	-4.8486	245.9621	921.6729
21	12.2411	1.7661	-254.6988	766.2305
22	9.4340	5.7894	-280.5779	407.7148
23	8.4981	6.1030	-124.1411	56.7931
24	7.7034	4.0501	-126.3056	-36.4232

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

FINGERTIP KINEMATICS

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	6.7450	-2.7878	36.0761	50.5225
2	8.0235	-2.4193	128.8493	115.3250
3	10.1639	-1.6092	111.0673	160.4772
4	11.9351	0.2129	46.2209	199.4853
5	13.6205	2.7852	28.9406	278.0669
6	15.8880	5.4885	29.2741	348.3962
7	14.2174	8.4602	-458.2129	-143.1430
8	8.6957	11.8280	-478.6409	-171.1185
9	4.4530	13.9822	-502.6345	-250.7296
10	1.0110	14.8817	-442.4480	-242.8602
11	-2.9495	13.3052	-485.8794	-402.7017
12	-7.4525	9.8819	-315.7224	-277.4353
13	-10.7419	6.6903	-192.2417	-194.3820
14	-12.2029	0.5068	115.6613	-67.9772
15	-13.0309	-6.0140	237.3614	-142.2164
16	-10.3644	-13.5217	854.8118	262.2844
17	-3.5513	-16.6383	959.0449	504.0994
18	3.7589	-20.5851	1038.2976	687.6350
19	12.7467	-19.8546	1200.5708	864.6750
20	23.3241	-12.0767	888.9778	1240.4426
21	23.9415	4.0858	-609.4888	690.5027
22	14.7194	11.5701	-733.8955	-66.2537
23	9.9936	9.9930	-314.6790	-80.9207
24	8.0093	5.4640	-164.9308	-198.4336

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# LINEAR VELOCITIES AND ACCELERATIONS OF SEGMENTAL ENDPOINTS

## KINEMATICS OF THE HAND CENTER OF GRAVITY

FRAME	X-VELOCITY	Y-VELOCITY	X-ACCELERATION	Y-ACCELERATION
1	6.4256	-2.5742	36.0761	50.5225
2	7.4659	-2.1144	106.8076	127.3814
3	9.1013	-1.2418	88.6186	168.2395
4	10.4650	0.3338	34.9349	200.4133
5	12.0375	2.4402	25.8233	277.3877
6	14.5478	4.7218	38.6581	353.7644
7	13.1998	7.4103	-460.0383	-145.0261
8	8.1751	10.4611	-481.2944	-176.1521
9	4.1684	12.5078	-500.7280	-240.8543
10	1.1189	13.5247	-442.7627	-238.9012
11	-2.5852	12.2137	-491.2891	-386.4932
12	-6.9257	8.9697	-312.0388	-283.8130
13	-9.7567	5.0394	-170.8131	-217.2415
14	-10.5316	-0.3956	128.4746	-74.8960
15	-10.6707	-6.2393	209.8210	-145.3121
16	-8.0103	-12.5507	842.6113	257.2942
17	-2.1159	-17.2332	940.3931	483.2417
18	4.4589	-18.6229	1045.3464	707.3943
19	12.5411	-16.7776	1189.9771	945.0339
20	19.7550	-9.0719	831.4968	1288.8367
21	19.5183	3.0677	-523.9092	710.2004
22	13.0443	9.3665	-679.8801	4.8054
23	9.6151	6.5930	-303.5818	-39.8722
24	7.9778	5.0865	-159.5552	-134.0316

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





KINETICS OF THE UPPER EXTREMITY  
FORCES AND MOMENTS AT THE WRIST JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	27.59819	46.15744	-1.98948
2	81.70782	95.73132	-4.19215
3	67.79320	130.27275	-3.77660
4	26.72519	160.11397	-1.34668
5	19.75484	220.22887	1.20869
6	29.57347	274.03052	4.25121
7	-351.92920	-101.99664	7.09458
8	-366.19019	-123.39795	2.70116
9	-383.05688	-184.30043	-4.68481
10	-338.71338	-178.28032	-8.47246
11	-375.83594	-300.55884	-16.96515
12	-238.70969	-204.73027	-11.96204
13	-130.67200	-141.19447	-7.09832
14	98.28307	-44.49483	3.03584
15	206.41309	-101.28784	8.82561
16	644.59741	208.15527	20.87061
17	719.40063	393.14355	6.94029
18	799.68994	533.54834	-9.05239
19	910.33228	668.98389	-30.01141
20	636.69497	956.44604	-43.27295
21	-400.79028	535.74194	18.73053
22	-520.10815	-43.17632	9.26424
23	-232.24005	-54.39662	-0.72288
24	-122.05969	-144.29399	-7.07310

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



KINETICS OF THE UPPER EXTREMITY

FORCES AND MOMENTS AT THE ELBOW JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	71.36731	185.42992	-1.34712
2	198.23219	264.08130	-12.54917
3	130.50851	407.61279	-10.67876
4	60.19386	471.25488	-6.22329
5	110.63362	642.52295	-17.90781
6	232.24989	806.11694	-43.35260
7	-926.70564	552.59033	99.17929
8	-886.14697	309.01401	82.13716
9	-888.06079	64.54955	66.71606
10	-763.91968	-12.14287	33.56236
11	-961.14502	-521.69995	31.46428
12	-583.08984	-498.28125	1.66054
13	-227.26093	-600.00269	-6.50873
14	410.28979	-534.90967	38.59314
15	478.07446	-418.75146	68.37207
16	1475.05347	-237.40996	213.40779
17	1637.63428	434.34229	219.40523
18	1691.39526	953.73267	183.31975
19	1884.14868	1758.53076	60.30132
20	1051.77075	2530.65820	-55.31744
21	-831.23096	1847.25635	104.88644
22	-994.28442	662.44702	122.34450
23	-442.03833	58.16927	37.11214
24	-335.51587	-189.26353	40.49915

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES



# KINETICS OF THE UPPER EXTREMITY

## FORCES AND MOMENTS AT THE SHOULDER JOINT

FRAME	X-JOINT FORCES	Y-JOINT FORCES	MOMENT AT THE JOINT
1	99.44191	277.34058	-88.86542
2	304.84155	393.09766	-172.74065
3	93.06477	638.76929	-126.42302
4	32.09715	632.23608	-57.00288
5	282.12378	863.50708	-72.80551
6	738.51782	1061.79053	-104.96469
7	-1651.97241	1076.77002	754.99097
8	-1391.22949	670.94556	559.28174
9	-1308.79761	274.15625	308.23560
10	-1041.04761	167.02536	74.61775
11	-1546.12036	-922.81226	-448.83472
12	-822.72119	-824.99902	-415.15942
13	-144.79643	-1038.66504	-208.23524
14	975.59473	-876.10352	351.45313
15	532.03174	-332.27686	344.28394
16	2067.50854	-547.91309	827.38086
17	2196.37231	620.75879	197.23097
18	2542.43652	1403.54736	-529.47974
19	2248.12720	2501.14331	-1255.85010
20	1085.75635	3266.36743	-1135.46924
21	-1060.38623	2332.80566	225.26204
22	-1031.56567	1134.89917	523.36206
23	-412.28540	32.09003	228.49144
24	-600.60327	-339.15674	214.12585

N.B. DATA FOR SUBJECT 4, PITCH 1, TIME INTERVAL .02 SECONDS BETWEEN FRAMES





## APPENDIX H

Raw Data for Three Dimensional Analysis



RAW DATA FOR SUBJECT 1.

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\*  
\* CALCULATED X,Y,Z COORDINATES \*  
\* THEIR STANDARD ERROR OF ESTIMATE \*  
\* AND PROBABILITY FACTOR \*  
\*  
\*.....

NUM	X	Y	Z	SX	SY	SZ	PROBA
1	0.42544E+02	0.46022E+01	0.16374E+02	0.73790E+01	0.10117E+01	0.32079E+01	0.0
2	0.25836E+02	0.14201E+02	0.24207E+02	0.17505E+01	0.12500E+01	0.25114E+01	0.99607E+00
3	0.16177E+02	0.10909E+02	0.31022E+02	0.21444E+01	0.20059E+01	0.22521E+01	0.25032E+00
4	0.17402E+02	0.54607E+02	0.13549E+02	0.23457E+01	0.40033E+01	0.27044E+01	0.77717E+00
5	0.26002E+02	0.56177E+01	0.12433E+02	0.46036E+01	0.75240E+00	0.20056E+01	0.15757E+00
6	0.24002E+02	0.22022E+00	0.21144E+02	0.11030E+02	0.76541E+00	0.41757E+01	0.72202E+00
7	0.20552E+02	0.11145E+02	0.25201E+02	0.33569E+01	0.10130E+01	0.23740E+01	0.53441E+00
8	0.17440E+02	0.24902E+02	0.30240E+02	0.22360E+01	0.19270E+01	0.22679E+01	0.3801E+00
9	0.19016E+02	0.50856E+02	0.32379E+02	0.24636E+01	0.42685E+01	0.26144E+01	0.7132E+00
10	0.37720E+02	0.83444E+01	0.15681E+02	0.59591E+01	0.10726E+01	0.26294E+01	0.16054E+01
FIT IS STOPPED AFTER TOO MANY CONSECUTIVE DIVERGENCES. = 11							
11	0.43833E+02	0.25826E+01	0.18130E+02	0.73802E+01	0.92922E+00	0.41014E+01	0.52538E+01
12	0.16044E+02	0.11215E+02	0.29075E+02	0.12394E+01	0.10049E+01	0.25704E+01	0.45552E+00
13	0.16255E+02	0.10453E+02	0.32000E+02	0.23423E+01	0.20550E+01	0.24229E+01	0.25153E+00
14	0.20147E+02	0.59554E+02	0.31069E+02	0.24961E+01	0.41040E+01	0.25444E+01	0.77544E+00

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15	0.73531F+01	0.17594F+02	0.55924E+01	0.3075F+01	0.9114F+00	0.34075F+01	0.24402F+00
16	0.2170F+02	0.11105F+02	0.11105F+02	0.80591E+00	0.46221E+01	0.74380E+00	
17	0.30762F+02	0.31984F+01	0.31984F+01	0.80225E+00	0.23824F+01	0.65401E+00	
18	0.22799E+01	0.22799E+01	0.22799E+01	0.19489F+01	0.24204E+01	0.33057F+00	
19	0.25397E+01	0.25397E+01	0.25397E+01	0.44795E+01	0.26059E+01	0.30805E+00	
20	0.27139F+01	0.27139F+01	0.27139F+01	0.64901E+00	0.27139F+01	0.969F+00	
21	0.27139F+01	0.27139F+01	0.27139F+01	0.82648F+00	0.50933F+01	0.9151F+00	
22	0.27139F+01	0.27139F+01	0.27139F+01	0.82792E+00	0.25320E+01	0.73771E+00	
23	0.27139F+01	0.27139F+01	0.27139F+01	0.20453E+01	0.24947E+01	0.3724E+00	
24	0.27139F+01	0.27139F+01	0.27139F+01	0.44703F+01	0.26551F+01	0.3777E+00	
25	0.27139F+01	0.27139F+01	0.27139F+01	0.66334E+00	0.29793E+01	0.5218E+00	
END OF MANY CONSECUTIVE DIVERGENCES = 11							
26	0.51143E+01	0.20625E+02	0.11540E+02	0.88807E+00	0.54676E+01	0.98270E+01	
27	0.41559E+01	0.42827E+02	0.35575F+01	0.86670F+00	0.27522F+01	0.76570E+00	
28	0.20740F+02	0.30854F+02	0.26042F+01	0.21929E+01	0.27126E+01	0.54135E+00	
29	0.21917E+02	0.52047E+02	0.20732E+01	0.46592E+01	0.27345E+01	0.92208E+00	
30	0.11150F+01	0.31546E+02	0.12129E+01	0.66071E+00	0.31689F+01	0.51142E+00	
31	0.97534F+01	0.64749F+01	0.86909F+01	0.79311E+00	0.46923E+01	0.25267E+00	
32	0.22129F+02	0.32679E+02	0.18121E+01	0.95553E+00	0.29752F+01	0.81638E+00	
33	0.22129F+02	0.32679E+02	0.27203F+01	0.23684E+01	0.27556F+01	0.53579E+00	
34	0.22129F+02	0.32679E+02	0.22849F+02	0.44505E+01	0.27592E+01	0.97470F+00	
35	0.31663E+01	0.43519E+02	0.12533E+02	0.94949E+00	0.62111E+01	0.18249E+00	
36	0.31663E+01	0.43519E+02	0.74659E+02	0.17646E+01	0.27846F+02	0.24208E+00	
37	0.10086F+02	0.75541E+02	0.28605F+01	0.97749F+00	0.31816F+01	0.42674E+00	
38	0.30693E+02	0.35512E+02	0.30283E+01	0.23521E+01	0.30768E+01	0.9508F+00	
39	0.61287F+02	0.32689F+02	0.27793F+01	0.44846E+01	0.28319E+01	0.9761E+00	
40	0.12457F+01	0.42176F+02	0.49542F+01	0.79882E+00	0.44086F+01	0.38524E+00	
41	0.32764E+01	0.72742E+02	0.49367E+02	0.15681E+01	0.23158E+02	0.42512E+00	
42	0.19463E+02	0.37173E+02	0.37465F+01	0.96334E+00	0.32975E+01	0.50393E+00	
43	0.24177F+02	0.35103F+02	0.29566F+01	0.24009E+01	0.25937F+01	0.2424E+00	
44	0.23433F+02	0.31459E+02	0.28571E+01	0.49284E+01	0.27944F+01	0.47542F+00	
45	0.34962F+01	0.41834F+02	0.45220F+02	0.77055E+00	0.40319F+01	0.46120E+00	
46	0.20141E+01	0.66051E+02	0.29320E+02	0.11594E+01	0.14807F+02	0.58504E+00	
47	0.11159E+02	0.35829E+02	0.43227E+01	0.10734E+01	0.37567E+01	0.85138E+00	
48	0.27320F+02	0.37089F+02	0.13013E+01	0.26276E+01	0.33669F+01	0.24347E+00	
49	0.25600F+02	0.31948F+02	0.30616F+01	0.51148E+01	0.29459E+01	0.57930E+00	
50	0.49511E+00	0.42043F+02	0.74099F+01	0.74921E+00	0.35565E+01	0.62191E+00	
51	0.26137E+02	0.54232E+02	0.15037F+02	0.89694E+00	0.75471F+01	0.56111E+00	
52	0.25504E+02	0.39694F+02	0.42949E+01	0.12409E+01	0.38477E+01	0.85961E+00	
53	0.27364E+02	0.37386E+02	0.43417F+01	0.27448E+01	0.32046E+01	0.23558E+00	
54	0.24392F+02	0.31573F+02	0.23247F+01	0.4740E+01	0.28731F+01	0.97289E+00	
55	0.44732F+01	0.42134E+02	0.67713E+01	0.75791E+00	0.34930E+01	0.65712F+00	
56	0.16444F+01	0.44840F+02	0.48521F+01	0.48379F+00	0.42900F+01	0.70275E+00	
57	0.30625F+02	0.15715F+02	0.45804E+01	0.14820E+01	0.41121F+01	0.8764E+00	
58	0.30643F+02	0.34299E+02	0.38019F+01	0.28926F+01	0.36992F+01	0.94307F+00	
59	0.24654E+02	0.45177F+02	0.32652E+01	0.48979E+01	0.22561E+01	0.56677E+00	
60	0.12431F+02	0.46541E+01	0.41894F+02	0.78064F+00	0.36113E+01	0.75777E+00	
61	0.26109F+02	0.70105F+01	0.42560F+02	0.52914E+00	0.51747E+01	0.47267E+00	
62	0.33025F+02	0.18703F+02	0.40670F+02	0.17936F+01	0.43763F+01	0.85000F+00	
63	0.34621F+02	0.45799F+02	0.78231F+02	0.32753E+01	0.39113F+01	0.94356F+00	
64	0.26133F+02	0.43254E+02	0.21702F+02	0.52537F+01	0.29827E+01	0.91850F+00	
65	0.16027F+02	0.70434F+01	0.42576F+02	0.80744E+00	0.39051E+01	0.28022E+00	
66	0.26224F+02	0.48767F+01	0.44335F+02	0.96638E+00	0.50216F+01	0.86210F+00	
67	0.27174F+02	0.21061F+02	0.40526F+02	0.21203F+01	0.41004F+01	0.50049F+00	
68	0.35017F+02	0.37297F+02	0.79134F+02	0.35149F+01	0.41003F+01	0.54539E+00	
69	0.27567F+02	0.46497F+02	0.32766F+02	0.54111E+01	0.21126F+01	0.87231F+00	
70	0.21573F+02	0.85491F+01	0.44132F+02	0.95561E+00	0.43456F+01	0.63563E+00	
71	0.32451E+02	0.12577E+02	0.44031E+02	0.13446E+01	0.51083E+01	0.8115E+00	
72	0.46264F+02	0.24919E+02	0.40562F+02	0.26279E+01	0.47772E+01	0.40540E+00	





73	0.37715E+02	0.40967E+02	0.38915E+02	0.47604E+01	0.40618E+01	0.42950E+01	0.95174E+00
74	0.30422E+02	0.64193E+02	0.31582E+02	0.36299E+01	0.56976E+01	0.32010E+01	0.97241E+00
75	0.31140E+02	0.13175E+02	0.42894E+02	0.55069E+01	0.13528E+01	0.47642E+01	0.07788E+00
76	0.30787E+02	0.12657E+02	0.45126E+02	0.55941E+01	0.13045E+01	0.49546E+01	0.08293E+00
77	0.41513E+02	0.27420E+02	0.42111E+02	0.57713E+01	0.29650E+01	0.50577E+01	0.91075E+00
78	0.37121E+02	0.41573E+02	0.42015E+02	0.47127E+01	0.40991E+01	0.45683E+01	0.95146E+00
79	0.25111E+02	0.64322E+02	0.14057E+02	0.10790E+01	0.52225E+01	0.31070E+01	0.91789E+00
80	0.37627E+02	0.16723E+02	0.42947E+02	0.57077E+01	0.17548E+01	0.49504E+01	0.08757E+00
81	0.41577E+02	0.17615E+02	0.42976E+02	0.54326E+01	0.19753E+01	0.53961E+01	0.08783E+00
82	0.47163E+02	0.31506E+02	0.39748E+02	0.65783E+01	0.36897E+01	0.50731E+01	0.90864E+00
83	0.40525E+02	0.44335E+02	0.29423E+02	0.52320E+01	0.46436E+01	0.45814E+01	0.54630E+00
84	0.31111E+02	0.65024E+02	0.31520E+02	0.57233E+01	0.58564E+01	0.32414E+01	0.57076E+00
85	0.42447E+02	0.21379E+02	0.42194E+02	0.62702E+01	0.23901E+01	0.52757E+01	0.90324E+00
86	0.24901E+02	0.20767E+02	0.44362E+02	0.69110E+01	0.23376E+01	0.55597E+01	0.90144E+00
87	0.49054E+02	0.36558E+02	0.39865E+02	0.64153E+01	0.44129E+01	0.53422E+01	0.91843E+00
88	0.40210E+02	0.47243E+02	0.41568E+02	0.52024E+01	0.49361E+01	0.47887E+01	0.95491E+00
89	0.24197E+02	0.65560E+02	0.33175E+02	0.35046E+01	0.57983E+01	0.32695E+01	0.57281E+00
90	0.46157E+02	0.25065E+02	0.41148E+02	0.66535E+01	0.29214E+01	0.53574E+01	0.90187E+00
91	0.52441E+02	0.27755E+02	0.40784E+02	0.78547E+01	0.35505E+01	0.50181E+01	0.90440E+00
92	0.40716E+02	0.40131E+02	0.40360E+02	0.72304E+01	0.49718E+01	0.55297E+01	0.91907E+00
93	0.41215E+02	0.49244E+02	0.43344E+02	0.54025E+01	0.53303E+01	0.50731E+01	0.95786E+00
94	0.24124E+02	0.66425E+02	0.33213E+02	0.34994E+01	0.58298E+01	0.32735E+01	0.96585E+00
95	0.47540E+02	0.28305E+02	0.41945E+02	0.53228E+01	0.33582E+01	0.55264E+01	0.90402E+00
96	0.54674E+02	0.33277E+02	0.41059E+02	0.80823E+01	0.43450E+01	0.59394E+01	0.90564E+00
97	0.51137E+02	0.44414E+02	0.40453E+02	0.77370E+01	0.57681E+01	0.57449E+01	0.92754E+00
98	0.40103E+02	0.53935E+02	0.44528E+02	0.53145E+01	0.57129E+01	0.51570E+01	0.96501E+00
99	0.30849E+02	0.67074E+02	0.32216E+02	0.36811E+01	0.60191E+01	0.32836E+01	0.96551E+00
100	0.50561E+02	0.32801E+02	0.41271E+02	0.71955E+01	0.40827E+01	0.56911E+01	0.90795E+00
101	0.55535E+02	0.37642E+02	0.39507E+02	0.84185E+01	0.50462E+01	0.58656E+01	0.85907E+00
102	0.52947E+02	0.48103E+02	0.40494E+02	0.76430E+01	0.62089E+01	0.57321E+01	0.52267E+00
103	0.44454E+02	0.57167E+02	0.42740E+02	0.60025E+01	0.64924E+01	0.54238E+01	0.96465E+00
104	0.30458E+02	0.67835E+02	0.31769E+02	0.36490E+01	0.60708E+01	0.32363E+01	0.96551E+00
105	0.54055E+02	0.38912E+02	0.39024E+02	0.99716E+01	0.49819E+01	0.56806E+01	0.90128E+00
106	0.50857E+02	0.42342E+02	0.37625E+02	0.90692E+01	0.59061E+01	0.58395E+01	0.89153E+00
107	0.52310E+02	0.52639E+02	0.40050E+02	0.79085E+01	0.68673E+01	0.57535E+01	0.92471E+00
108	0.45561E+02	0.59976E+02	0.43427E+02	0.62016E+01	0.69466E+01	0.54915E+01	0.91661E+00
109	0.31432E+02	0.66031E+02	0.28750E+02	0.17436E+01	0.62442E+01	0.30604E+01	0.95350E+00
110	0.57121E+02	0.43210E+02	0.37891E+02	0.86146E+01	0.58789E+01	0.55973E+01	0.89831E+00
111	0.56039E+02	0.47793E+02	0.37312E+02	0.48344E+01	0.65966E+01	0.57228E+01	0.88894E+00
112	0.53214E+02	0.56574E+02	0.41166E+02	0.77510E+01	0.73420E+01	0.58560E+01	0.92675E+00
113	0.44531E+02	0.63272E+02	0.44844E+02	0.69405E+01	0.72975E+01	0.55935E+01	0.93557E+00
114	0.20761E+02	0.70009E+02	0.31717E+02	0.16410E+01	0.63229E+01	0.32547E+01	0.96740E+00
115	0.59245E+02	0.48980E+02	0.36312E+02	0.91192E+01	0.68719E+01	0.56859E+01	0.90045E+00
116	0.56541E+02	0.53177E+02	0.35641E+02	0.92761E+01	0.75395E+01	0.56482E+01	0.94176E+00
117	0.57835E+02	0.65555E+02	0.36492E+02	0.88046E+01	0.91150E+01	0.56409E+01	0.92461E+00
118	0.43661E+02	0.66186E+02	0.46515E+02	0.58827E+01	0.74853E+01	0.56959E+01	0.97107E+00
119	0.31212E+02	0.69545E+02	0.29656E+02	0.17254E+01	0.63331E+01	0.30624E+01	0.92366E+00
120	0.6251E+02	0.54537E+02	0.45064E+02	0.91527E+01	0.77666E+01	0.55168E+01	0.94062E+00
121	0.3427E+02	0.60267E+02	0.34373E+02	0.10192E+01	0.89755E+01	0.57407E+01	0.94815E+00
122	0.5424E+02	0.72126E+02	0.37047E+02	0.91143E+01	0.10236E+02	0.58200E+01	0.92500E+00
123	0.44275E+02	0.67259E+02	0.45094E+02	0.61352E+01	0.80446E+01	0.56766E+01	0.96575E+00
124	0.30780E+02	0.70093E+02	0.28251E+02	0.36647E+01	0.63381E+01	0.29764E+01	0.97768E+00
125	0.42013E+02	0.62376E+02	0.33647E+02	0.11080E+01	0.92452E+01	0.56173E+01	0.85542E+00
126	0.6346E+02	0.70472E+02	0.31715E+02	0.1151E+02	0.11182E+02	0.57318E+01	0.90237E+00
127	0.4505E+02	0.76447E+02	0.37501E+02	0.86499E+01	0.10857E+02	0.58491E+01	0.94071E+00
128	0.44265E+02	0.72646E+02	0.45001E+02	0.60177E+01	0.84047E+01	0.56308E+01	0.97224E+00
129	0.26763E+02	0.59454E+02	0.26058E+02	0.35008E+01	0.61639E+01	0.27413E+01	0.95502E+00
130	0.44450E+02	0.70752E+02	0.32741E+02	0.19515E+02	0.10744E+02	0.57658E+01	0.91367E+00
131	0.42520E+02	0.76522E+02	0.33532E+02	0.10914E+02	0.11872E+02	0.55076E+01	0.92120E+00
132	0.41273E+02	0.81413E+02	0.37490E+02	0.45427E+01	0.11255E+02	0.57224E+01	0.94115E+00









193	0.26152F+02	0.73392E+02	0.25304F+02	0.10940F+01	0.61601E+01	0.25394F+01	0.49500E+00
194	0.42418E+02	0.56020F+02	0.21897E+02	0.54063F+01	0.60993F+01	0.29882F+01	0.68510E+00
195	0.14394E+02	0.11747E+02	0.42167E+02	0.27031F+01	0.99561E+01	0.26081F+01	0.65842E+00
196	0.63494E+01	0.11145E+02	0.76074E+02	0.22596L+01	0.92825E+01	0.32977F+01	0.65975E+00
197	0.14329E+02	0.94618E+02	0.24551E+02	0.223805E+01	0.71606E+01	0.22517E+01	0.95837E+00
198	0.25744E+02	0.67461E+02	0.25543E+02	0.27992F+01	0.52594E+01	0.24802E+01	0.57234E+00
199	0.40605E+02	0.53992E+02	0.24672E+02	0.50595E+01	0.56740E+01	0.31297F+01	0.49279E+00
200	0.90173E+01	0.11002E+02	0.41269E+02	0.23759E+01	0.86225E+01	0.34394E+01	0.95552E+00
201	0.17262E+01	0.10617E+02	0.27021E+02	0.27034E+01	0.79325E+01	0.29424E+01	0.69599E+00
202	0.13066E+02	0.83552E+02	0.33505E+02	0.22213F+01	0.59121E+01	0.26404E+01	0.65841E+00
203	0.25015E+02	0.55812E+02	0.25197E+02	0.27608E+01	0.44776E+01	0.24231E+01	0.95111E+00
204	0.47741E+02	0.57692E+02	0.24874E+02	0.667126E+01	0.6718E+01	0.3506E+01	0.62618E+00
205	0.56054E+01	0.59615E+02	0.39021E+02	0.21585E+01	0.72506E+01	0.30402E+01	0.6558E+00
206	-0.19514E+01	0.75024E+02	0.34957E+02	0.17398E+01	0.67089E+01	0.26308E+01	0.65555E+00
207	0.13284E+02	0.71910E+02	0.31262E+02	0.21215E+01	0.48303E+01	0.23825E+01	0.69867E+00
208	0.29615E+02	0.5110E+02	0.25544E+02	0.14034E+01	0.43629E+01	0.26161E+01	0.96277E+00
209	0.47214E+02	0.55591E+02	0.24021E+02	0.52920E+01	0.65071E+01	0.34375E+01	0.92466E+00
210	0.41374E+01	0.62730E+02	0.37014E+02	0.70205E+01	0.60903E+01	0.27284E+01	0.69999E+00
211	-0.75548E-01	0.79112E+02	0.33173E+02	0.17093F+01	0.50733E+01	0.22173E+01	0.65941E+00
212	0.15418E+02	0.61154E+02	0.31231E+02	0.22103L+01	0.40690E+01	0.23742E+01	0.65507E+00
213	0.30929E+02	0.42256E+02	0.24805E+02	0.35534F+01	0.36690E+01	0.26013E+01	0.93156E+00
214	0.49563E+02	0.52847E+02	0.24631E+02	0.67701E+01	0.64017E+01	0.30220E+01	0.61129E+00
215	0.47702E+01	0.74464E+02	0.24989E+02	0.192225E+01	0.46870E+01	0.24179E+01	0.10000E+01
216	0.37559E+01	0.62639E+02	0.30633E+02	0.17819E+01	0.37447E+01	0.20407E+01	0.65737E+00
217	0.19714E+02	0.47466E+02	0.28087E+02	0.24126E+01	0.32294E+01	0.22321E+01	0.65739E+00
218	0.32520E+02	0.34696E+02	0.25658E+02	0.38035E+01	0.31016E+01	0.27472E+01	0.90194E+00
219	0.49104E+02	0.49875E+02	0.23551E+02	0.66662E+01	0.59899E+01	0.35147E+01	0.6874E+00
220	0.82080E+01	0.54766E+02	0.32994E+02	0.13367E+01	0.35212E+01	0.22141E+01	0.65596E+00
221	0.11051E+02	0.46122E+02	0.28274E+02	0.19833E+01	0.27208E+01	0.19521E+01	0.95201E+00
222	0.24265E+02	0.34099E+02	0.28665E+02	0.24099E+01	0.25751E+01	0.25331E+01	0.6526E+00
223	0.3347E+02	0.24441E+02	0.29221E+02	0.40583F+01	0.26095E+01	0.31176E+01	0.87755E+00
224	0.50649E+02	0.50045E+02	0.25061E+02	0.67989E+01	0.61529E+01	0.37238E+01	0.90520E+00
225	0.1440E+02	0.41074E+02	0.31304E+02	0.21474E+01	0.25555E+01	0.22276E+01	0.65599E+00
226	0.15331E+02	0.17735E+02	0.25556E+02	0.272104E+01	0.12638E+01	0.1958E+01	0.9640E+00
227	0.26140E+02	0.19534E+02	0.23060E+02	0.22231E+01	0.16175E+01	0.23402E+01	0.56010E+00
228	0.3489E+02	0.23611E+02	0.22675E+02	0.42527E+01	0.22561E+01	0.26494E+01	0.70069E+00
229	0.43197E+02	0.43149E+02	0.20041E+02	0.53718E+01	0.49567E+01	0.2418E+01	0.6596E+00
230	0.25254E+02	0.25845E+02	0.20704E+02	0.27601E+01	0.20283E+01	0.27900E+01	0.10000E+01
231	0.4023E+02	0.76777E+01	0.27094E+02	0.48552E+01	0.10653E+01	0.45744E+01	0.65507E+00
232	0.44514E+02	0.17531E+02	0.27641E+02	0.66930E+01	0.1918E+01	0.34584E+01	0.65321E+00
233	0.48256E+02	0.27791E+02	0.25867E+02	0.67067E+01	0.31812E+01	0.37276E+01	0.90027E+00
234	0.54739E+02	0.49725E+02	0.24990E+02	0.7880E+01	0.63485E+01	0.40501E+01	0.90597E+00
235	0.39505E+02	0.10767E+02	0.30947E+02	0.73294E+01	0.12894E+01	0.44396E+01	0.65599E+00
236	0.52142E+02	-0.31394E+01	0.21439E+02	0.29153E+02	0.15357E+01	0.12520E+02	0.65624E+00
237	0.39732E+02	0.84690E+01	0.34927E+02	0.43177E+01	0.11125E+01	0.51578E+01	0.92232E+00
238	0.44274E+02	0.22641E+02	0.28582E+02	0.60644E+01	0.25443E+01	0.38023E+01	0.65712E+00
239	0.53035E+02	0.44259E+02	0.28608E+02	0.25570E+01	0.59753E+01	0.42919E+01	0.9127E+00
240	0.39556E+02	0.10575E+00	0.39233E+02	0.33897E+02	0.14383E+01	0.1367E+02	0.9482E+00
241	0.67179E+02	-0.70179E+01	0.2389E+02	0.22982E+02	0.16510E+01	0.11005E+02	0.6987E+00
242	0.26262E+02	0.45094E+01	0.44413E+02	0.11256E+02	0.85552E+00	0.60825E+01	0.67445E+00
243	0.48584E+02	0.27183E+02	0.28733E+02	0.70078E+01	0.26038E+01	0.41274E+01	0.9823E+00
244	0.4783E+02	0.48201E+02	0.26736E+02	0.66384E+01	0.63132E+01	0.45187E+01	0.6178E+00
245	0.59104E+02	-0.76151E+01	0.18950E+02	0.43901E+02	0.17131E+01	0.13256E+02	0.7582E+00
246	0.25173E+02	-0.10531E+02	0.57107E+02	0.16629E+02	0.58735E+01	0.58325E+02	0.6552E+00
247	-0.87133E+01	0.10471E+01	0.61282E+02	0.16479E+02	0.92048E+00	0.76284E+01	0.5065E+00
248	0.43974E+02	0.20259E+02	0.31368E+02	0.01936E+01	0.22893E+01	0.41308E+01	0.4454E+00
249	0.5522E+02	0.45411E+02	0.7074E+02	0.70219E+01	0.46250E+01	0.46299E+01	0.6097E+00
250	0.4170E+02	-0.12942E+02	0.12718E+02	0.51748E+02	0.13585E+02	0.21346E+02	0.621E+00
251	-0.41257E+02	-0.20394E+01	0.81968E+02	0.24081E+02	0.11635E+01	0.14547E+02	0.6255E+00
252	0.1100E+02	0.3662E+01	0.56203E+02	0.10859E+02	0.85877E+00	0.5F304E+01	0.63674E+00









## RAW DATA FOR SUBJECT 2.

- CALCULATED X,Y,Z COORDINATES
- THEIR STANDARD ERROR OF ESTIMATE
- AND PROBABILITY FACTOR

LINE	ITEM	QTY	UNIT	PRICE	TOTAL	TAX	DISC	NET	GRAND
1	0.515501+02	-0.155145+01	0.752055+01	0.405035+01	0.603175+00	0.346105+01	0.100555+00	0.100555+00	0.100555+00
2	0.205410+02	0.527055+01	0.233425+02	0.400615+01	0.774065+00	0.297125+01	0.018555+02	0.018555+02	0.018555+02
3	0.247125+02	0.275255+01	0.224505+02	0.300545+01	0.212005+01	0.227125+01	0.051245+03	0.051245+03	0.051245+03
4	0.299755+02	0.505255+02	0.224505+02	0.543195+01	0.576025+01	0.326555+01	0.051975+03	0.051975+03	0.051975+03
5	0.400415+02	0.302555+00	0.104415+02	0.617815+01	0.656065+00	0.445575+01	0.125555+03	0.125555+03	0.125555+03
6	0.550425+02	-0.710755+00	0.115005+02	0.744025+01	0.677505+00	0.567375+01	0.077070+03	0.077070+03	0.077070+03
7	0.224215+02	0.655575+01	0.251375+02	0.402015+01	0.460365+00	0.325845+01	0.203265+01	0.203265+01	0.203265+01
8	0.271715+02	0.214575+02	0.211135+02	0.414665+01	0.224645+01	0.234005+01	0.212505+03	0.212505+03	0.212505+03
9	0.415155+02	0.512375+02	0.222075+02	0.559155+01	0.556265+01	0.234305+01	0.042105+03	0.042105+03	0.042105+03
10	0.536155+02	0.275625+01	0.142245+02	0.312595+01	0.494350+00	0.540045+01	0.050005+03	0.050005+03	0.050005+03
11	0.665575+02	-0.111595+01	0.053305+01	0.462115+01	0.501245+00	0.540045+01	0.137915+01	0.137915+01	0.137915+01
12	0.443325+01	0.449761+01	0.302240+02	0.404035+01	0.760625+00	0.244055+01	0.265635+02	0.265635+02	0.265635+02
13	0.270345+02	0.239575+02	0.223705+02	0.401705+01	0.224755+01	0.245665+01	0.255515+03	0.255515+03	0.255515+03
14	0.395705+02	0.512725+02	0.240945+02	0.545555+01	0.596315+01	0.391745+01	0.050255+03	0.050255+03	0.050255+03
15	0.452175+02	0.611945+01	0.176725+02	0.105275+02	0.724915+00	0.562745+01	0.052237+02	0.052237+02	0.052237+02
16	-0.751595+02	0.160275+01	0.054455+02	0.624915+02	0.179525+00	0.520045+02	0.073145+02	0.073145+02	0.073145+02
17	0.750505+01	0.522115+01	0.307075+02	0.414305+01	0.742150+00	0.260745+01	0.140025+02	0.140025+02	0.140025+02
18	0.104525+02	0.253405+02	0.320205+02	0.406325+01	0.261415+01	0.375945+01	0.051075+03	0.051075+03	0.051075+03
19	0.426745+02	0.519425+02	0.246345+02	0.606375+01	0.624375+01	0.365745+01	0.070545+03	0.070545+03	0.070545+03
20	0.270175+02	0.213125+01	0.231715+02	0.117215+02	0.691415+00	0.406745+01	0.205245+02	0.205245+02	0.205245+02
21	-0.440261+02	0.238545+01	0.430425+02	0.356195+02	0.110465+01	0.150225+02	0.140525+02	0.140525+02	0.140525+02
22	0.204525+02	0.791075+01	0.260635+02	0.478315+01	0.944155+00	0.391575+01	0.126605+01	0.126605+01	0.126605+01





23	0.34147E+02	0.25632E+02	0.31584E+02	0.55526E+01	0.28172E+01	0.35631E+01	0.32222E+00
24	0.43504E+02	0.52425E+02	0.25195E+02	0.62194E+01	0.64911E+01	0.37599E+01	0.61183E+00
25	0.42020E+02	0.27092E+01	0.23756E+02	0.17356E+02	0.67991E+00	0.76599E+01	0.41258E-03
26	0.13929E+02	0.33000E+01	0.29475E+02	0.16230E+02	0.71511E+00	0.34509E+01	0.11694E-01
27	0.37642E+02	0.11014E+02	0.25195E+02	0.55526E+01	0.14242E+01	0.44500E+01	0.13300E+00
28	0.30277E+02	0.24223E+02	0.34609E+02	0.51767E+01	0.25002E+01	0.39987E+01	0.23260E+00
29	0.44466E+02	0.53027E+02	0.24776E+02	0.63579E+01	0.66718E+01	0.37719E+01	0.65054E+00
30	0.13534E+02	0.43430E+01	0.27251E+02	0.11515E+02	0.73465E+00	0.30130E+01	0.2054E-02
31	0.10710E+02	0.49101E+01	0.24200E+02	0.12497E+02	0.75470E+00	0.31000E+01	0.32087E-02
32	0.24453E+02	0.10442E+02	0.31000E+02	0.44517E+01	0.12244E+01	0.41947E+01	0.37151E-01
33	0.43024E+02	0.25073E+02	0.25139E+02	0.56989E+01	0.27366E+01	0.41246E+01	0.25776E+00
34	0.43263E+02	0.52940E+02	0.25066E+02	0.62430E+01	0.65195E+01	0.38380E+01	0.55237E+00
35	0.12705E+02	0.57021E+01	0.24700E+02	0.10949E+02	0.60537E+00	0.31545E+01	0.31029E-02
36	0.54054E+00	0.47547E+01	0.22296E+02	0.13333E+02	0.76278E+00	0.36965E+01	0.17276E-02
37	0.29214E+02	0.11145E+02	0.22595E+02	0.67551E+01	0.13000E+01	0.42337E+01	0.34061E-01
38	0.37544E+02	0.27116E+02	0.35442E+02	0.64383E+01	0.32164E+01	0.46939E+01	0.32624E+00
39	0.45666E+02	0.56321E+02	0.24409E+02	0.45563E+01	0.70589E+01	0.37934E+01	0.65950E+00
40	0.14247E+02	0.67604E+01	0.24737E+02	0.96826E+01	0.87656E+00	0.31340E+01	0.30056E-02
41	0.25854E+02	0.47492E+01	0.31454E+02	0.10577E+02	0.12057E+01	0.42947E+01	0.12678E-01
42	0.5419E+02	0.14174E+02	0.24123E+02	0.84399E+01	0.17324E+01	0.46174E+01	0.52551E-01
43	0.34951E+02	0.27666E+02	0.25491E+02	0.67514E+01	0.33717E+01	0.48656E+01	0.78838E+00
44	0.45748E+02	0.55715E+02	0.25195E+02	0.56813E+01	0.70619E+01	0.58704E+01	0.53692E+00
45	0.29042E+02	0.10146E+02	0.31532E+02	0.96729E+01	0.12222E+01	0.41145E+01	0.10550E-01
46	0.22134E+02	0.91910E+01	0.34122E+02	0.96790E+01	0.10625E+01	0.34720E+01	0.67379E-02
47	0.26187E+02	0.12034E+02	0.34047E+02	0.77804E+01	0.13131E+01	0.39936E+01	0.15689E-01
48	0.40205E+02	0.24919E+02	0.26955E+02	0.69702E+01	0.36058E+01	0.50342E+01	0.30129E+00
49	0.7251E+02	0.57725E+02	0.24402E+02	0.68890E+01	0.73335E+01	0.34807E+01	0.61195E+00
50	0.32507E+02	0.11472E+02	0.34141E+02	0.95543E+01	0.14417E+01	0.46142E+01	0.21423E-01
51	0.33340E+02	0.12611E+02	0.33609E+02	0.95863E+01	0.15348E+01	0.45030E+01	0.12177E-01
52	0.45444E+02	0.14691E+02	0.33751E+02	0.99204E+01	0.25858E+01	0.52536E+01	0.45579E-01
53	0.38552E+02	0.29355E+02	0.38742E+02	0.68693E+01	0.36181E+01	0.52033E+01	0.21624E+00
54	0.46326E+02	0.57144E+02	0.25775E+02	0.60403E+01	0.73450E+01	0.35690E+01	0.53210E+00
55	0.4700E+02	0.17249E+02	0.33524E+02	0.10841E+02	0.24546E+01	0.52477E+01	0.50728E-01
56	0.54735E+02	0.20433E+02	0.23705E+02	0.12142E+02	0.31413E+01	0.57890E+01	0.52100E-01
57	0.54541E+02	0.22950E+02	0.25354E+02	0.11351E+02	0.37250E+01	0.60943E+01	0.15092E+00
58	0.35424E+02	0.32141E+02	0.35616E+02	0.76321E+01	0.43135E+01	0.57103E+01	0.78200E+00
59	0.47423E+02	0.58699E+02	0.25050E+02	0.79727E+01	0.75844E+01	0.74747E+01	0.60842E+00
60	0.56983E+02	0.21433E+02	0.35290E+02	0.12613E+02	0.35330E+01	0.62823E+01	0.59476E-01
61	0.59246E+02	0.24165E+02	0.16207E+02	0.13066E+02	0.40173E+01	0.64442E+01	0.84923E-01
62	0.57763E+02	0.27742E+02	0.26693E+02	0.11912E+02	0.45101E+01	0.65127E+01	0.16205E+00
63	0.43427E+02	0.24209E+02	0.41462E+02	0.77423E+01	0.45851E+01	0.55742E+01	0.26375E+00
64	0.4490E+02	0.57194E+02	0.27919E+02	0.67147E+01	0.73571E+01	0.41820E+01	0.50674E+00
65	0.4231E+02	0.27921E+02	0.14271E+02	0.13630E+02	0.47956E+01	0.65071E+01	0.11831E+00
66	0.6550E+02	0.24363E+02	0.33271E+02	0.13450E+02	0.51066E+01	0.62064E+01	0.67556E-01
67	0.46655E+02	0.30560E+02	0.42133E+02	0.11718E+02	0.49828E+01	0.64105E+01	0.13011E+00
68	0.46655E+02	0.31284E+02	0.25336E+02	0.11612E+02	0.51664E+01	0.64209E+01	0.27300E+00
69	0.4711E+02	0.60594E+02	0.25336E+02	0.70401E+01	0.73851E+01	0.40215E+01	0.59175E+00
70	0.71457E+02	0.31672E+02	0.30657E+02	0.14840E+02	0.56107E+01	0.61676E+01	0.43664E-01
71	0.82354E+02	0.39105E+02	0.32136E+02	0.17915E+02	0.76261E+01	0.71042E+01	0.14543E+00
72	0.6808E+02	0.37071E+02	0.25500E+02	0.14321E+02	0.68661E+01	0.70584E+01	0.20370E+00
73	0.44351E+02	0.345261E+02	0.43009E+02	0.74414E+01	0.52716E+01	0.62704E+01	0.27203E+00
74	0.48134E+02	0.60150E+02	0.25424E+02	0.72243E+01	0.79294E+01	0.40964E+01	0.50402E+00
75	0.49544E+02	0.60139E+02	0.11303E+02	0.17392E+02	0.86304E+01	0.74411E+01	0.31647E+00
76	0.43654E+02	0.47975E+02	0.24970E+02	0.14911E+02	0.94841E+01	0.70174E+01	0.20658E+00
77	0.69452E+02	0.42339E+02	0.25929E+02	0.14455E+02	0.77628E+01	0.71744E+01	0.21356E+00
78	0.50714E+02	0.42339E+02	0.41594E+02	0.25544E+02	0.63446E+01	0.67402E+01	0.75155E+00
79	0.48674E+02	0.60713E+02	0.25544E+02	0.73053E+01	0.80324E+01	0.40944E+01	0.52026E+00
80	0.47251E+02	0.60311E+02	0.29436E+02	0.17144E+02	0.51560E+01	0.76015E+01	0.25573E+00
81	0.47345E+02	0.42551E+02	0.31462E+02	0.12031E+02	0.59375E+01	0.72933E+01	0.61037E+00
82	0.70669E+02	0.45451E+02	0.36434E+02	0.14712E+02	0.85100E+01	0.73197E+01	0.70141E+00





83	0.50453E+02	0.46140E+02	0.44077E+02	0.91852E+01	0.65383E+01	0.70637E+01	0.31408E+00
84	0.49460E+02	0.42923E+02	0.23306E+02	0.72392E+01	0.81819E+01	0.31471E+01	0.52890E+00
85	0.48255E+02	0.41755E+02	0.13424E+02	0.11842E+02	0.97700E+01	0.74577E+01	0.11866E+00
86	0.95255E+02	0.54561E+02	0.32043E+02	0.22440E+02	0.12486E+02	0.80510E+01	0.27106E+00
87	0.79746E+02	0.54267E+02	0.32107E+02	0.17582E+02	0.11028E+02	0.83381E+01	0.27616E+00
88	0.52511E+02	0.50479E+02	0.44617E+02	0.30592E+01	0.78207E+01	0.73511E+01	0.32476E+00
89	0.49051E+02	0.41141E+02	0.24667E+02	0.72926E+01	0.85018E+01	0.40077E+01	0.51652E+00
90	0.92334E+02	0.57766E+02	0.33528E+02	0.20700E+02	0.12110E+02	0.80414E+01	0.28098E+00
91	0.10161E+03	0.64355E+02	0.40721E+02	0.22931E+02	0.14170E+02	0.78514E+01	0.14444E+00
92	0.80607E+02	0.41340E+02	0.37561E+02	0.17659E+02	0.12472E+02	0.83334E+01	0.34424E+00
93	0.55724E+02	0.56233E+02	0.44449E+02	0.10455E+02	0.52029E+01	0.70832E+01	0.12084E+00
94	0.52550E+02	0.41347E+02	0.23775E+02	0.78818E+01	0.89032E+01	0.40833E+01	0.61015E+00
95	0.94554E+02	0.65434E+02	0.33154E+02	0.21102E+02	0.13826E+02	0.81041E+01	0.34407E+00
96	0.95240E+02	0.71174E+02	0.35070E+02	0.21904E+02	0.15508E+02	0.80004E+01	0.51214E+00
97	0.78431E+02	0.41777E+02	0.40567E+02	0.17293E+02	0.13132E+02	0.88805E+01	0.34145E+00
98	0.56546E+02	0.60664E+02	0.45570E+02	0.10677E+02	0.10084E+02	0.79743E+01	0.39432E+00
99	0.51475E+02	0.56291E+02	0.22680E+02	0.75384E+01	0.87309E+01	0.38535E+01	0.61169E+00
100	0.87231E+02	0.67322E+02	0.41450E+02	0.20463E+02	0.14815E+02	0.94017E+01	0.36357E+00
101	0.89255E+02	0.72608E+02	0.41421E+02	0.21214E+02	0.16258E+02	0.55480E+01	0.35162E+00
102	0.86845E+02	0.71754E+02	0.40717E+02	0.18027E+02	0.14909E+02	0.91402E+01	0.35552E+00
103	0.57326E+02	0.66714E+02	0.42495E+02	0.10664E+02	0.11086E+02	0.74550E+01	0.42103E+00
104	0.54484E+02	0.65921E+02	0.19362E+02	0.75475E+01	0.84030E+01	0.36649E+01	0.76175E+00
105	0.87701E+02	0.72327E+02	0.40678E+02	0.20473E+02	0.15909E+02	0.56103E+01	0.31364E+00
106	0.89708E+02	0.76650E+02	0.40114E+02	0.21067E+02	0.17477E+02	0.56274E+01	0.35664E+00
107	0.77007E+02	0.74490E+02	0.40613E+02	0.16622E+02	0.15098E+02	0.86783E+01	0.35281E+00
108	0.59184E+02	0.71742E+02	0.40897E+02	0.11064E+02	0.12132E+02	0.72843E+01	0.46092E+00
109	0.55131E+02	0.65935E+02	0.41177E+02	0.74284E+01	0.82194E+01	0.25679E+01	0.82450E+00
110	0.96016E+02	0.81814E+02	0.37034E+02	0.22449E+02	0.18284E+02	0.52405E+01	0.46331E+00
111	0.89825E+02	0.84189E+02	0.40425E+02	0.20837E+02	0.18738E+02	0.57894E+01	0.36737E+00
112	0.74581E+02	0.60204E+02	0.41362E+02	0.15935E+02	0.15998E+02	0.88131E+01	0.41452E+00
113	0.59010E+02	0.77077E+02	0.41712E+02	0.11012E+02	0.13061E+02	0.75601E+01	0.53950E+00
114	0.58525E+02	0.64344E+02	0.16224E+02	0.76835E+01	0.78334E+01	0.35143E+01	0.77573E+00
115	0.88564E+02	0.83556E+02	0.40664E+02	0.20544E+02	0.18493E+02	0.67413E+01	0.43455E+00
116	0.85024E+02	0.87144E+02	0.38767E+02	0.19165E+02	0.19567E+02	0.65013E+01	0.36648E+00
117	0.76470E+02	0.87324E+02	0.28103E+02	0.16807E+02	0.17328E+02	0.82453E+01	0.45245E+00
118	0.59320E+02	0.83314E+02	0.41314E+02	0.10940E+02	0.14102E+02	0.75266E+01	0.63923E+00
119	0.56864E+02	0.63950E+02	0.19143E+02	0.77859E+01	0.80565E+01	0.46164E+01	0.70765E+00
120	0.86255E+02	0.88678E+02	0.36783E+02	0.19171E+02	0.18685E+02	0.85822E+01	0.42616E+00
121	0.75622E+02	0.94660E+02	0.40524E+02	0.16154E+02	0.19882E+02	0.67710E+01	0.47526E+00
122	0.39462E+01	0.91584E+02	0.44220E+02	0.23141E+01	0.62883E+01	0.35627E+01	0.72139E+00
123	0.23540E+02	0.85744E+02	0.31679E+02	0.20125E+01	0.13372E+02	0.65192E+01	0.36697E+00
124	0.60141E+02	0.61846E+02	0.41814E+02	0.13191E+01	0.79971E+01	0.37913E+01	0.80756E+00
125	0.74753E+02	0.94827E+02	0.41744E+02	0.15946E+02	0.19034E+02	0.89726E+01	0.44506E+00
126	0.69350E+02	0.19262E+03	0.41812E+02	0.14270E+02	0.10691E+02	0.85487E+01	0.52256E+00
127	0.61223E+02	0.93676E+02	0.36518E+02	0.11524E+02	0.16243E+02	0.73475E+01	0.54797E+00
128	0.52135E+02	0.81342E+02	0.21294E+02	0.84787E+01	0.12221E+02	0.52207E+01	0.65814E+00
129	0.61620E+02	0.62172E+02	0.217574E+02	0.44580E+01	0.72921E+01	0.37781E+01	0.76469E+00
130	0.68524E+02	0.97967E+02	0.41513E+02	0.19151E+02	0.12563E+02	0.84334E+01	0.53150E+00
131	0.61449E+02	0.10672E+03	0.40751E+02	0.11706E+02	0.18783E+02	0.77153E+01	0.58698E+00
132	0.56778E+02	0.46594E+02	0.36072E+02	0.13010E+02	0.15536E+02	0.65971E+01	0.60518E+00
133	0.50284E+02	0.81414E+02	0.26000E+02	0.76370E+01	0.11122E+02	0.45337E+01	0.64513E+00
134	0.61412E+02	0.62234E+02	0.18234E+02	0.86122E+01	0.81248E+01	0.38217E+01	0.65012E+00
135	0.62373E+02	0.10172E+03	0.40344E+02	0.11930E+02	0.17880E+02	0.71654E+01	0.55555E+00
136	0.53674E+02	0.10759E+03	0.40756E+02	0.43667E+01	0.17292E+02	0.70505E+01	0.67647E+00
137	0.53173E+02	0.57800E+02	0.24214E+02	0.80574E+01	0.14946E+02	0.56450E+01	0.66745E+00
138	0.51473E+02	0.42498E+02	0.23394E+02	0.75610E+01	0.11041E+02	0.40806E+01	0.80425E+00
139	0.64513E+02	0.60803E+02	0.15764E+02	0.44862E+01	0.75344E+01	0.36977E+01	0.71420E+00
140	0.55256E+02	0.10244E+03	0.39201E+02	0.94244E+01	0.16631E+02	0.66621E+01	0.67142E+00
141	0.37357E+02	0.11054E+03	0.37027E+02	0.75324E+01	0.51099E+02	0.55220E+01	0.67215E+00
142	0.47920E+02	0.99290E+02	0.36324E+02	0.76925E+01	0.14215E+02	0.55079E+01	0.77150E+00



143	0.50851E+02	0.81425E+02	0.22141E+02	0.72271E+01	0.10612E+02	0.39215E+01	0.92061E+00
144	0.65110E+02	0.58359E+02	0.16427E+02	0.87884E+01	0.78050E+01	0.37848E+01	0.6F0C3E+00
145	0.49723E+02	0.10688E+03	0.27428E+02	0.82975E+01	0.16008E+02	0.61428E+01	0.71997E+00
146	0.40475E+02	0.11157E+03	0.35140E+02	0.81653E+01	0.14604E+02	0.51621E+01	0.84182E+00
147	0.43085E+02	0.92594E+02	0.21245E+02	0.65589E+01	0.12487E+02	0.50197E+01	0.84885E+00
148	0.51603E+02	0.77793E+02	0.21729E+02	0.72760E+01	0.10103E+02	0.38924E+01	0.94130E+00
149	0.60578E+02	0.57179E+02	0.22175E+02	0.94260E+01	0.78958E+01	0.42215E+01	0.43337E+00
150	0.40854E+02	0.10635E+03	0.25297E+02	0.63655E+01	0.14147E+02	0.51375E+01	0.77054E+00
151	0.34205E+02	0.11294E+03	0.10740E+02	0.88624E+01	0.13172E+02	0.41548E+01	0.92483E+00
152	0.38976E+02	0.96553E+02	0.25270E+02	0.55377E+01	0.11607E+02	0.41997E+01	0.99021E+00
153	0.48616E+02	0.73950E+02	0.16920E+02	0.60711E+01	0.85011E+01	0.21889E+01	0.30371E+00
154	0.62571E+02	0.50061E+02	0.21994E+02	0.99083E+01	0.78248E+01	0.43067E+01	0.81372E+00
155	0.36116E+02	0.10810E+03	0.32902E+02	0.52539E+01	0.13072E+02	0.46254E+01	0.60370E+00
156	0.27128E+02	0.10987E+03	0.27687E+02	0.36522E+01	0.11130E+02	0.33724E+01	0.89034E+00
157	0.34652E+02	0.92843E+02	0.26523E+02	0.46289E+01	0.10318E+02	0.36034E+01	0.94007E+00
158	0.48765E+02	0.69215E+02	0.15104E+02	0.57586E+01	0.75901E+01	0.30080E+01	0.92283E+00
159	0.59744E+02	0.55762E+02	0.15617E+02	0.10573E+02	0.79415E+01	0.43712E+01	0.63332E+00
160	0.28533E+02	0.10536E+03	0.71495E+02	0.39891E+01	0.11096E+02	0.38275E+01	0.97377E+00
161	0.22132E+02	0.10424E+03	0.27271E+02	0.77499E+01	0.94834E+01	0.25227E+01	0.90999E+00
162	0.31578E+02	0.86294E+02	0.25521E+02	0.41282E+01	0.90206E+01	0.33066E+01	0.55790E+00
163	0.47609E+02	0.64057E+02	0.18121E+02	0.60810E+01	0.74099E+01	0.32294E+01	0.62329E+00
164	0.71567E+02	0.53640E+02	0.21478E+02	0.11648E+02	0.81621E+01	0.47767E+01	0.56804E+00
165	0.24063E+02	0.10031E+03	0.26904E+02	0.32407E+01	0.94410E+01	0.32345E+01	0.95587E+00
166	0.16227E+02	0.97184E+02	0.22017E+02	0.22857E+01	0.76140E+01	0.22707E+01	0.92190E+00
167	0.20497E+02	0.78869E+02	0.22626E+02	0.37313E+01	0.77747E+01	0.25169E+01	0.94492E+00
168	0.50952E+02	0.58650E+02	0.17618E+02	0.65423E+01	0.69836E+01	0.32744E+01	0.96376E+00
169	0.66146E+02	0.40794E+02	0.25413E+02	0.11356E+02	0.79100E+01	0.44827E+01	0.37923E+00
170	0.21648E+02	0.93098E+02	0.24852E+02	0.28417E+01	0.81069E+01	0.27200E+01	0.97309E+00
171	0.15519E+02	0.82630E+02	0.17744E+02	0.20295E+01	0.59931E+01	0.18642E+01	0.57749E+00
172	0.32865E+02	0.67192E+02	0.18456E+02	0.37399E+01	0.65363E+01	0.21325E+01	0.88371E+00
173	0.51844E+02	0.51895E+02	0.17775E+02	0.67157E+01	0.62074E+01	0.33894E+01	0.95751E+00
174	0.67557E+02	0.49318E+02	0.27097E+02	0.12034E+02	0.75904E+01	0.53409E+01	0.26788E+00
175	0.21229E+02	0.80499E+02	0.22039E+02	0.26279E+01	0.66218E+01	0.24905E+01	0.81004E+00
176	0.17248E+02	0.57931E+02	0.13276E+02	0.19673E+01	0.39646E+01	0.15377E+01	0.46841E+00
177	0.33262E+02	0.49135E+02	0.17284E+02	0.37655E+01	0.46750E+01	0.24704E+01	0.94592E+00
178	0.53219E+02	0.42778E+02	0.20027E+02	0.75279E+01	0.53832E+01	0.36595E+01	0.70522E+00
179	0.75257E+02	0.52792E+02	0.26252E+02	0.13585E+02	0.84165E+01	0.50927E+01	0.654122E+00
180	0.22395E+02	0.57333E+02	0.17385E+02	0.24832E+01	0.45119E+01	0.19953E+01	0.81174E+00
181	0.22521E+02	0.81433E+02	0.13464E+02	0.22501E+01	0.31186E+01	0.10969E+01	0.26194E+00
182	0.41029E+02	0.37217E+02	0.16977E+02	0.49211E+01	0.39266E+01	0.24309E+01	0.55106E+00
183	0.27650E+02	0.38625E+02	0.25119E+02	0.92918E+01	0.55033E+01	0.46352E+01	0.71951E+00
184	0.75162E+02	0.52802E+02	0.28799E+02	0.14138E+02	0.92621E+01	0.61628E+01	0.51727E+00
185	0.28737E+02	0.41714E+02	0.17038E+02	0.30245E+01	0.36307E+01	0.21635E+01	0.51920E+00
186	0.24365E+02	0.18297E+02	0.75504E+01	0.28611E+01	0.16655E+01	0.17951E+01	0.14497E+02
187	0.48002E+02	0.25652E+02	0.14057E+02	0.55708E+01	0.28085E+01	0.24574E+01	0.98191E+00
188	0.62529E+02	0.32963E+02	0.23801E+02	0.10397E+02	0.44832E+01	0.47034E+01	0.57745E+00
189	0.77644E+02	0.52017E+02	0.26798E+02	0.14354E+02	0.90025E+01	0.55088E+01	0.54863E+00
190	0.38084E+02	0.26716E+02	0.15466E+02	0.42402E+01	0.27345E+01	0.20234E+01	0.65200E+00
191	0.49793E+02	0.59772E+01	0.77278E+01	0.49861E+01	0.12745E+01	0.30125E+01	0.80184E+03
192	0.62787E+02	0.14792E+02	0.11736E+02	0.76334E+01	0.20215E+01	0.37729E+01	0.76876E+00
193	0.78244E+02	0.30555E+02	0.18994E+02	0.11380E+02	0.44454E+01	0.47360E+01	0.90008E+00
194	0.79454E+02	0.52930E+02	0.27019E+02	0.14874E+02	0.92975E+01	0.60457E+01	0.53976E+00
195	0.53221E+02	0.95515E+01	0.10201E+02	0.60322E+01	0.15519E+01	0.22526E+01	0.92550E+01

FIT IS STOPPED AFTER TOO MANY CONSECUTIVE DIVERGENCES. = 11

196	0.46770E+02	0.29779E+01	0.31306E+02	0.10297E+02	0.11020E+01	0.61658E+01	0.28327E+02
197	0.74572E+02	0.85513E+01	0.12566E+02	0.10751E+02	0.17771E+01	0.55140E+01	0.67795E+00
198	0.75668E+02	0.20813E+02	0.22146E+02	0.13160E+02	0.47117E+01	0.51871E+01	0.52402E+00
199	0.60225E+02	0.51552E+02	0.26612E+02	0.14987E+02	0.50908E+01	0.60401E+01	0.55103E+00





FIT IS STOPPED AFTER TOO MANY CONSECUTIVE DIFFERENCES. = 11

200	0.7850E+02	0.5158E+01	0.3074E+02	0.1930E+02	0.1968E+01	0.1034E+02	0.2160E+02	0.2160E+02
201	0.6656E+02	0.5270E+01	0.3120E+02	0.1656E+02	0.1352E+01	0.7232E+01	0.1738E+00	0.1738E+00
202	0.6805E+02	0.4850E+01	0.2651E+02	0.2048E+02	0.1366E+01	0.1015E+02	0.3374E+00	0.3374E+00
203	0.6245E+02	0.2670E+02	0.2212E+02	0.1480E+02	0.2455E+01	0.5715E+01	0.4505E+00	0.4505E+00
204	0.6085E+02	0.5307E+02	0.2614E+02	0.1494E+02	0.9250E+01	0.3070E+01	0.5745E+00	0.5745E+00
205	0.6598E+02	0.4452E+01	0.2774E+02	0.1749E+02	0.1200E+01	0.4040E+01	0.7252E+00	0.7252E+00
206	0.1075E+03	0.9769E+01	0.1415E+02	0.1546E+02	0.1742E+01	0.7258E+01	0.9577E+00	0.9577E+00
207	0.1954E+02	0.2694E+01	0.4610E+02	0.3598E+02	0.1115E+01	0.1206E+02	0.3142E+01	0.3142E+01
208	0.7064E+02	0.2540E+02	0.2708E+02	0.1415E+02	0.4300E+01	0.5855E+01	0.2536E+00	0.2536E+00
209	0.6058E+02	0.5375E+02	0.2668E+02	0.1506E+02	0.9454E+01	0.6040E+01	0.5436E+00	0.5436E+00
210	0.1117E+03	0.6586E+01	0.1112E+02	0.1490E+02	0.1312E+01	0.8261E+01	0.9710E+00	0.9710E+00
211	0.2462E+03	0.2897E+01	0.1006E+03	0.2620E+03	0.5217E+01	0.1054E+03	0.7275E+01	0.7275E+01
212	0.1116E+03	0.4757E+01	0.9499E+02	0.3492E+02	0.3283E+01	0.4951E+02	0.5027E+01	0.5027E+01
213	0.6525E+02	0.2472E+02	0.3169E+02	0.1381E+02	0.4205E+01	0.6176E+01	0.1476E+00	0.1476E+00
214	0.6141E+02	0.5427E+02	0.2903E+02	0.1599E+02	0.9985E+01	0.6514E+01	0.4603E+00	0.4603E+00
215	0.1215E+03	0.2058E+01	0.1099E+02	0.1722E+02	0.1150E+01	0.8134E+01	0.4343E+00	0.4343E+00
216	0.1747E+03	0.2084E+01	0.1331E+03	0.1378E+03	0.3395E+01	0.8553E+02	0.3024E+01	0.3024E+01
217	0.7362E+01	0.70574E+01	0.4620E+02	0.1664E+02	0.9370E+00	0.4582E+01	0.2717E+01	0.2717E+01
218	0.5437E+02	0.2341E+02	0.3614E+02	0.1670E+02	0.3664E+01	0.6287E+01	0.1086E+00	0.1086E+00
219	0.8016E+02	0.5483E+02	0.3071E+02	0.1619E+02	0.1020E+02	0.6817E+01	0.4445E+00	0.4445E+00
220	0.1737E+03	0.1955E+01	0.4299E+02	0.7104E+02	0.1847E+01	0.3133E+02	0.1741E+00	0.1741E+00
221	0.7055E+00	0.7576E+01	0.5116E+02	0.1680E+02	0.9797E+00	0.5713E+01	0.1532E+01	0.1532E+01
222	0.2602E+02	0.1156E+02	0.4625E+02	0.1136E+02	0.1341E+01	0.5821E+01	0.3615E+01	0.3615E+01
223	0.6254E+02	0.2710E+02	0.3742E+02	0.1362E+02	0.4680E+01	0.7137E+01	0.1720E+00	0.1720E+00
224	0.6352E+02	0.1154E+03	0.2614E+02	0.1724E+02	0.1170E+02	0.7213E+01	0.4572E+00	0.4572E+00
225	0.5303E+04	0.1154E+03	0.2614E+02	0.1724E+02	0.1170E+02	0.7213E+01	0.4572E+00	0.4572E+00
226	0.2880E+02	0.1120E+02	0.3904E+02	0.1705E+02	0.1337E+01	0.5957E+01	0.1449E+00	0.1449E+00
227	0.1063E+03	0.2912E+02	0.3904E+02	0.2492E+02	0.7045E+01	0.1094E+02	0.3854E+00	0.3854E+00
228	0.7210E+02	0.3186E+02	0.3670E+02	0.1613E+02	0.6119E+01	0.8292E+01	0.2489E+00	0.2489E+00
229	0.8034E+02	0.5818E+02	0.3612E+02	0.1766E+02	0.1161E+02	0.7982E+01	0.7026E+00	0.7026E+00
230	0.6862E+02	0.6459E+01	0.5001E+02	0.7566E+02	0.1327E+02	0.4028E+02	0.2500E+00	0.2500E+00
231	0.1322E+02	0.1817E+02	0.4721E+02	0.1937E+02	0.3292E+01	0.9483E+01	0.1106E+00	0.1106E+00
232	0.8978E+02	0.2909E+02	0.4474E+02	0.2492E+02	0.5922E+01	0.1110E+02	0.2779E+00	0.2779E+00
233	0.7322E+02	0.3375E+02	0.4261E+02	0.1701E+02	0.6080E+01	0.9111E+01	0.3205E+00	0.3205E+00
234	0.6507E+02	0.6101E+02	0.3704E+02	0.1881E+02	0.1260E+02	0.8533E+01	0.3202E+00	0.3202E+00
235	0.1125E+02	0.7604E+01	0.6207E+02	0.3479E+02	0.1363E+01	0.1154E+02	0.2611E+00	0.2611E+00
236	0.7304E+02	0.2306E+02	0.5042E+02	0.2147E+02	0.4764E+01	0.1114E+02	0.1632E+00	0.1632E+00
237	0.8900E+02	0.2412E+02	0.4900E+02	0.2487E+02	0.6532E+01	0.1219E+02	0.2225E+00	0.2225E+00
238	0.7695E+02	0.3706E+02	0.8613E+02	0.1430E+02	0.7704E+01	0.1022E+02	0.3491E+00	0.3491E+00
239	0.6534E+02	0.6122E+02	0.3901E+02	0.1929E+02	0.1343E+02	0.9093E+01	0.4611E+00	0.4611E+00
240	0.7344E+01	0.1134E+02	0.6747E+02	0.1609E+02	0.1218E+01	0.8445E+01	0.0195E+01	0.0195E+01
241	0.6573E+02	0.2395E+02	0.5390E+02	0.2036E+02	0.4825E+01	0.1149E+02	0.1620E+00	0.1620E+00
242	0.6046E+02	0.3100E+02	0.5153E+02	0.2588E+02	0.7451E+01	0.1313E+02	0.3024E+00	0.3024E+00
243	0.7731E+02	0.3825E+02	0.4840E+02	0.1878E+02	0.8091E+01	0.1092E+02	0.3405E+00	0.3405E+00
244	0.4767E+02	0.6604E+02	0.3967E+02	0.2019E+02	0.1434E+02	0.9420E+01	0.4617E+00	0.4617E+00
245	0.1310E+02	0.1302E+02	0.6542E+02	0.1558E+02	0.1354E+01	0.7391E+01	0.2332E+01	0.2332E+01
246	0.8145E+02	0.2634E+02	0.5875E+02	0.2401E+02	0.6013E+01	0.1084E+02	0.2300E+00	0.2300E+00
247	0.1065E+03	0.7091E+02	0.5290E+02	0.2994E+02	0.8550E+01	0.1400E+02	0.3670E+00	0.3670E+00
248	0.8357E+02	0.6217E+02	0.4941E+02	0.2098E+02	0.9470E+01	0.1179E+02	0.3724E+00	0.3724E+00
249	0.9176E+02	0.6410E+02	0.3911E+02	0.2147E+02	0.1512E+02	0.6574E+01	0.4440E+00	0.4440E+00
250	0.2692E+02	0.1642E+02	0.6566E+02	0.1379E+02	0.1892E+01	0.9073E+01	0.1370E+00	0.1370E+00
251	0.8597E+02	0.2737E+02	0.6900E+02	0.2707E+02	0.9567E+01	0.1507E+02	0.2522E+00	0.2522E+00
252	0.1034E+01	0.3551E+02	0.5622E+02	0.1153E+02	0.9547E+01	0.1593E+02	0.3564E+00	0.3564E+00
253	0.8549E+02	0.6442E+02	0.5293E+02	0.2201E+02	0.1029E+02	0.1243E+02	0.3430E+00	0.3430E+00
254	0.0568E+02	0.6631E+02	0.3064E+02	0.2268E+02	0.1542E+02	0.9675E+01	0.5041E+00	0.5041E+00
255	0.3283E+02	0.1774E+02	0.7163E+02	0.1725E+02	0.2245E+01	0.1040E+02	0.1625E+00	0.1625E+00
256	0.8593E+02	0.2540E+02	0.6091E+02	0.2483E+02	0.6121E+01	0.1545E+02	0.2521E+00	0.2521E+00
257	0.9622E+02	0.3593E+02	0.5849E+02	0.4231E+02	0.9270E+01	0.1575E+02	0.3355E+00	0.3355E+00
258	0.8840E+02	0.4766E+02	0.5494E+02	0.2340E+02	0.1142E+02	0.1363E+02	0.3942E+00	0.3942E+00





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* 259 ** 0.95021E+02 * 0.69280E+02 * 0.39446E+02 ** 0.22750E+02 * 0.15742E+02 * 0.59497E+01 ** 0.42315E+00 *
* 260 ** 0.48771E+02 * 0.21505E+02 * 0.7162E+02 * 0.18743E+02 * 0.34330E+01 * 0.12531E+02 ** 0.20E28F+00 *
* 261 ** 0.93844E+02 * 0.27762E+02 * 0.63173E+02 * 0.31526E+02 * 0.71942E+01 * 0.17195E+02 ** 0.29E85E+00 *
* 262 ** 0.45044E+02 * 0.14524E+02 * 0.62530E+02 * 0.24473E+02 * 0.41304E+01 * 0.15497E+02 ** 0.30E33E+00 *
* 263 ** 0.87872E+02 * 0.47620E+02 * 0.58230E+02 * 0.23512E+02 * 0.11435E+02 * 0.14564E+02 ** 0.36815E+00 *
* 264 ** 0.96023E+02 * 0.69921E+02 * 0.79137E+02 * 0.23033E+02 * 0.15942E+02 * 0.59476E+01 ** 0.44542E+00 *
* 265 ** 0.44444E+02 * 0.23202E+02 * 0.72135E+02 * 0.14597E+02 * 0.40351E+01 * 0.13553E+02 ** 0.23208E+00 *
* 266 ** 0.04170E+02 * 0.26872E+02 * 0.66904E+02 * 0.30735E+02 * 0.67472E+01 * 0.10220E+02 ** 0.32128E+00 *
* 267 ** 0.42400E+02 * 0.37217E+02 * 0.65574E+02 * 0.26599E+02 * 0.93359E+01 * 0.17037E+02 ** 0.34025E+00 *
* 268 ** 0.07747E+02 * 0.51221E+02 * 0.59660E+02 * 0.33911E+02 * 0.12417E+02 * 0.14947E+02 ** 0.39059E+00 *
* 269 ** 0.56920E+02 * 0.70659E+02 * 0.39881E+02 * 0.23310E+02 * 0.16327E+02 * 0.10117E+02 ** 0.44605E+00 *
* 270 ** 0.58196E+02 * 0.25204E+02 * 0.75095E+02 * 0.20026E+02 * 0.45992E+01 * 0.14655E+02 ** 0.25081E+00 *
* 271 ** 0.47747E+02 * 0.27244E+02 * 0.70440E+02 * 0.30647E+02 * 0.68322E+01 * 0.14581E+02 ** 0.32333E+00 *
* 272 ** 0.48790E+02 * 0.37648E+02 * 0.67518E+02 * 0.26076E+02 * 0.99307E+01 * 0.17555E+02 ** 0.34369E+00 *
* 273 ** 0.46440E+02 * 0.14592E+02 * 0.64448E+02 * 0.27092E+02 * 0.14723E+02 * 0.15856E+02 ** 0.42433E+00 *
* 274 ** 0.49747E+02 * 0.70494E+02 * 0.39519E+02 * 0.24444E+02 * 0.16613E+02 * 0.10216E+02 ** 0.45773E+00 *
* 275 ** 0.60566E+02 * 0.27177E+02 * 0.77106E+02 * 0.42019E+02 * 0.51490E+01 * 0.15490E+02 ** 0.42746E+00 *
* 276 ** 0.71161E+02 * 0.27194E+02 * 0.73850E+02 * 0.23785E+02 * 0.58060E+01 * 0.16617E+02 ** 0.27478E+00 *
* 277 ** 0.47190E+02 * 0.37951E+02 * 0.70348E+02 * 0.23649E+02 * 0.89837E+01 * 0.17186E+02 ** 0.21553E+00 *
* 278 ** 0.96721E+02 * 0.56604E+02 * 0.60594E+02 * 0.27240E+02 * 0.14808E+02 * 0.16375E+02 ** 0.42584E+00 *
* 279 ** 0.78330E+02 * 0.70944E+02 * 0.39871E+02 * 0.22194E+02 * 0.16518E+02 * 0.10233E+02 ** 0.47575E+00 *
* 280 ** 0.65705E+02 * 0.29404E+02 * 0.76544E+02 * 0.20564E+02 * 0.54759E+01 * 0.16154E+02 ** 0.24367E+00 *
* 281 ** 0.00571E+02 * 0.33457E+02 * 0.75713E+02 * 0.42998E+02 * 0.87027E+01 * 0.20618E+02 ** 0.35194E+00 *
* 282 ** 0.42004E+02 * 0.43194E+02 * 0.71513E+02 * 0.27449E+02 * 0.11214E+02 * 0.19084E+02 ** 0.36578E+00 *
* 283 ** 0.96152E+02 * 0.54814E+02 * 0.60726E+02 * 0.26948E+02 * 0.15339E+02 * 0.16340E+02 ** 0.41787E+00 *
* 284 ** 0.49167E+02 * 0.71197E+02 * 0.40722E+02 * 0.24530E+02 * 0.16799E+02 * 0.10526E+02 ** 0.46441E+00 *
* 285 ** 0.72545E+02 * 0.33232E+02 * 0.78194E+02 * 0.22157E+02 * 0.72431E+01 * 0.17840E+02 ** 0.31475E+00 *
* **
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